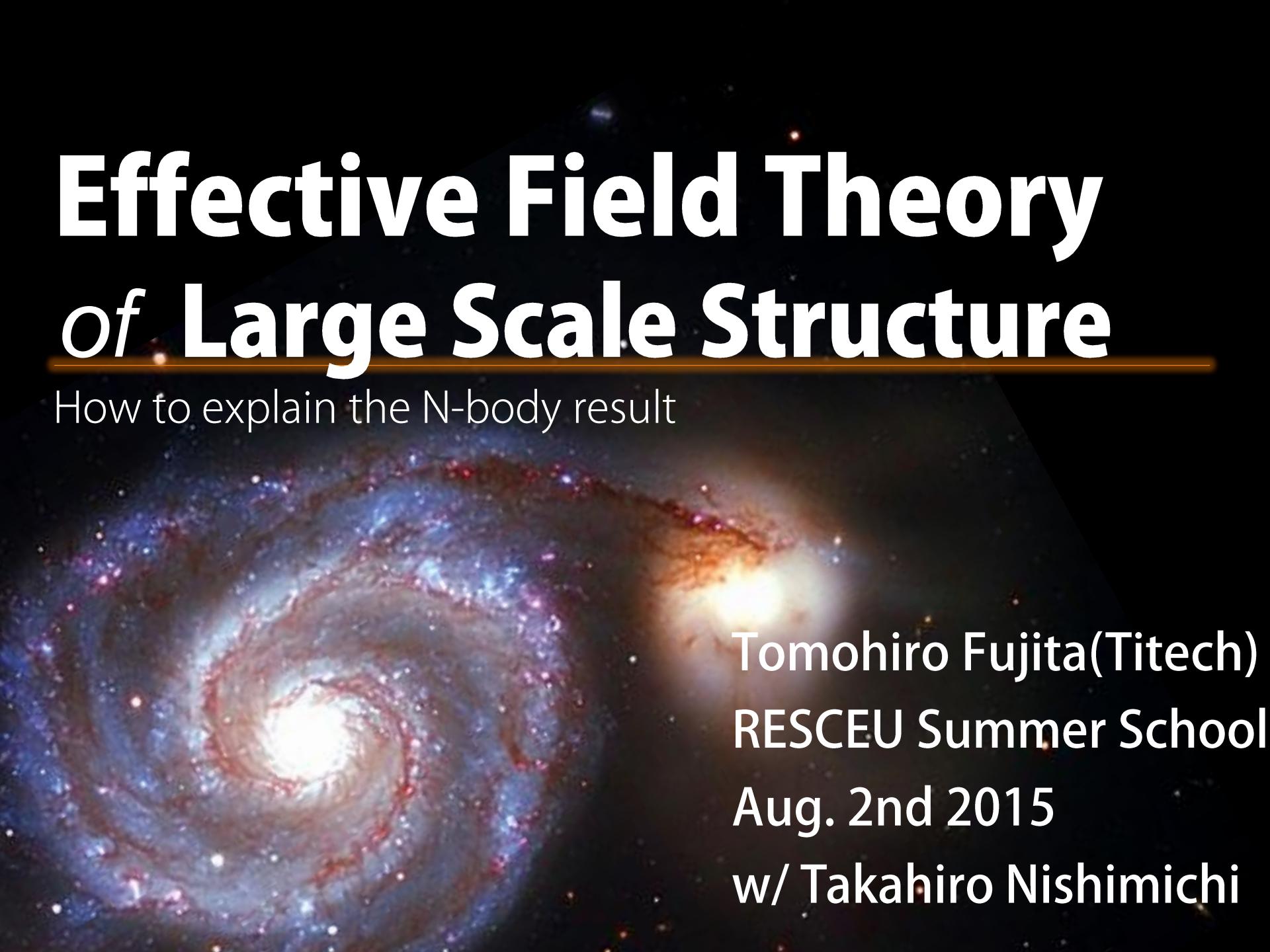


# Effective Field Theory of Large Scale Structure

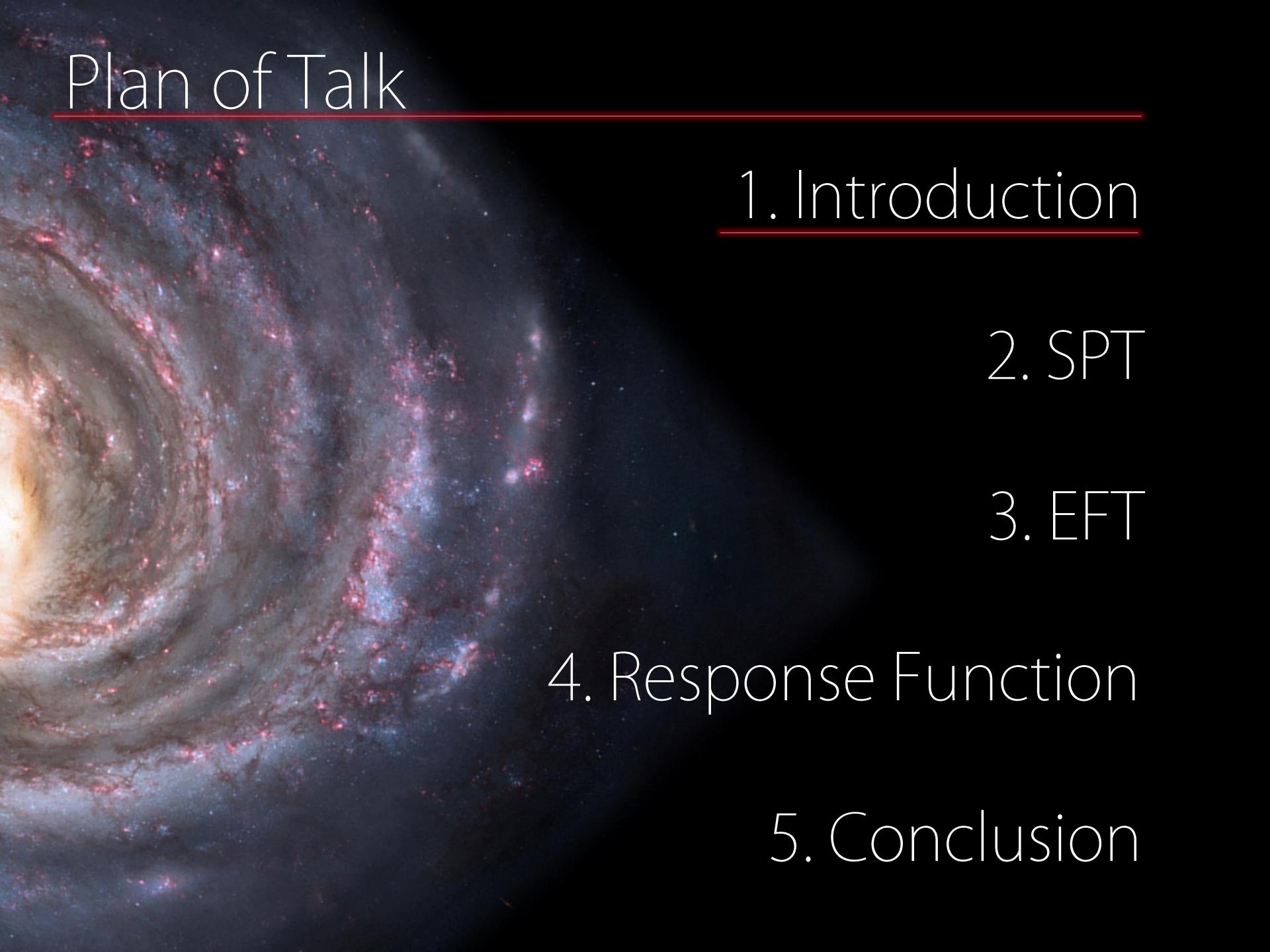
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How to explain the N-body result



Tomohiro Fujita(Titech)  
RESCEU Summer School  
Aug. 2nd 2015  
w/ Takahiro Nishimichi

