

# **Large-scale structure as a probe of dark energy**

**David Parkinson**  
University of Sussex, UK

# Question

Who was the greatest actor to portray James Bond in the 007 movies?

- a) Sean Connery
- b) George Lasenby
- c) Anthony Lasenby
- d) Roger Moore
- e) Timothy Dalton
- f) Pierce Brosnan
- g) Daniel Craig

# Dark Energy

Lots of well-asked questions:

Is it a cosmological constant?

Does  $w$  vary with time?

Does DE cluster?

Is it vacuum energy or modification of gravity?

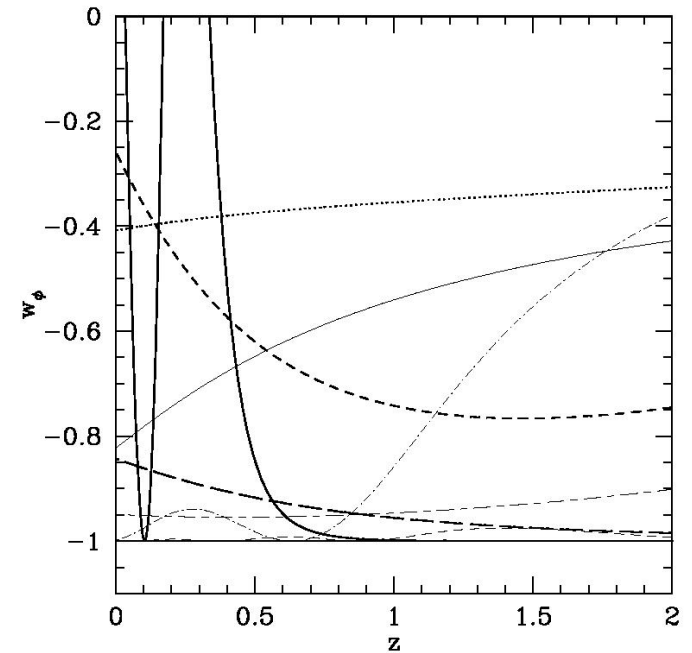
$$w = \frac{p_\Lambda}{\rho_\Lambda} = -1$$

Stress-Energy:

$$G_{\mu\nu} = 8\pi G [T_{\mu\nu}(\text{matter}) + T_{\mu\nu}(\text{new})]$$

Gravity:

$$G_{\mu\nu} + f(g_{\mu\nu}) = 8\pi G T_{\mu\nu}(\text{matter})$$



Albrecht & Weller 2002,  
astro-ph/0106079

# constraining dark energy

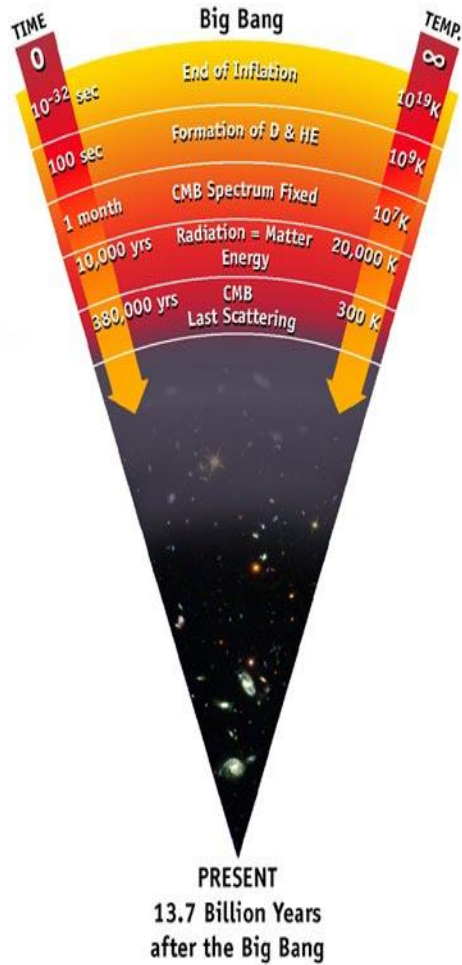
Two key ways of constraining dark energy:

1. build-up of structure (constrains DE form)
  - Mass function through cluster counts
  - Growth rate from weak lensing
  - Growth rate from merger rates/clustering amplitude
2. distance-redshift relation (constrains DE Equation of State  $w$ )
  - standard candles from SN-Ia
  - Standard rulers from Baryon Acoustic Oscillations (galaxy clustering)
  - Standard rulers from general clustering pattern (weak lensing)
3. Combined constraints
  - ISW effect (cross correlation of CMB & LSS)
  - Weak lensing constraints on structure
  - Strong lensing constraints on structure

