An upper limit on continuous GW in low-frequency regime using a torsion-bar antenna



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Motivation

- Recently, we have developed the torsion-bar antenna (TOBA) based on PRD 90, 064039.
- We operated the TOBA for 24 hours from Dec.10 to Dec.11 in 2014.
- \Box The sensitivity reached 10⁻¹⁰ Hz^{-1/2} at around 1 Hz.



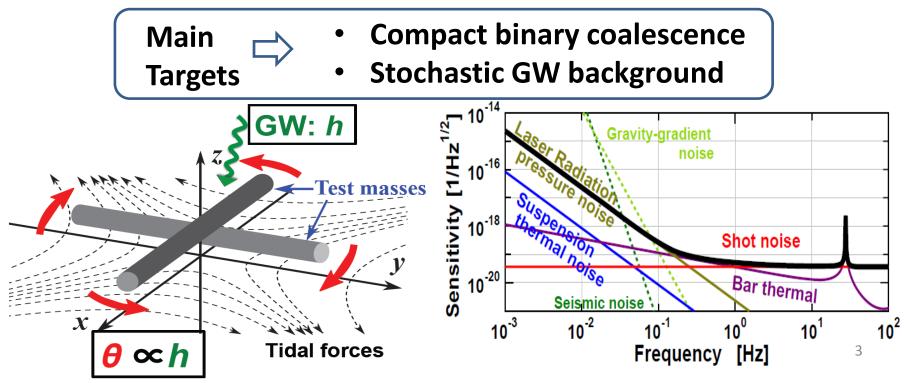
Continuous GWs in low-frequency regime have yet to be investigated so far.

We search for continuous GWs from an isolated neutron star.We put a constraint on the GW amplitude.

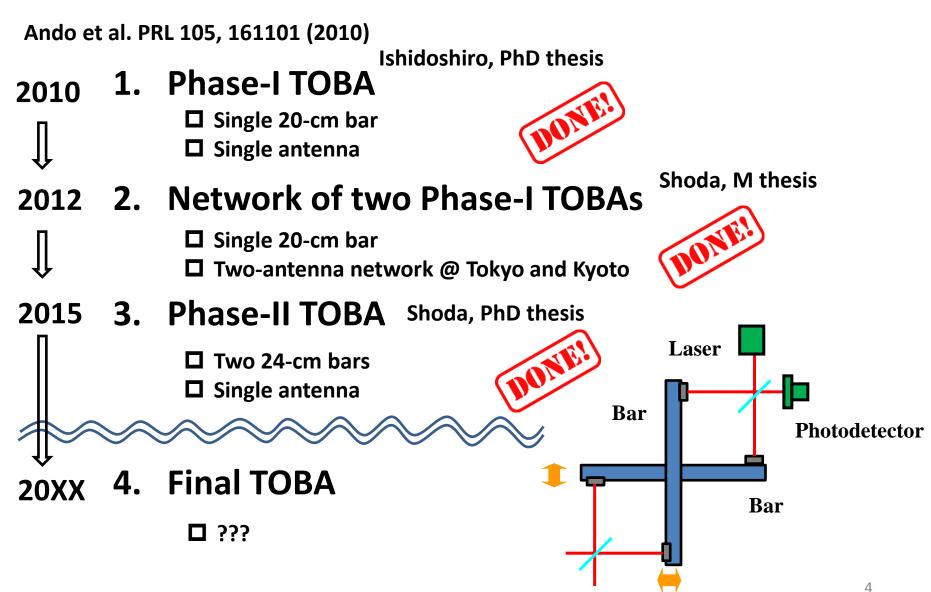
What is a TOBA ?