# Plan of Talk



1. Introduction

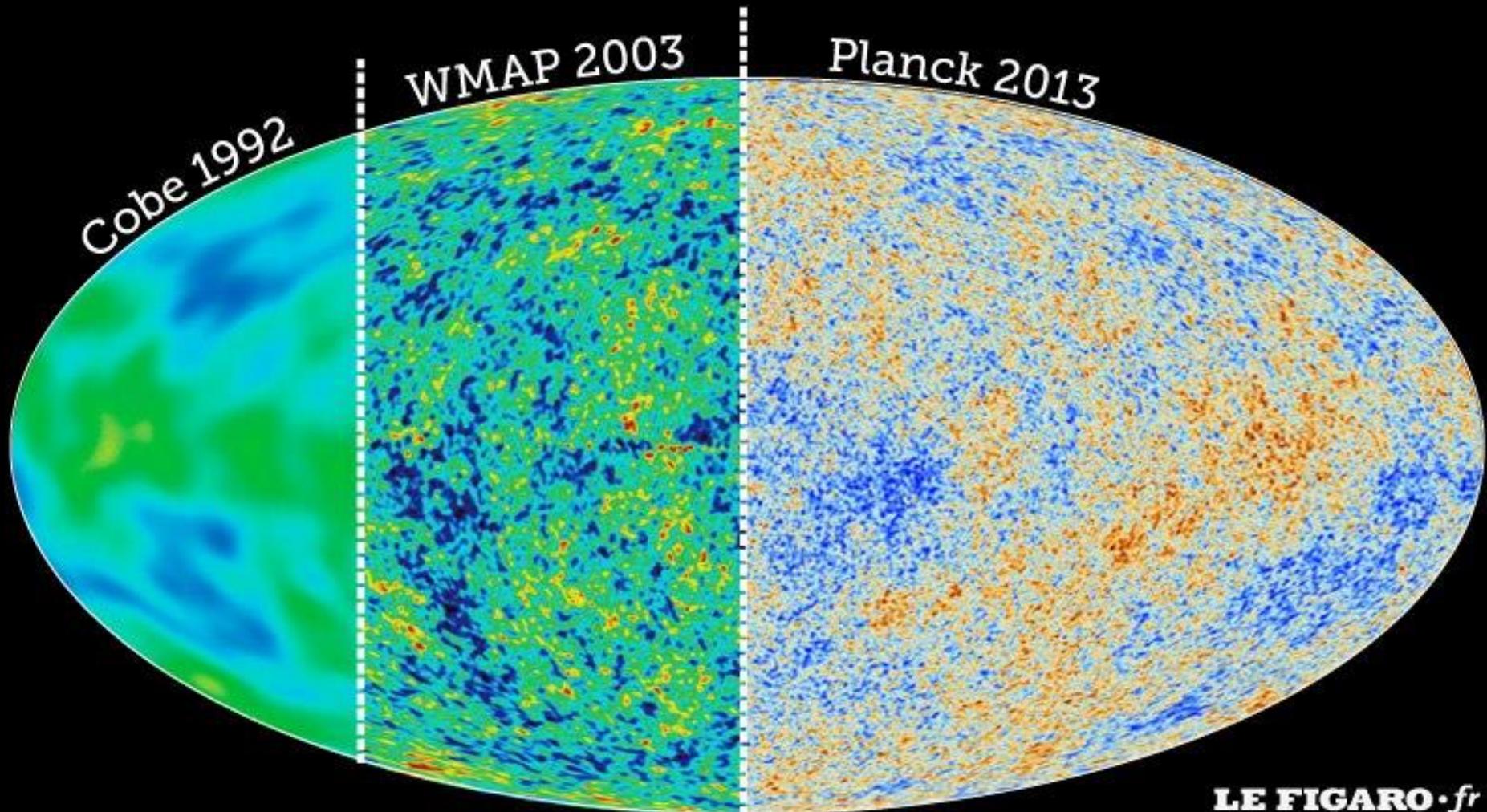
2. SPT

3. EFT

4. Response Function

5. Conclusion

# Golden age of CMB:



# Golden age of Galaxy Survey



Fight against

# Nonlinearity

---

©Dark Sky Simulations

CMB: OK with  
linear pert.

LSS:  $\delta$  grows  
on small scale



We need a theory to deal with Nonlinearity

# List of papers about EFTofLSS

## Pioneer work

- *Cosmological Non-Linearities as an Effective Fluid*  
Baumann et al. [JCAP 1207 (2012) 051]
- *The Effective Field Theory of Cosmological Large Scale Structures*  
Carrasco et al. [JHEP 1209 (2012) 082]

## Development

- *The 2-loop matter power spectrum and the IR-safe integrand*  
Carrasco et al. [JCAP 1407 (2014) 056 ]
- *The Effective Field Theory of Large Scale Structures at Two Loops*  
Carrasco et al. [JCAP 1407 (2014) 057 ]
- *On the Renormalization of the Effective Field Theory of Large Scale Structures*  
Pajer et al. [JCAP 1308 (2013) 037 ]
- *Effective field theory of dark matter and structure formation: Semianalytical results*  
Hertzberg [Phys.Rev. D89 (2014) 4, 043521 ]
- *The Lagrangian-space Effective Field Theory of Large Scale Structures*  
Porto et al. [JCAP 1405 (2014) 022 ]
- *The One-Loop Matter Bispectrum in the Effective Field Theory of Large Scale Structures*  
Angulo et al. [arXiv:1406.4143 ]
- *The IR-resummed Effective Field Theory of Large Scale Structures*  
Senatore & Zaldarriaga [JCAP 1502 (2015) 02, 013]
- *The EFT of Large Scale Structures at All Redshifts: Analytical Predictions for Lensing*  
Foreman et al. [arXiv:1503.01775]
- *On the reach of perturbative methods for dark matter density fields*  
Baldauf et al. [arXiv:1507.02255]
- *The Effective Field Theory of Large Scale Structure at Two Loops: the apparent scale dependence of the speed of sound*  
Baldauf et al. [arXiv:1507.02256 ]
- *Precision Comparison of the Power Spectrum in the EFTofLSS with Simulations*  
Foreman et al. [arXiv:1507.05326]

## Application

- *Bias in the Effective Field Theory of Large Scale Structures*  
L. Senatore [arXiv:1406.7843]
- *Redshift Space Distortions in the Effective Field Theory of Large Scale Structures*  
Senatore et al. [arXiv:1409.1225 ]
- *Analytic Prediction of Baryonic Effects from the EFT of Large Scale Structure*  
Lewandowski et al. [JCAP 1505 (2015) 05, 019 ]
- *On the Statistics of Biased Tracers in the Effective Field Theory of Large Scale Structures*  
Angulo et al. [arXiv:1503.08826]

# Plan of Talk

1. Introduction

2. SPT

3. EFT

4. Response Function

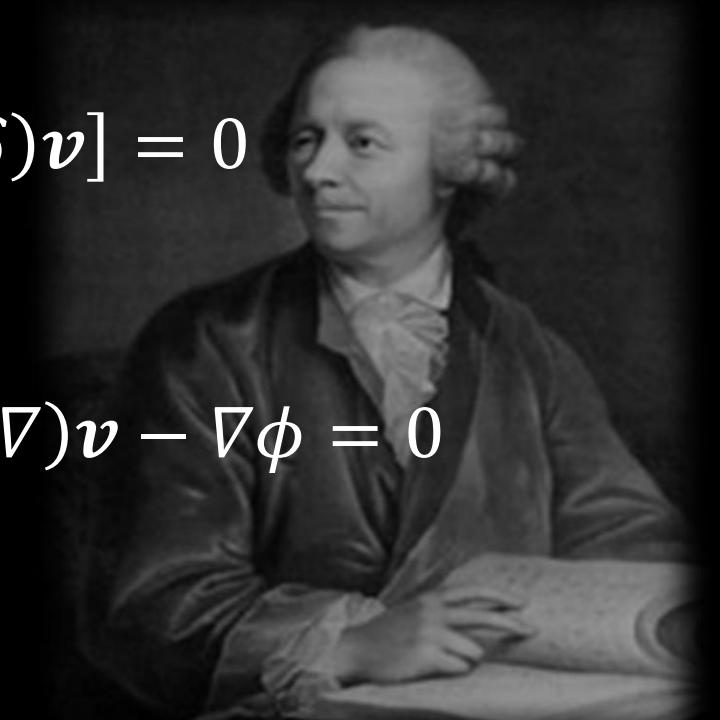
5. Conclusion

SPT = standard perturbation theory

assumes DM dynamics is approximated by pressureless fluid & solves fluid eqs. perturbatively.