Focus on constraining cosmology using galaxy clustering

# **Cosmic Microwave Background**

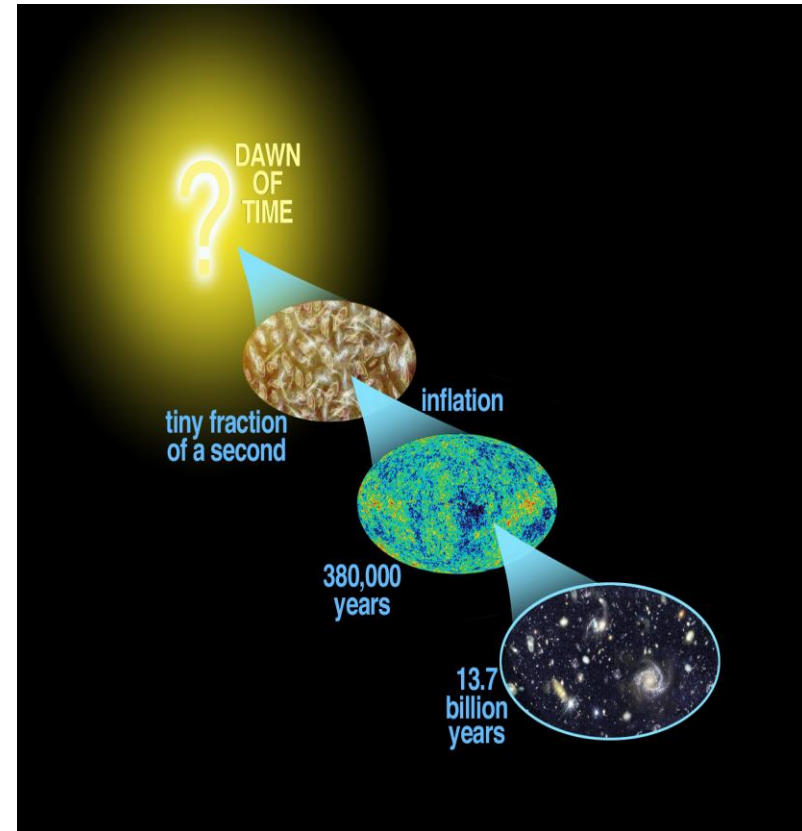
# The cosmic microwave background



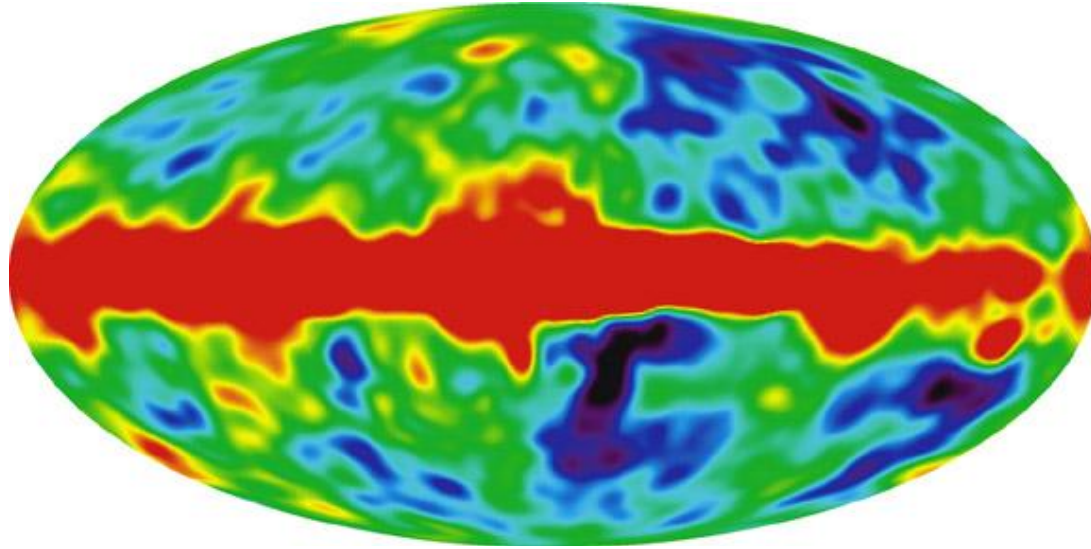
We can only see the surface of the cloud where light was last scattered



The cosmic microwave background Radiation's "surface of last scatter" is analogous to the light coming through the clouds to our eye on a cloudy day.

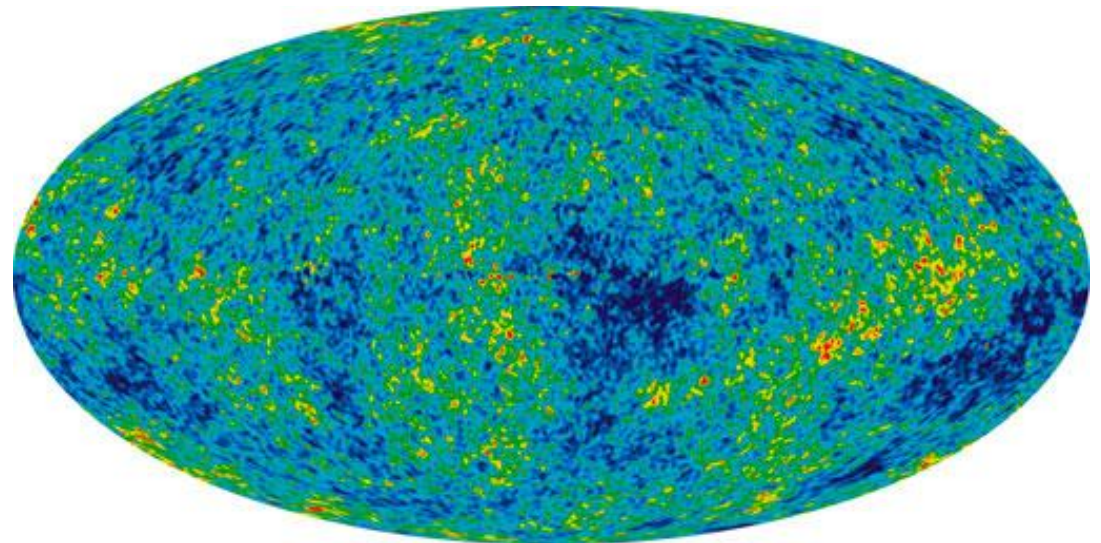


# Change in CMB observations in the last 10 years

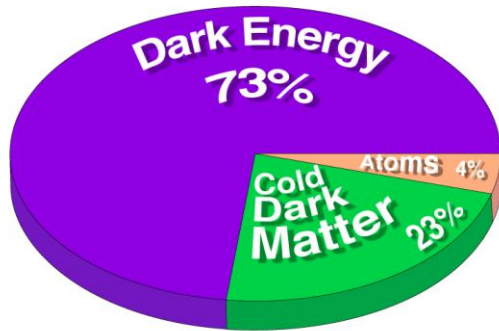
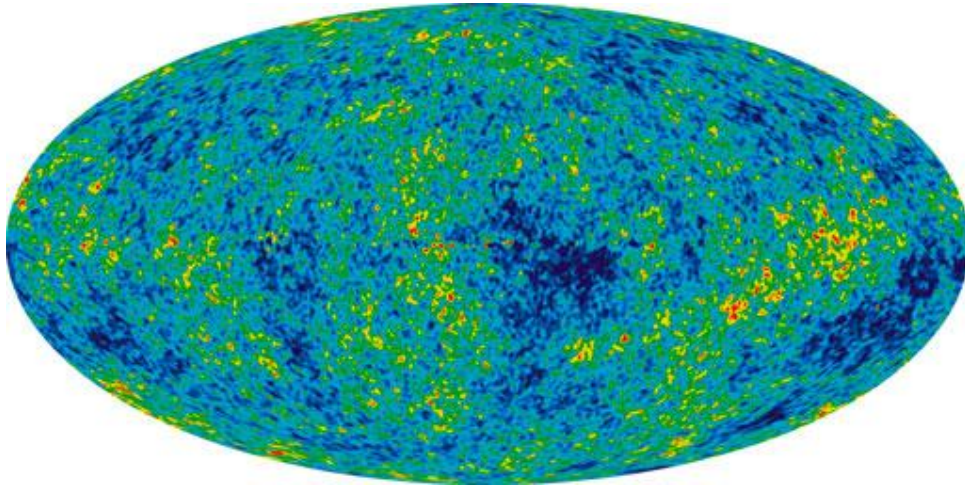