TOrsion-bar Antenna (TOBA) (Ando et al. PRL 105, 161101 (2010))

- ✓ Low-frequency GW antenna which measures rotations of bars
- ✓ formed by two bar-shaped orthogonal test masses
- ✓ sensitive to low-frequency GWs (f=0.1-1 Hz) even on the ground thanks to its resonant frequency f_{res} < 1mHz.</p>



History

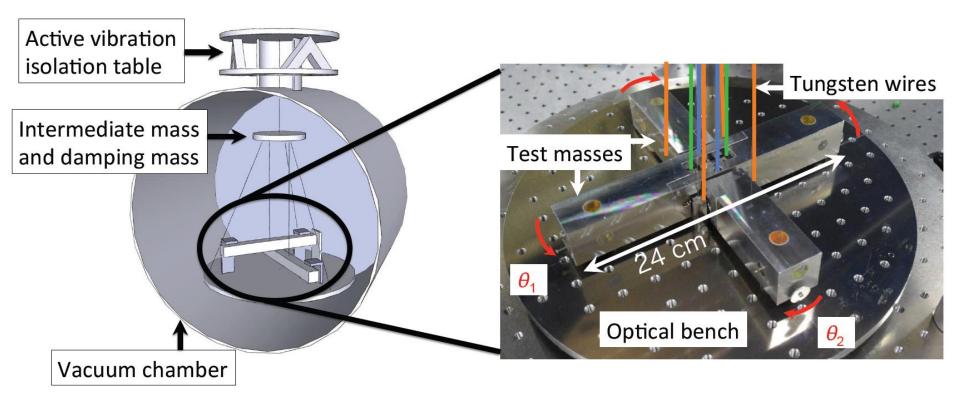


Design Overview

D Basic design for the Phase-II TOBA

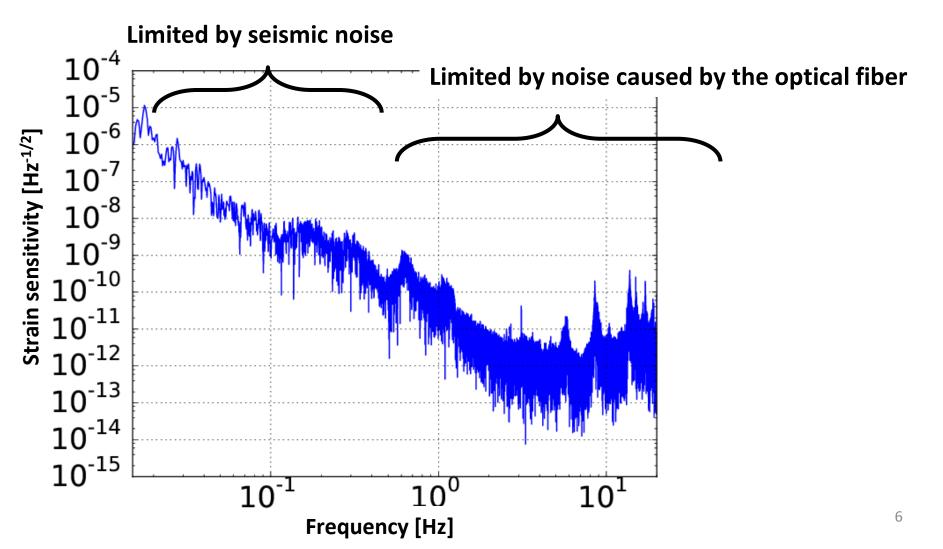
- ✓ Two 24-cm bars
- ✓ Mass of the bar : 0.61kg

✓ Location : University of Tokyo (35°42'49.0" N, 139°45'47.0" E)



Measured strain sensitivity

Sensitivity curve of the Phase-II TOBA



Known isolated NS search

GW from a known rapidly rotating neutron star

✓ GW signal in a detector

$$h(t) = \mathbf{h}_0 F_+(t, \psi) \frac{1 + \cos^2 \iota}{2} \cos \Phi(t) + \mathbf{h}_0 F_\times(t, \psi) \cos \iota \sin \Phi(t)$$

$$\Phi(t) = \phi_0 + 2\pi f_0 t \left(1 + \frac{\mathbf{v}(t) \cdot \mathbf{n}}{c}\right) \qquad \text{4 unknown parameters } \{\mathbf{h}_0, \psi, \iota, \phi_0\}$$