Continuity eq.       $\delta' + \nabla \cdot [(1 + \delta)\mathbf{v}] = 0$

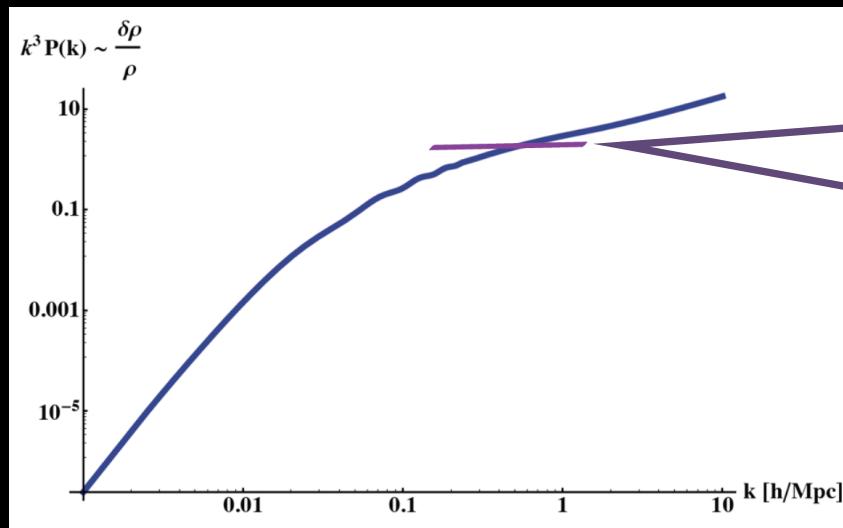
Euler eq.       $\mathbf{v}' + \mathcal{H}\mathbf{v} + (\mathbf{v} \cdot \nabla)\mathbf{v} - \nabla\phi = 0$



We can solve the EoMs perturbatively

$$\delta = \delta_1 + \delta_2 + \delta_3 \cdots$$

SPT relies on perturbation of  $\delta \ll 1$



$\delta > 1$   
on smaller scales

SPT fails on smaller scales,  $k \gtrsim 0.1 h\text{Mpc}^{-1}$

# Plan of Talk

1. Introduction

2. SPT

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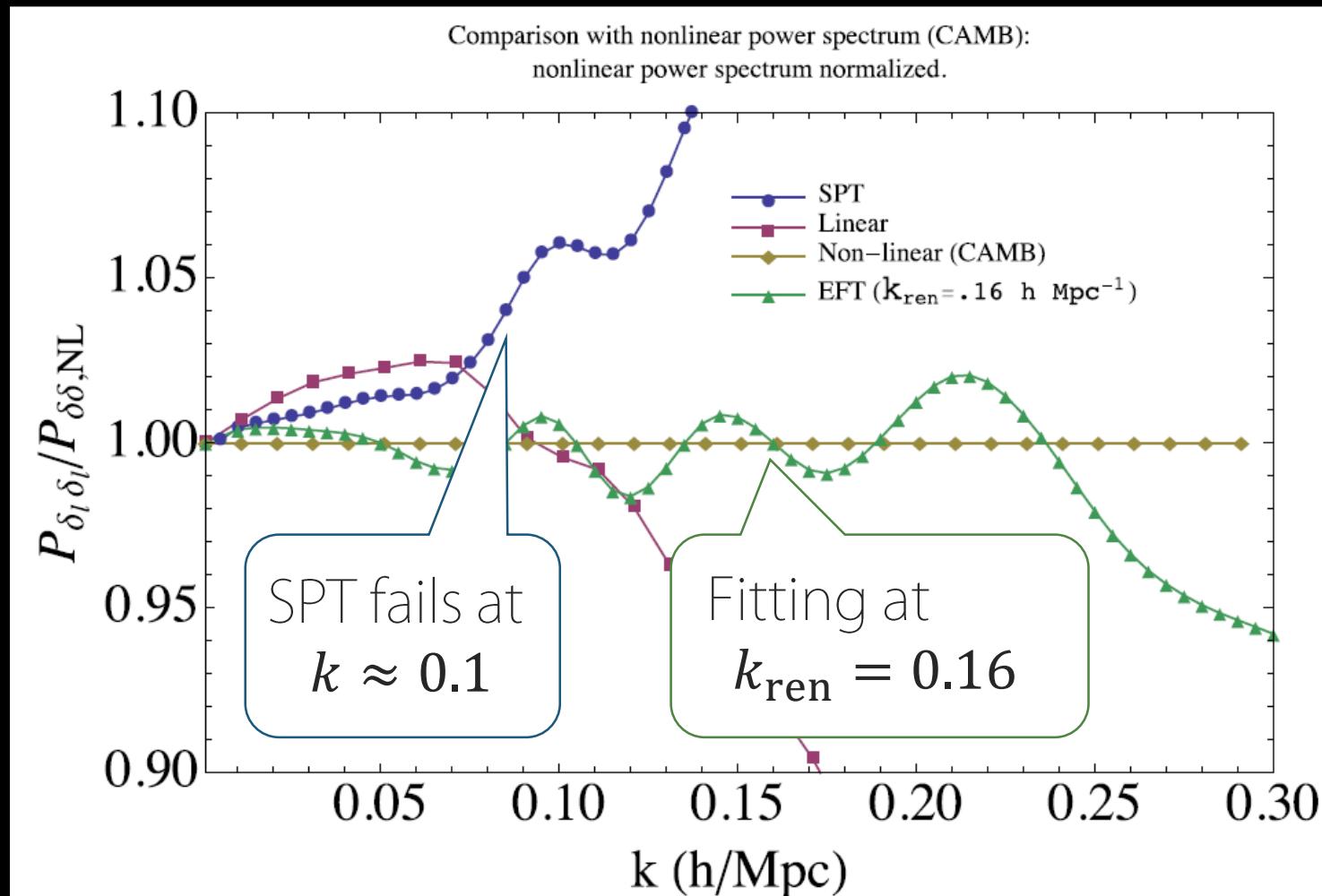
EFT = effective field theory  
 $\approx$  SPT + fitting parameter

Parameter is fixed s.t.  $P_\delta(k_{\text{ren}})$  in EFT of LSS  
agrees with observed or simulated  $P_\delta(k_{\text{ren}})$ .



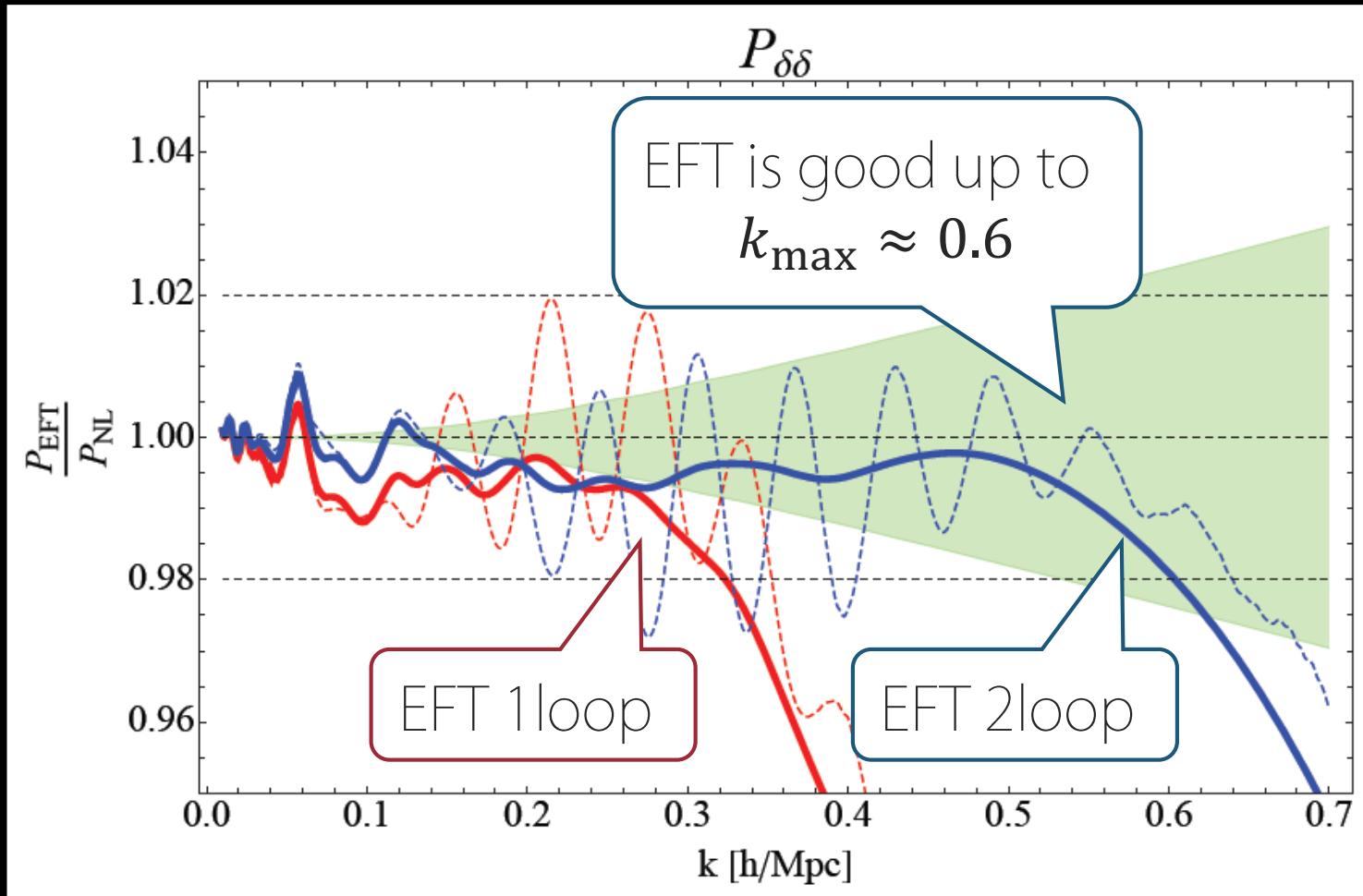
EFT prediction is consistent with  $P_{\text{N-body}}$   
up to much smaller scale than SPT.