Fluctuations in the  
CMB: as measured by  
COBE satellite in  
1992

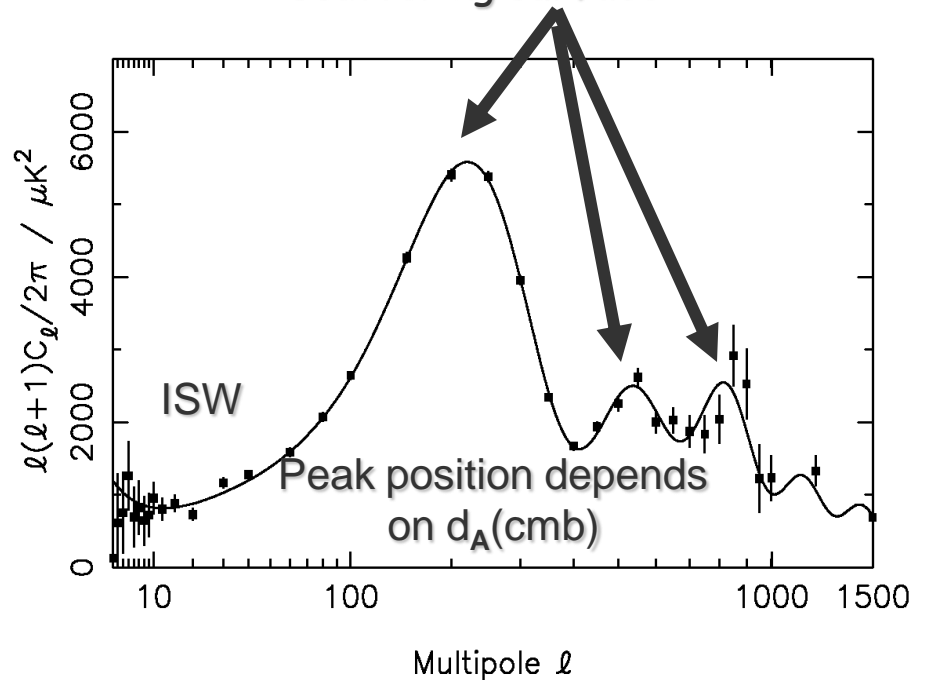
Fluctuations in the  
CMB as measured  
by WMAP satellite  
in 2001



# CMB only weakly dependent on dark energy



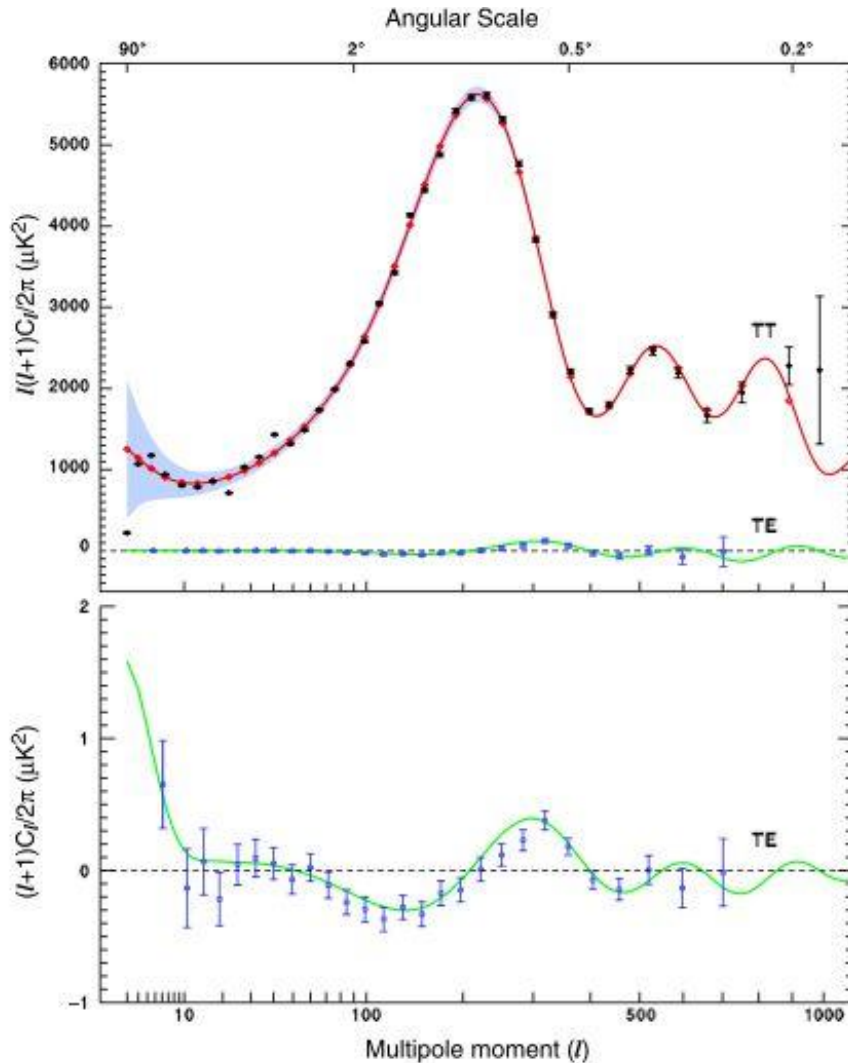
Baryon oscillations frozen into last scattering surface



CMB good measurement of  $\Omega_m$ ,  $\Omega_k$  and  $H_0$



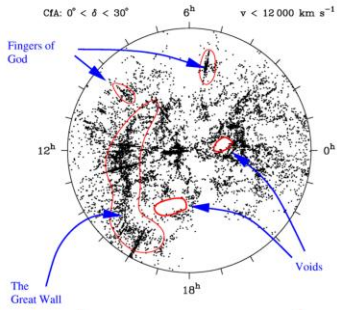
# CMB Polarisation



- Polarisation measures bulk motions on last scattering surface
- Gives important information as to nature of perturbations (must be Adiabatic, not Isocurvature or Causal seeds)
- Models of dark energy with a sudden transition in  $w$  have an enhanced ISW effect, degenerate with  $\tau$ , optical depth to reionisation (Corasaniti et al 2004)