Amplitude

- $\checkmark \varepsilon$: Ellipticity (<10⁻⁶) Horowitz & Kadau (2009)
- $\checkmark f_0$: Spin frequency

$$h_0 = \frac{4\pi^2 G}{c^4 r} \varepsilon I f_0^2$$

= $1.0 \times 10^{-30} \left(\frac{\varepsilon}{10^{-6}}\right) \left(\frac{I}{10^{38} \text{ kgm}^2}\right) \left(\frac{1 \text{ kpc}}{r}\right) \left(\frac{f_0}{1 \text{ Hz}}\right)^2$

Neutron star

Line of sight

Symmetric axis

Spin

Detection statistic

□*F*-statistic

- \checkmark *F*-statistic is based on the method of maximum likelihood.
- ✓ If $2F > 2F_{threshold}$, we regard that the signal is detected.
- ✓ We use *F*-statistic to discriminate whether or not GW signals exist in the antenna.

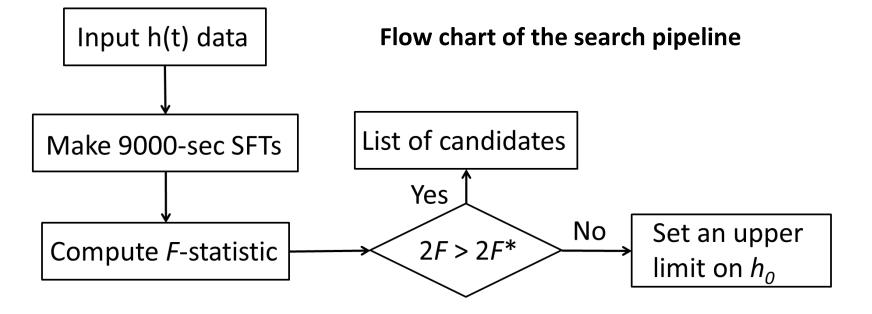
$$\ln \Lambda \left(\boldsymbol{s}; \boldsymbol{h} \right) = \ln \frac{P\left(\boldsymbol{s} | \boldsymbol{h} \right)}{P\left(\boldsymbol{s} | \boldsymbol{h} = \boldsymbol{0} \right)} = \left(\boldsymbol{s} | \boldsymbol{h} \right) - \frac{1}{2} \left(\boldsymbol{h} | \boldsymbol{h} \right)$$
$$2\mathcal{F} \equiv \max_{h_0, \phi_0, \iota, \psi} \left[2 \ln \Lambda \left(\boldsymbol{s}; \lambda \right) \right]$$
$$E\left[2\mathcal{F} \right] = 4 + \left(S/N \right)^2$$

Setting an upper limit

\Box How to set an upper limit on h_0

- ✓ If $2F < 2F_{th}$, we place an upper limit $h_0(C)$ with confidence C.
- ✓ The upper limit with confidence level C can be found by solving the below integration using Monte Carlo simulations.

$$C(h_0) = \int_{2\mathcal{F}_{obs}}^{\infty} p(2\mathcal{F}|h_0; \psi, \cos \iota) d(2\mathcal{F})$$



Search for GWs from PSR B 1944+17

Results

- ✓ Our target is a known isolated pulsar, PSR B 1944+17.
- ✓ We calculated 2*F*.
- \checkmark The measured value of 2F is not significant.
- ✓ Then, we proceeded to set an upper limit on the targeted signal using Monte Carlo simulations.

Distance r	Right ascension α	Declination δ	Spin frequency f_0	Spin down \dot{f}
0.30 kpc	19:46:53.0	+18:05:41.24	2.2695 Hz	-1.24x10 ⁻¹⁶ [Hz/s]

$$2\mathcal{F}_{obs} = 4.5$$

 $h_0^{95\%} = 8.7 \times 10^{-13}$

Summary

- The Phase-II TOBA was constructed based on PRD 90, 064039.
- **D**We operated the Phase-II TOBA during Dec.10 to Dec.11.
- **□** The sensitivity reached 10⁻¹⁰ Hz^{-1/2} at around 1 Hz.

- **D** We searched for the GW from PSR B 1944+17.
- □ We set an upper limit on h⁰ as 8.7x10⁻¹³ with 95% confidence level using the 24-hour TOBA data.