# 1loop result of EFT



- *The Effective Field Theory of Cosmological Large Scale Structures*  
Carrasco et al. [JHEP 1209 (2012) 082]

# 2loop result of EFT+IR resummation

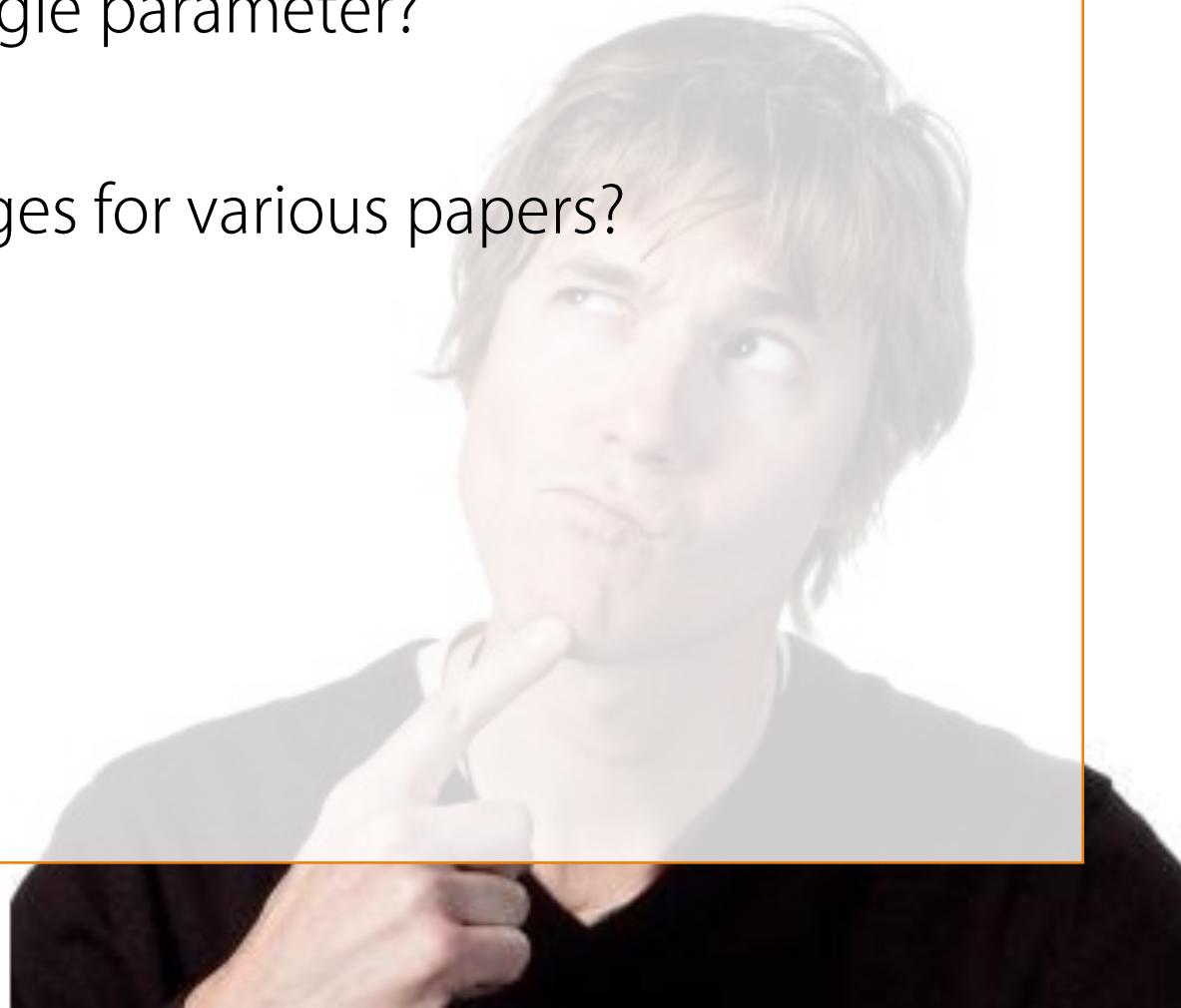


*The IR-resummed Effective Field Theory of Large Scale Structures*  
Senatore & Zaldarriaga [JCAP 1502 (2015) 02, 013]

# Questions

---

- Is non-linear dynamics of DM really described by adding a single parameter?
- Why  $k_{\max}$  changes for various papers?



# Change of $k_{\max}$

$$P_\delta(z = 0)$$

Carrasco et al. [JHEP 1209 (2012) 082]

$$k_{\max}^{1\text{loop}} = 0.24 h \text{Mpc}^{-1}$$

Carrasco et al. [JCAP 1407 (2014) 057 ]

$$k_{\max} = 0.6 h \text{Mpc}^{-1}$$

Senatore&Zaldarriaga [JCAP1502(2015)02,013]

$$k_{\max} \sim 0.6 h \text{Mpc}^{-1}$$

Foreman&Senatore [arXiv: 1503.01775 ]

$$k_{\max} = 0.6 h \text{Mpc}^{-1}$$

Baldauf et al. [arXiv: 1507.02256 ]

$$k_{\max} \approx 0.3 h \text{Mpc}^{-1}$$

Foreman et al. [arXiv:1507.05326 ]