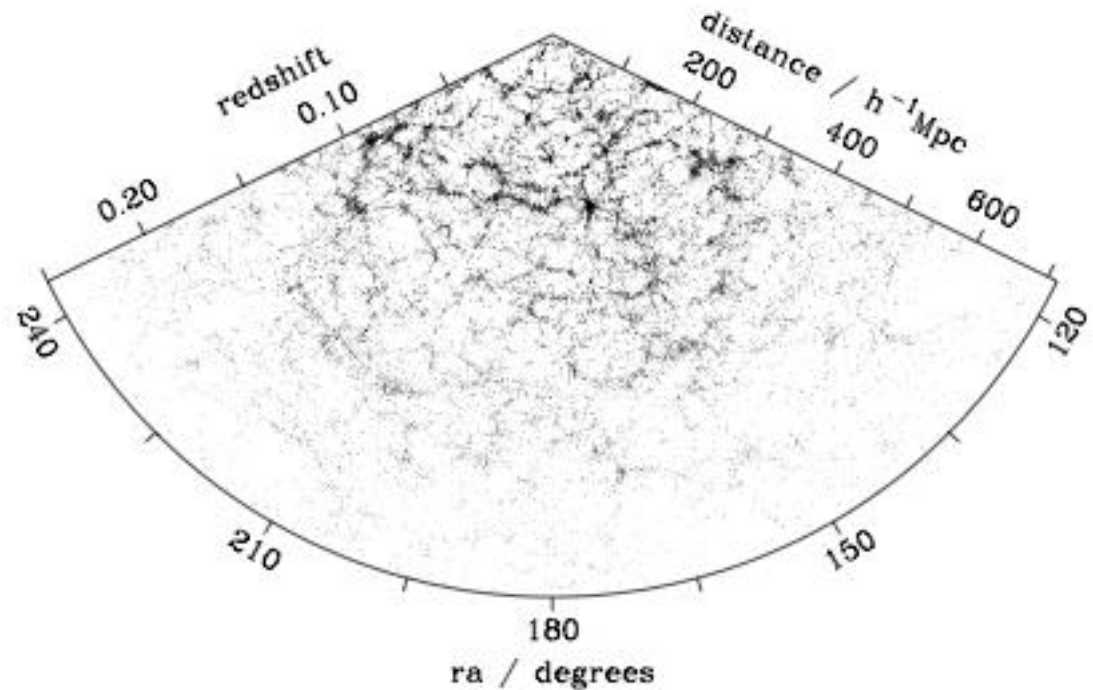
# **Galaxy redshift Surveys**

# Redshift survey progress



**mid-1980s: few  
thousand**

**Now SDSS +  
2dFGRS: soon  
1 000 000**

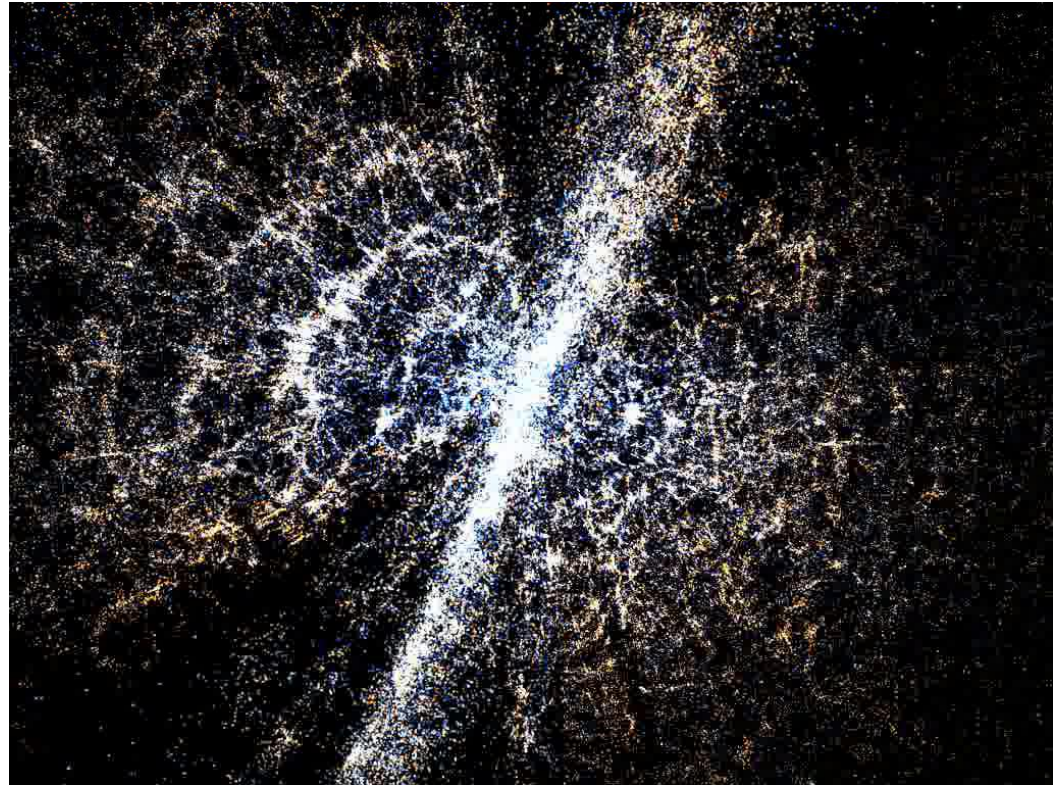


**only ~2,000,000  $z < 0.1$ : no more big local leaps**



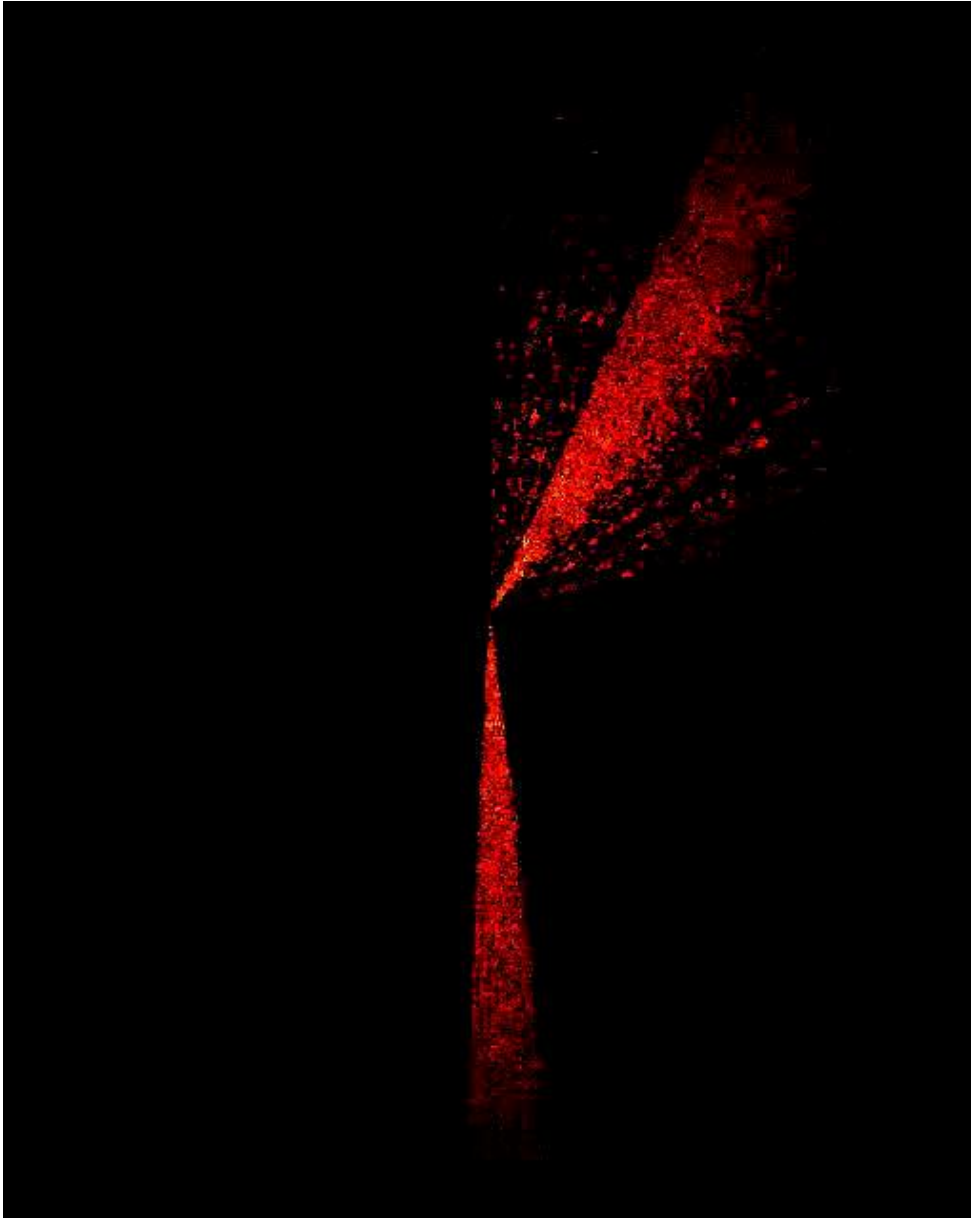
# Sloan Digital Sky Survey (SDSS)

- collaboration of 200 scientists in 14 institutions
- ongoing survey will measure redshifts for 1000000 galaxies in the local Universe (r-band selection)