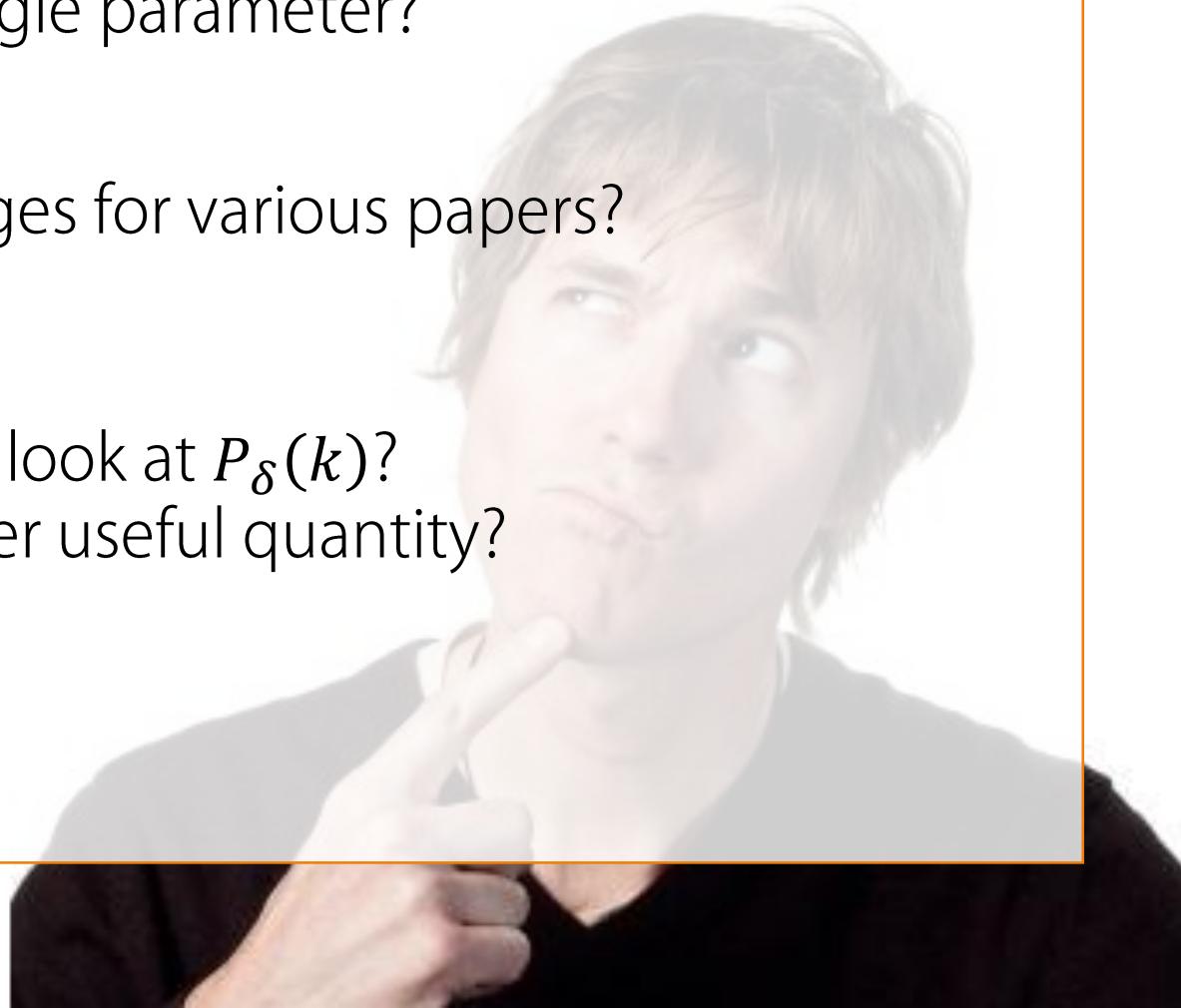
$$k_{\max} = 0.34 h \text{Mpc}^{-1}$$

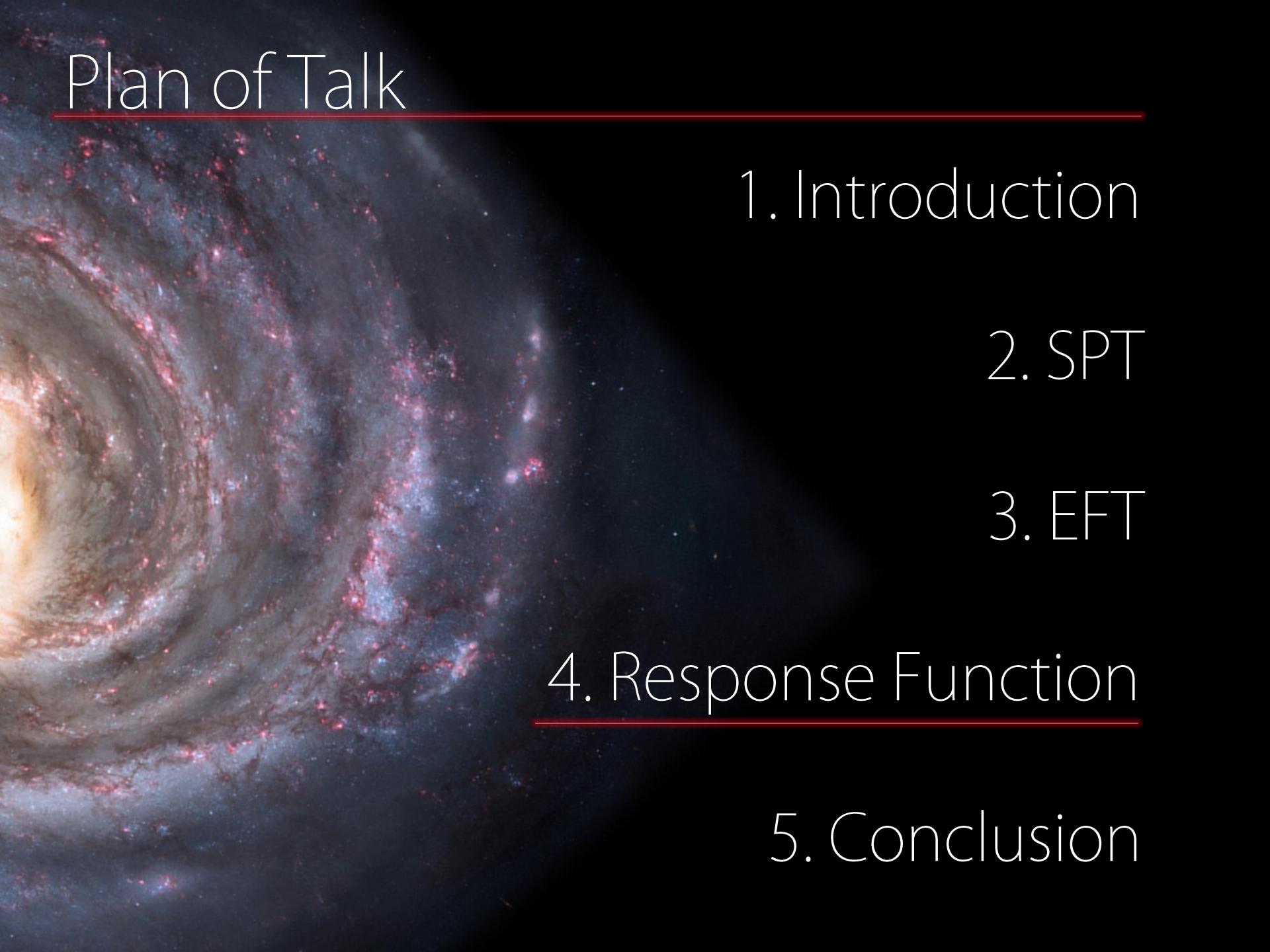
We found EFT describes the correct nonlinear dynamics up to  $k \approx 0.3$

# Questions

---

- Is non-linear dynamics of DM really described by adding a single parameter?
- Why  $k_{\max}$  changes for various papers?
- Is it sufficient to look at  $P_\delta(k)$ ?  
Is there any other useful quantity?





# Plan of Talk

1. Introduction

2. SPT

3. EFT

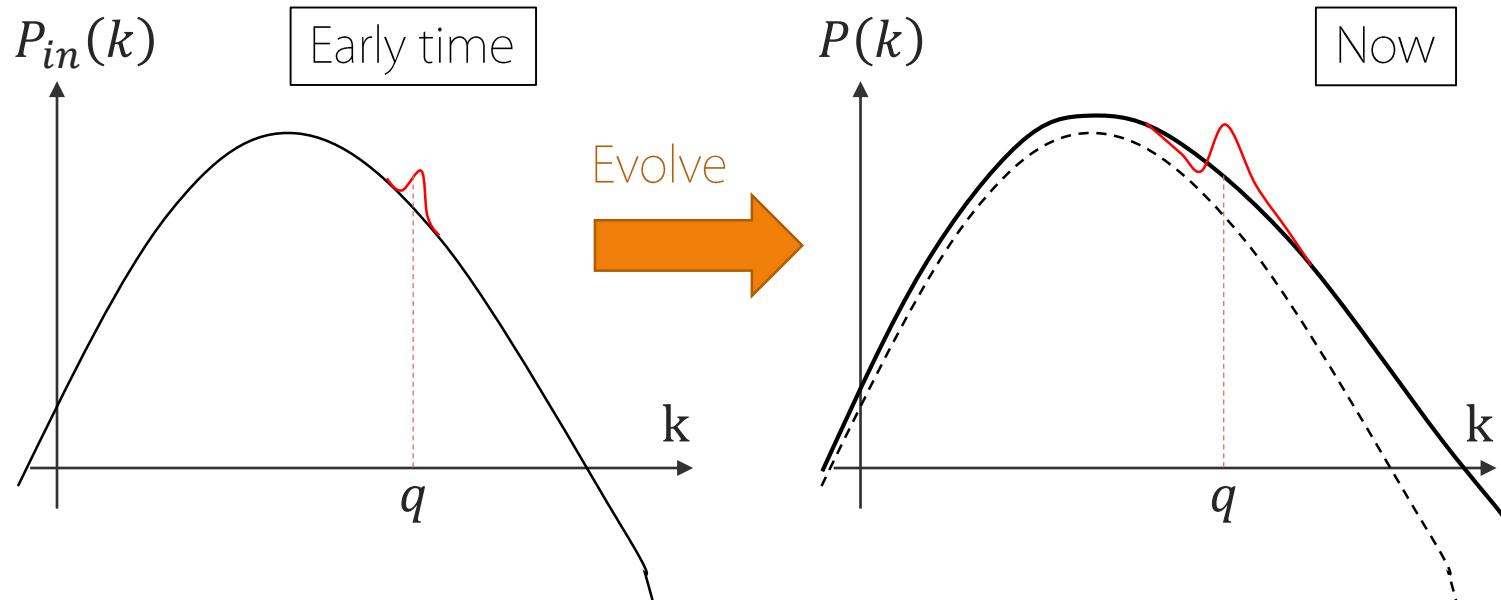
4. Response Function

5. Conclusion

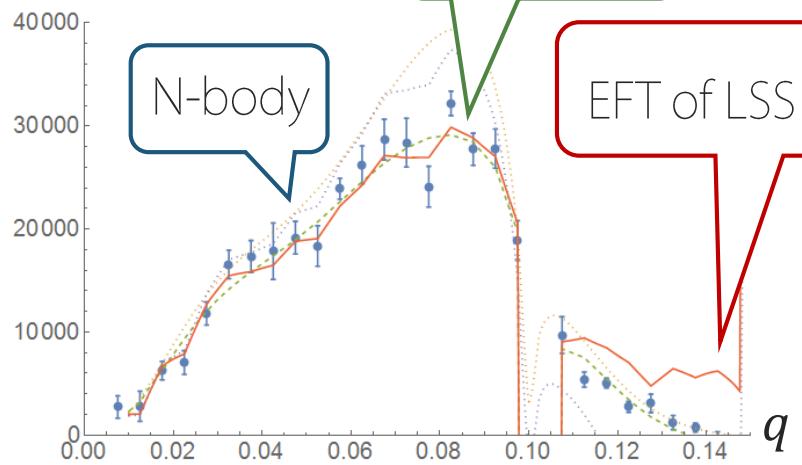
# Response Function

$$\mathcal{R}(k, q) \equiv \frac{\delta P(k)}{\delta P_{11}(q)}$$

$\mathcal{R}$  indicates how resultant  $P(k)$  changes, if one perturbs the initial condition  $P_{11}(q)$ .