- also observed ~60000 luminous red galaxies out to higher redshift
- 4<sup>th</sup> data release (DR4) just made public with ~400000 redshifts



DR6 data now public: [www.sdss.org](http://www.sdss.org)

# 2dF Galaxy Redshift Survey (2dFGRS)



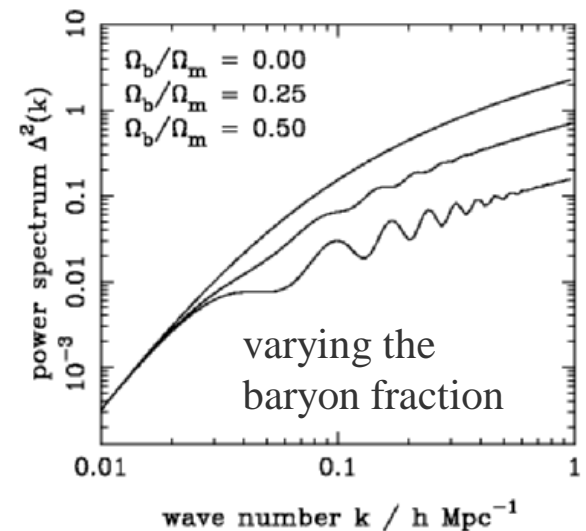
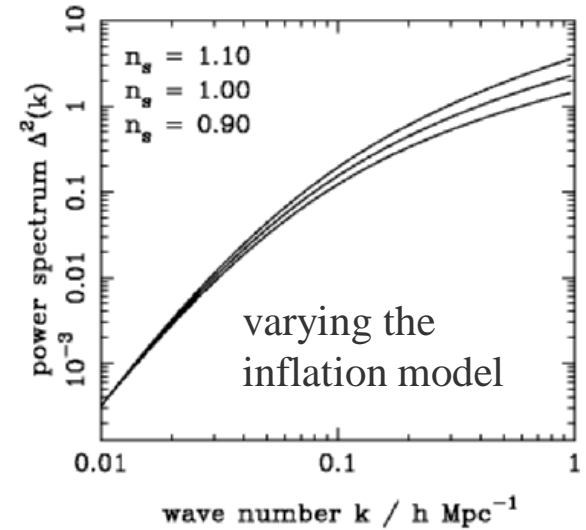
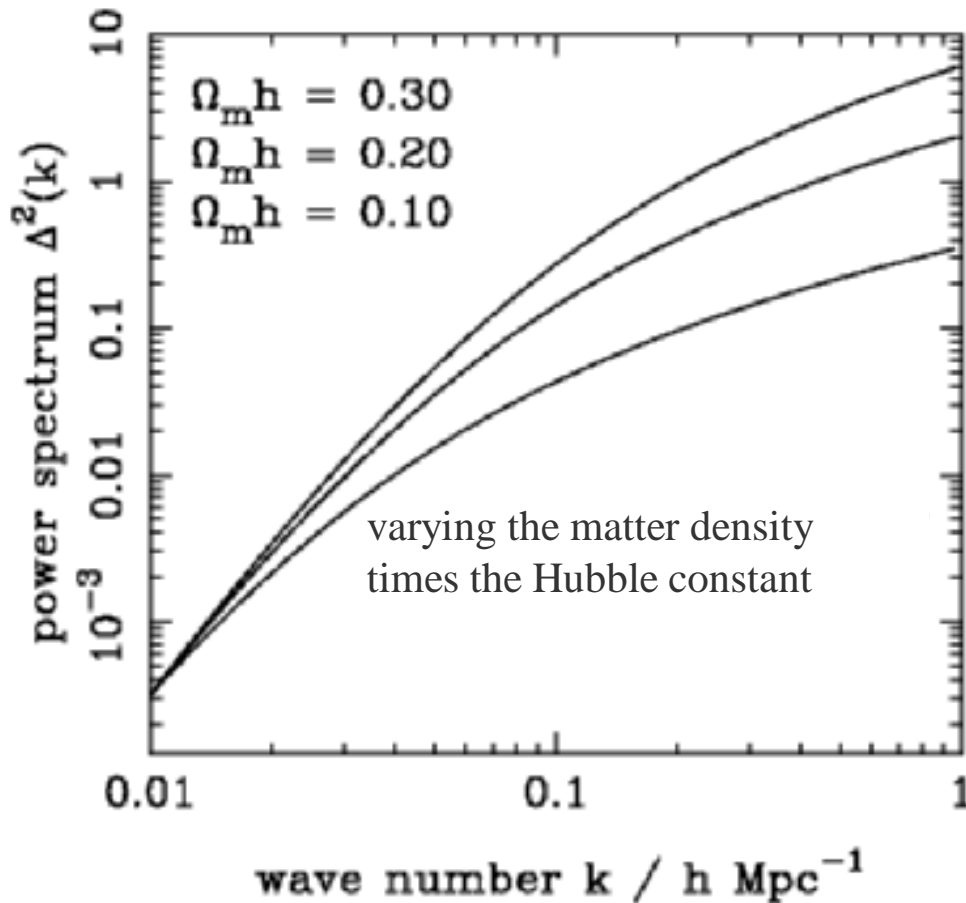
- collaboration of 30 astronomers split between Australia and the UK
- survey is now complete and has measured redshifts for 220000 galaxies in the local Universe (b-band selection)
- data has been released