$\mathcal{R}(k = 0.1, q)$

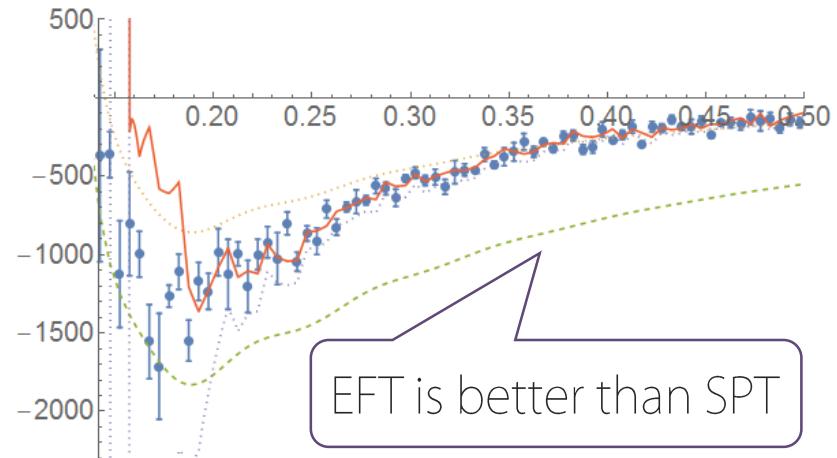


SPT 2loop

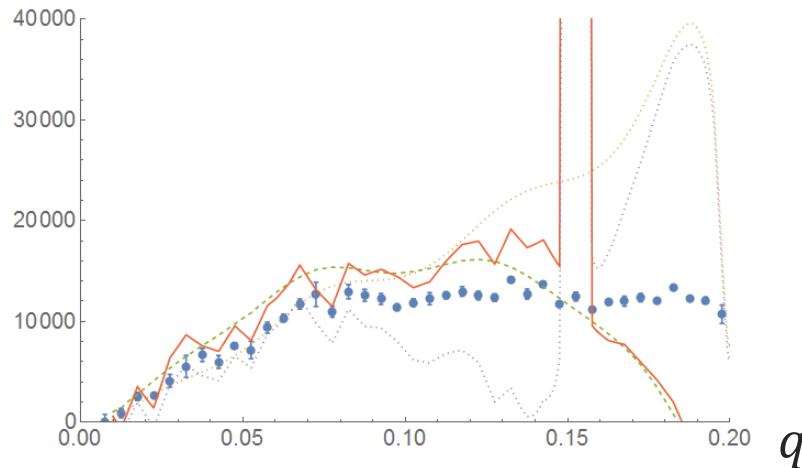
EFT of LSS

N-body

$\mathcal{R}(k = 0.1, q)$

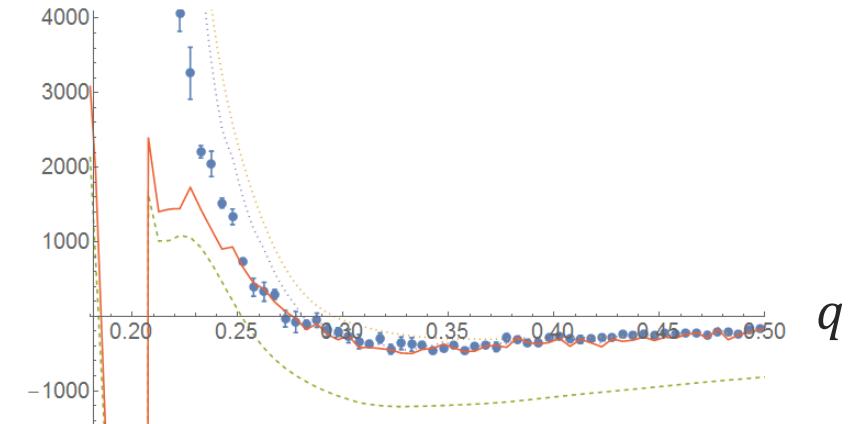


$\mathcal{R}(k = 0.2, q)$

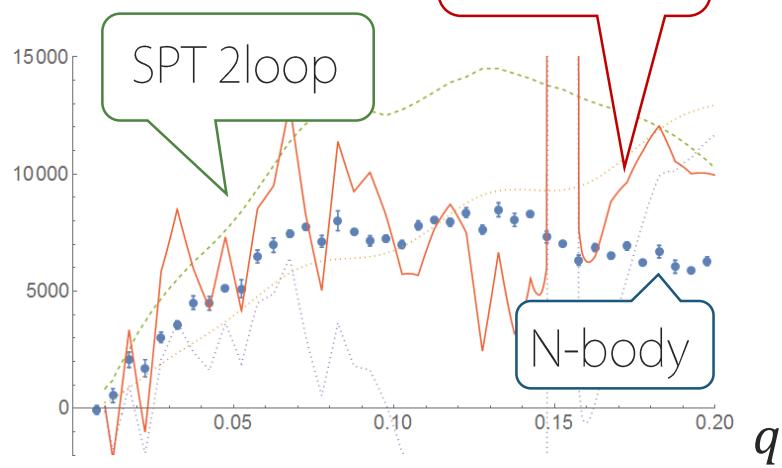


$\mathcal{R}(k = 0.2, q)$

$k_{\text{ren}} = 0.15$



$\mathcal{R}(k = 0.3, q)$

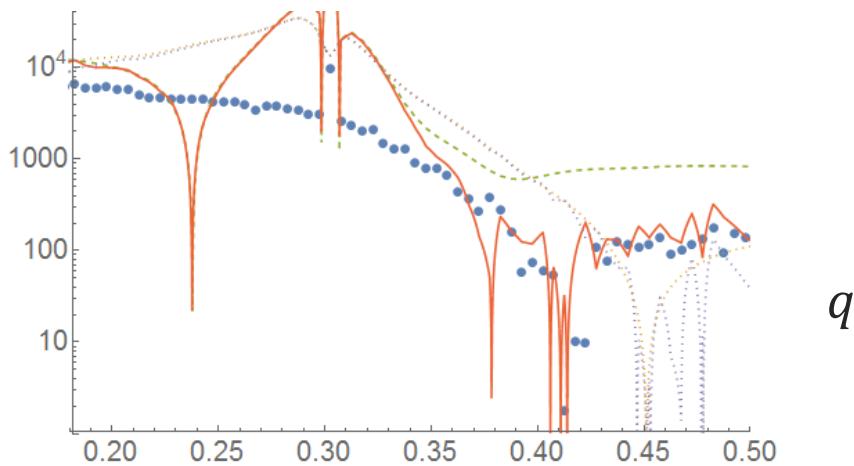


EFT of LSS

SPT 2loop

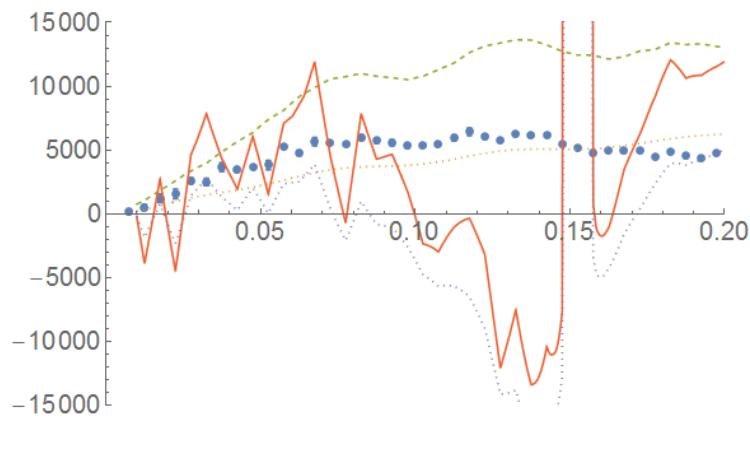
N-body

$\mathcal{R}(k = 0.3, q)$



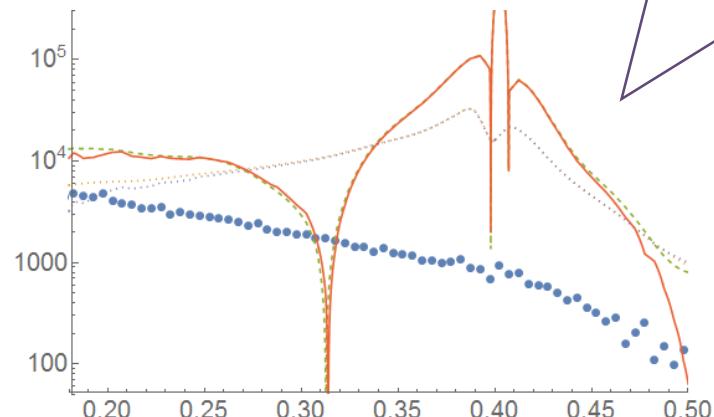
$q$

$\mathcal{R}(k = 0.4, q)$



$\mathcal{R}(k = 0.4, q)$

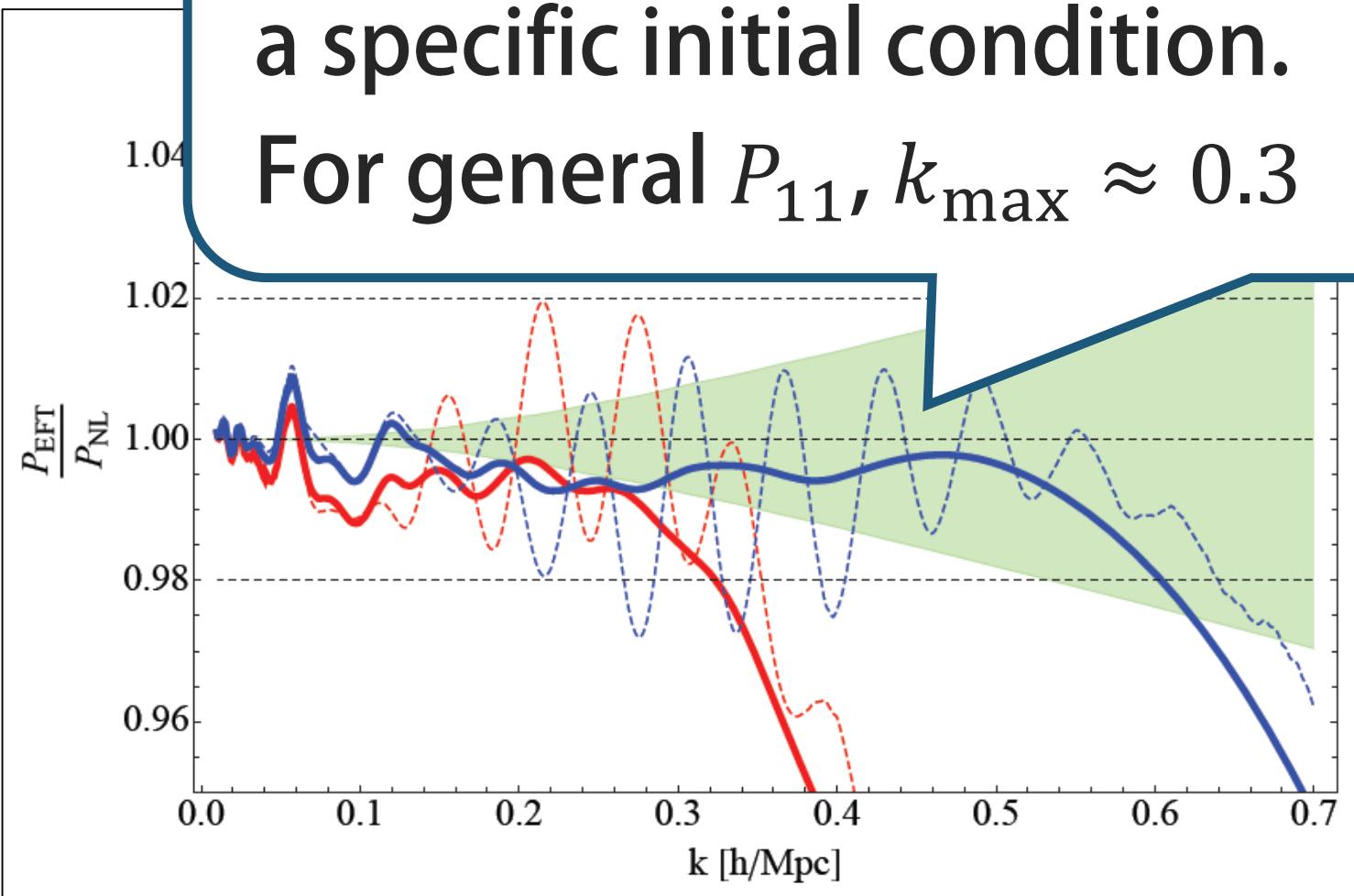
EFT fails to reproduce  $\mathcal{R}_{NL}$



$q$

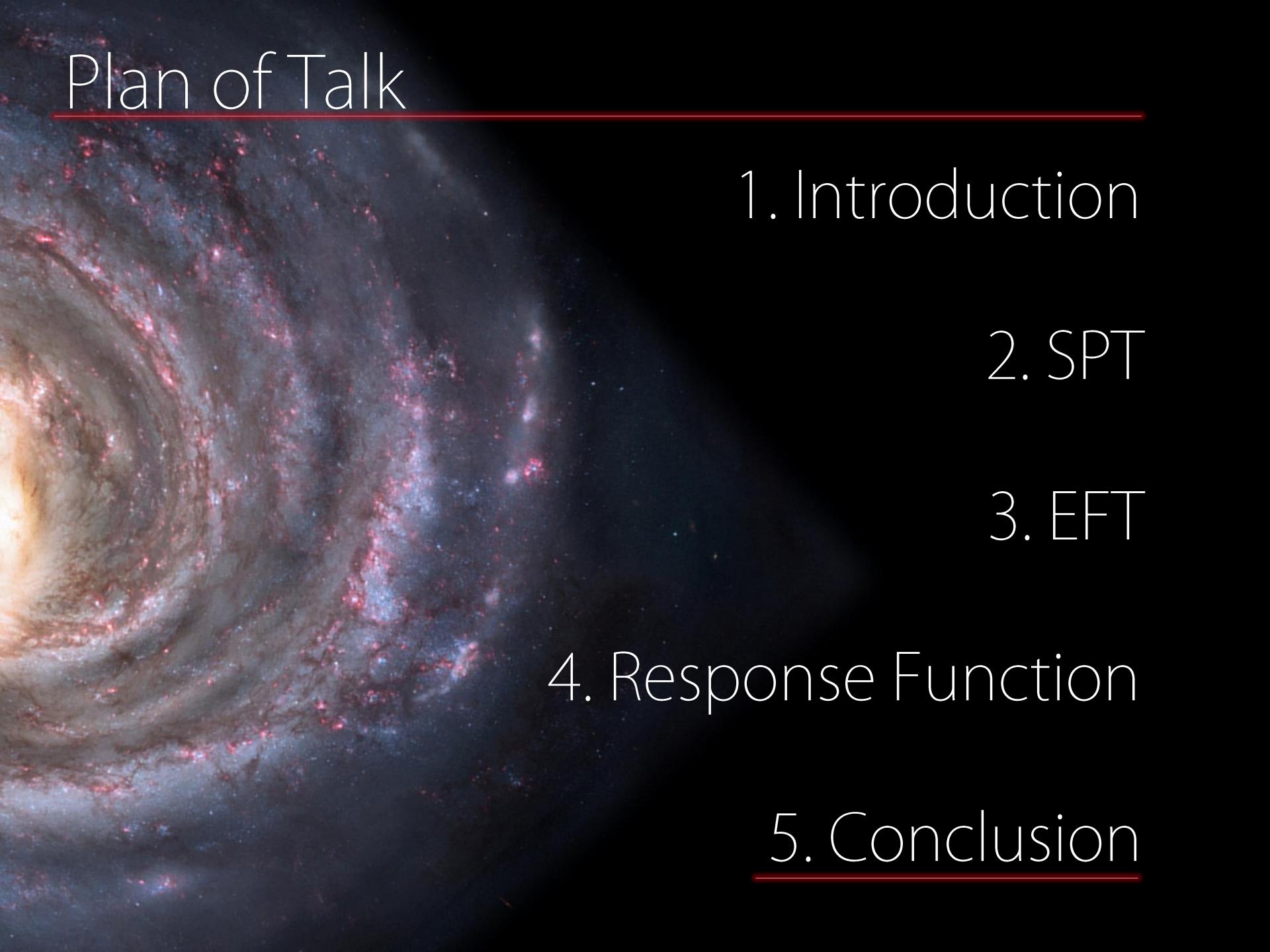
2loop n

It's an accidental success for  
a specific initial condition.  
For general  $P_{11}$ ,  $k_{\max} \approx 0.3$



*The IR-resummed Effective Field Theory of Large Scale Structures*  
Senatore & Zaldarriaga [JCAP 1502 (2015) 02, 013]

# Plan of Talk



1. Introduction

2. SPT

3. EFT

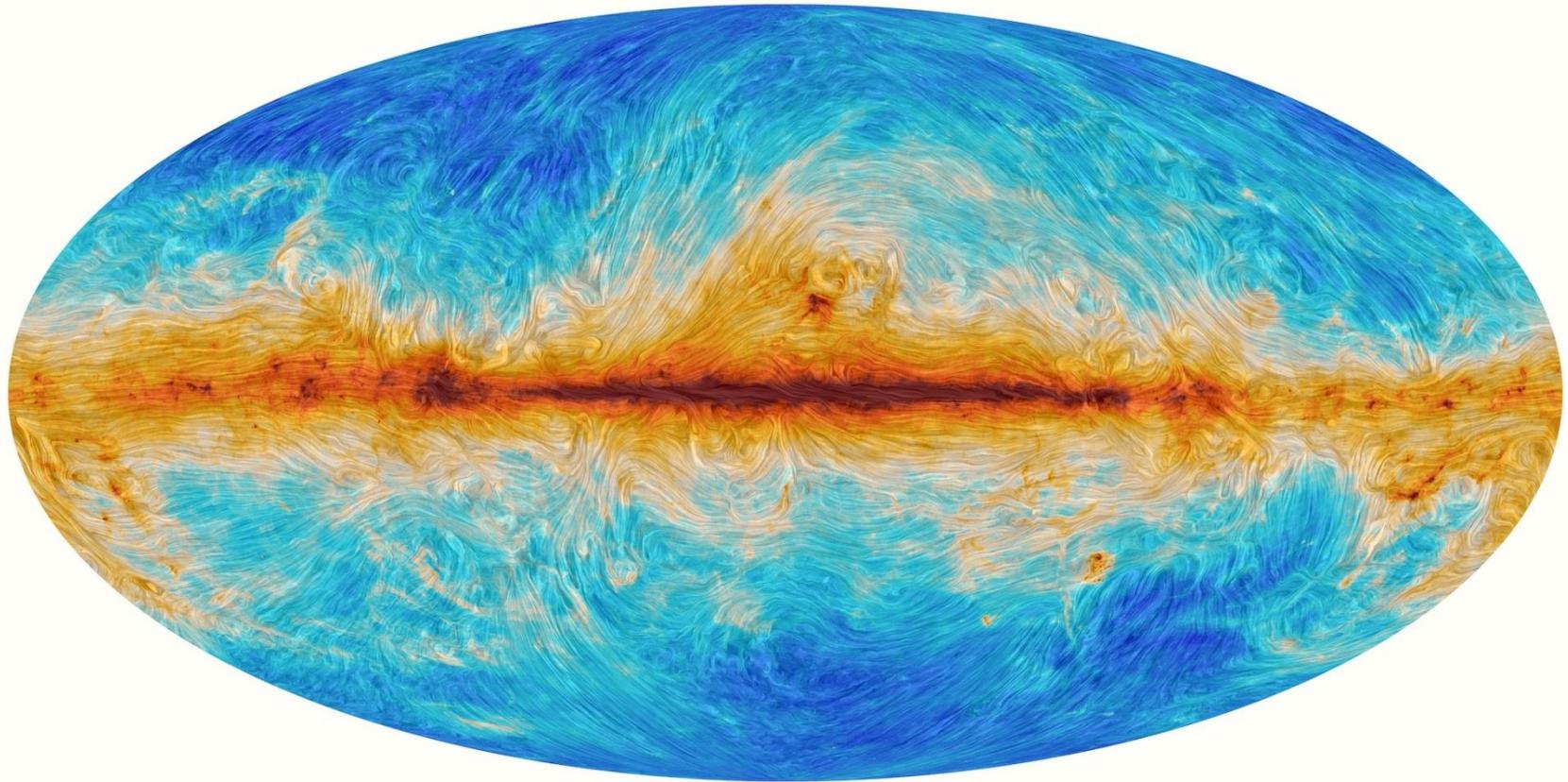
4. Response Function

5. Conclusion

# Conclusion

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- To exploit upcoming galaxy surveys, we need to develop a theory to deal with non-linearity.  
EFT of LSS is a promising theoretical foundation.
- Even if a theory reproduces  $P_\delta(k)$  for an initial condition, it does not guarantees the correct dynamics.  
The response function  $\mathcal{R}$  is a powerful discriminator.
- $\mathcal{R}(k, q)$  in EFT of LSS shows that 2loop EFT is consistent with N-body simulation up to  $k \approx 0.3 h\text{Mpc}^{-1}$ .



Thank you!