<http://www.mso.anu.edu.au/2dFGRS/>

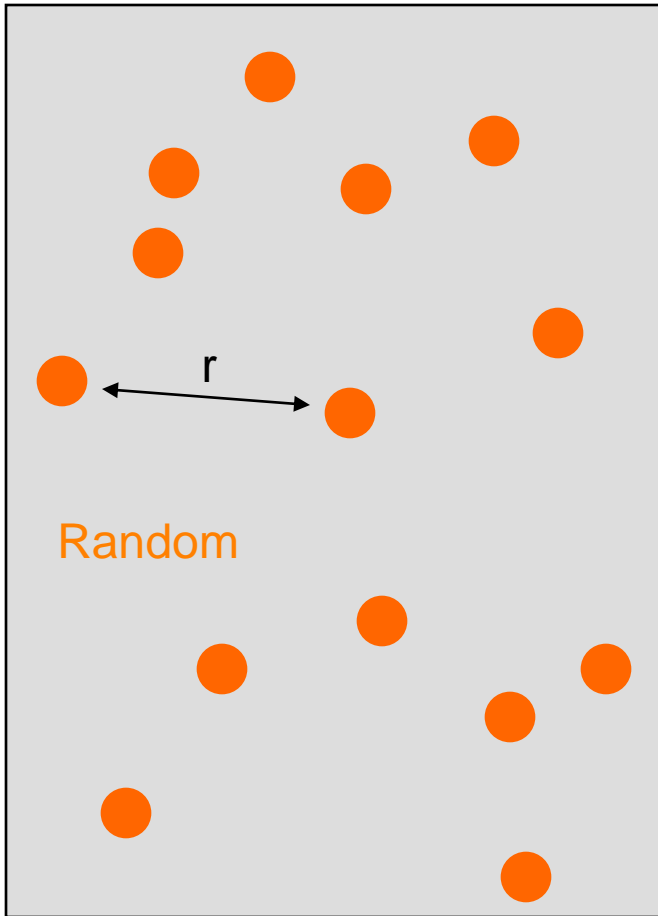
# The linear matter power spectrum

Can we use the power spectrum shape to tell us about evolution of scale?

Saw in last lecture that matter  $P(k)$  is fixed in the early universe, with simple evolution



# Measuring $\xi(r)$ and $P(k)$



Simple estimator:

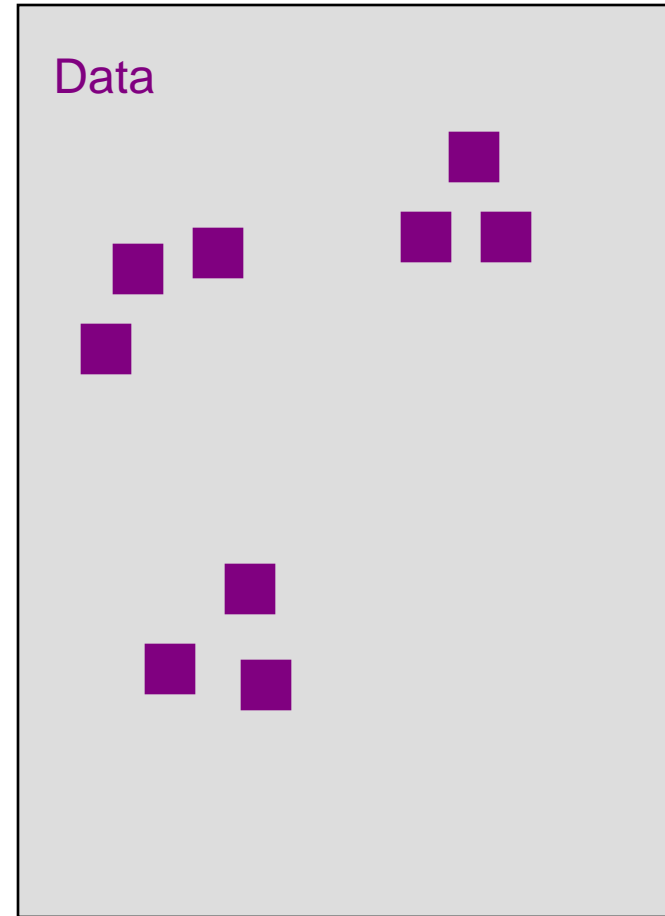
$$\xi(r) = DD(r)/RR(r) - 1$$

Advanced estimator:

$$\xi(r) = (DD - 2DR + RR)/RR$$

The latter does a better job with edge effects, which cause a bias to the mean density of points.

Usually 10x as many random points over SAME area / volume



Same techniques for  $P(k)$  - take Fourier transform of density field relative to a random catalog over same volume. Several techniques for this - see Tegmark et al. and Pope et al. Also "weighted" and mark correlations

## Errors on $\xi(r)$

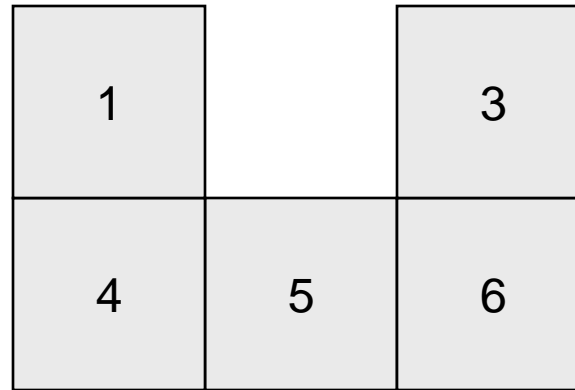
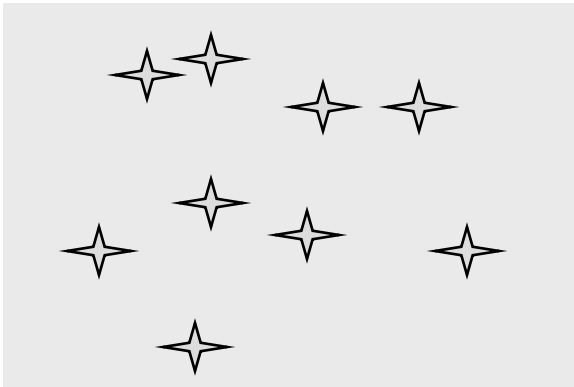
*Hardest part of estimating these statistics*

- On small scales, the errors are Poisson
- On large scales, errors correlated and typically larger than Poisson
- Use mocks catalogs
  - PROS: True measure of cosmic variance
  - CONS: Hard to include all observational effects and model clustering
- Use jack-knives (JK)
  - PROS: Uses the data directly
  - CONS: Noisy and unstable matrices



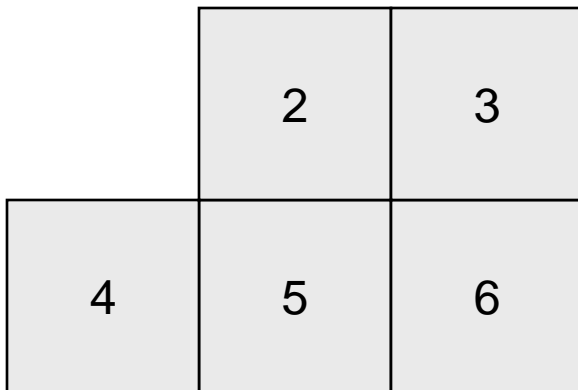
# Jack-knife errors

Real Data



N=6

- Split data into N equal subregions
- Remove each subregion in turn and compute  $\xi(r)$
- Measure variance between regions as function of scale



$$\sigma^2 = \frac{(N-1)}{N} \sum_{i=1}^N (\xi_i - \bar{\xi})^2$$

Note the (N-1) factor because there are N-1 estimates of mean

## Practicalities: measuring $\xi(\mathbf{r})$ for discrete samples

- the 2-pt function of a discrete random sampling of a density field is related to the correlation function of the field by

$$\langle n_g(\mathbf{r})n_g(\mathbf{r}') \rangle = \bar{n}(\mathbf{r})\bar{n}(\mathbf{r}') [1 + \xi(\mathbf{r}-\mathbf{r}')] + \bar{n}(\mathbf{r})\delta_D(\mathbf{r}-\mathbf{r}')$$

where  $n_g(\mathbf{r}) \equiv \sum_i \delta_D(\mathbf{r} - \mathbf{r}_i)$

shot noise term

given a synthetic catalogue (containing  $\alpha$  times as many galaxies) Poisson sampling the survey area  $n_s(\mathbf{r})$ , the correlation function can be estimated

$$1 + \langle \xi_{\text{field}} \rangle = \left( 1 + \alpha \frac{\langle DD \rangle}{\langle RR \rangle} \right) (1 + \sigma^2)$$

ratio of pair counts of separation  $\sim r$  in galaxy and synthetic catalogues

integral constraint (statistical bias as mean number of galaxies measured from survey itself)

# Practicalities: measuring $P(\mathbf{k})$ for discrete samples

as for the correlation function, given

$$F(\mathbf{r}) = n_g(\mathbf{r}) - n_s(\mathbf{r})/\alpha$$

the power spectrum can be written

$$\langle |F(\mathbf{k})|^2 \rangle = \int \frac{d^3 k'}{(2\pi)^3} [P(\mathbf{k}') - P(0)\delta_D(\mathbf{k})] |G(\mathbf{k} - \mathbf{k}')|^2 \\ + \left(1 + \frac{1}{\alpha}\right) \int d^3 r \bar{n}(\mathbf{r})$$

shot noise term (not as easily corrected as for the correlation function)

correction for the fact that not knowing true mean galaxy density

convolution with window function

# Practicalities: weighting galaxies by number density

If:

1. The wavelength  $2\pi/k$  is small compared with the survey scale
  2. fluctuations are Gaussian
- then the optimal weight for each galaxy is

$$w_i = \frac{1}{1 + \bar{n}(\mathbf{r}_i) \hat{P}(k)}$$

Depends on  $P(k)$   
prior



low densities - weights by galaxy  
high densities - weights by volume

change over scale dependent on  $P(k)$

# Practicalities: weighting galaxies by bias

- galaxies do not form a Poisson sampling of the matter distribution
- they are biased with respect to the distribution of mass

$$P_{\text{gal}}(k) = b^2(\text{galaxy}) P_{\text{mass}}(k)$$

- bias changes with galaxy colour and luminosity

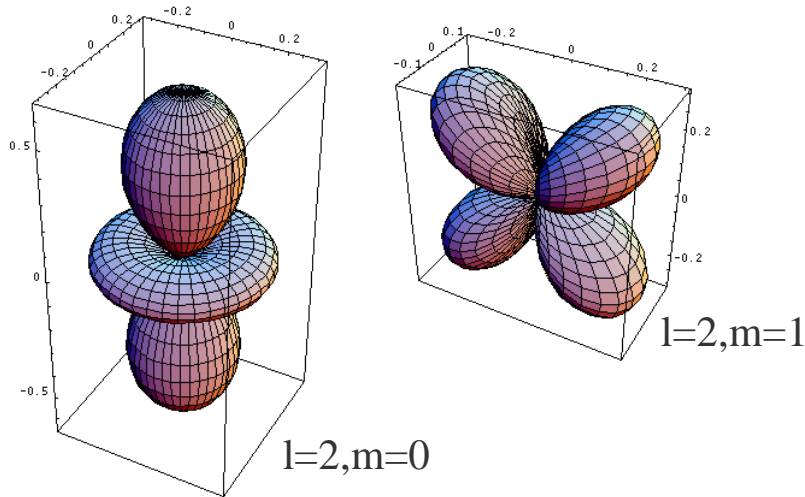
Given a sample of galaxies, each with linear bias  $b_j$ , the optimal weight is


$$w_i = \frac{b_i^2}{1 + \sum_j \bar{n}(\mathbf{r}_i, L_j) b_j^2 \hat{P}(k)}$$

up-weights very biased galaxies, containing the most signal

normalisation changes to match

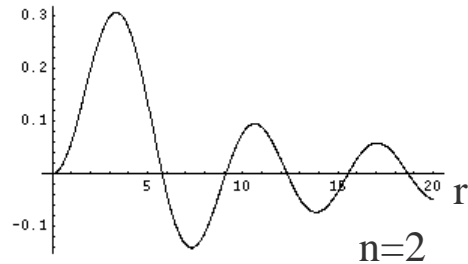
# Practicalities: weighting galaxies by bias



Spherical Harmonics  
()

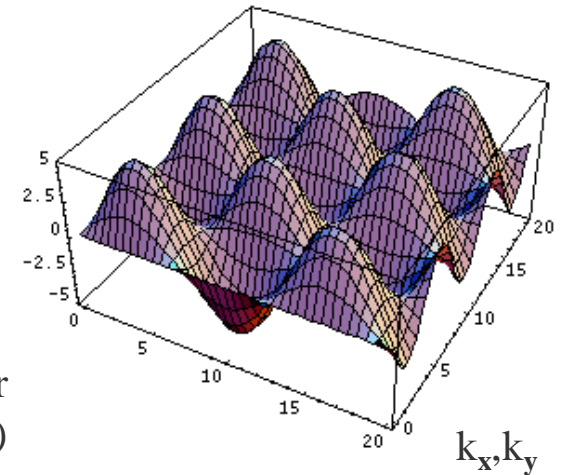
+

Spherical Bessel function ( $r$ )



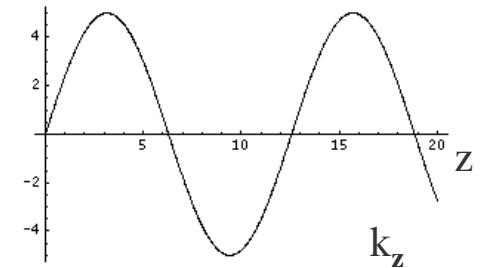
advantage: radial/angular split – more matched to survey geometry, easily model redshift space distortions

2d Fourier basis ( $x, y$ )



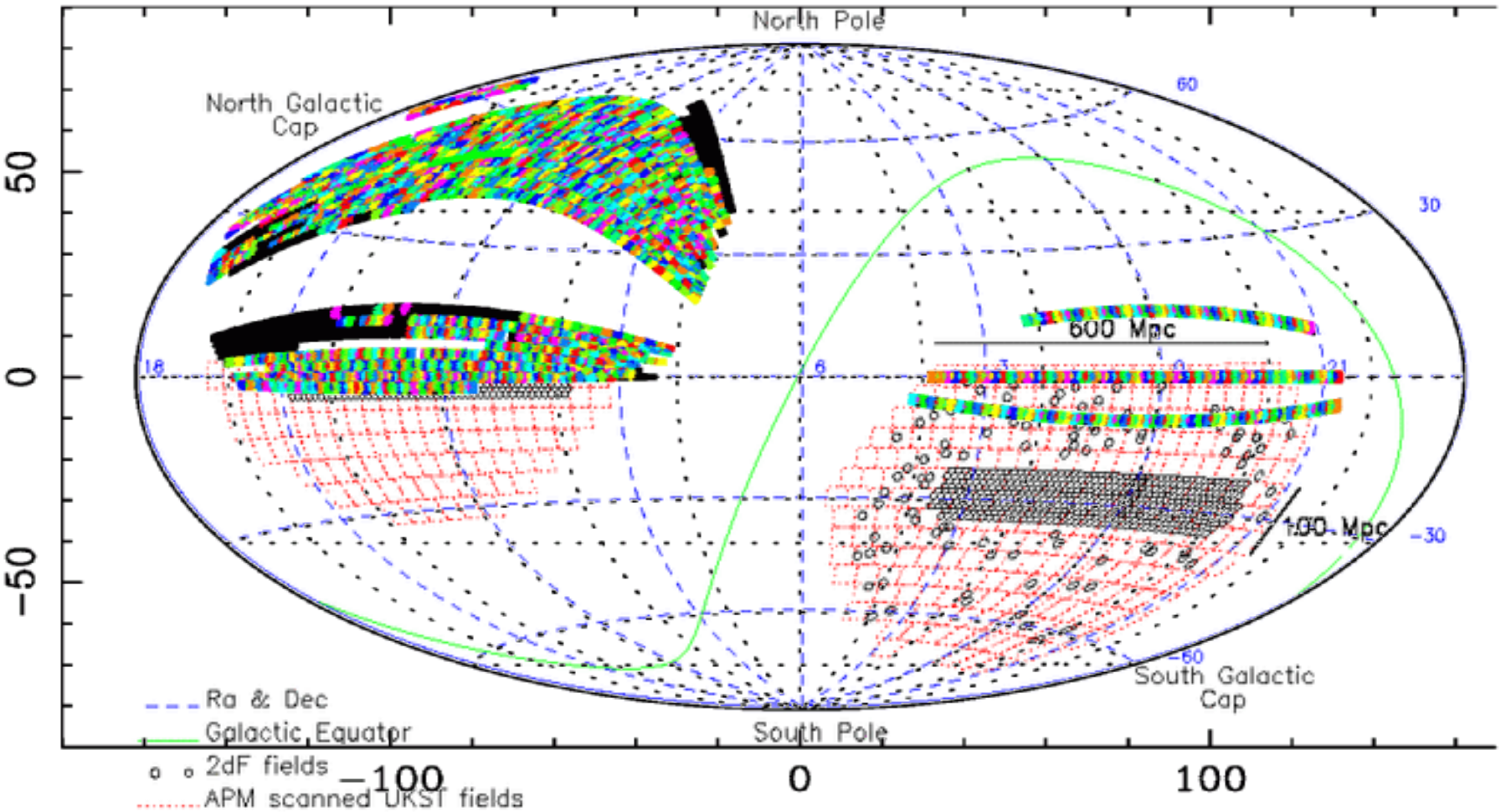
+

1d Fourier basis ( $z$ )

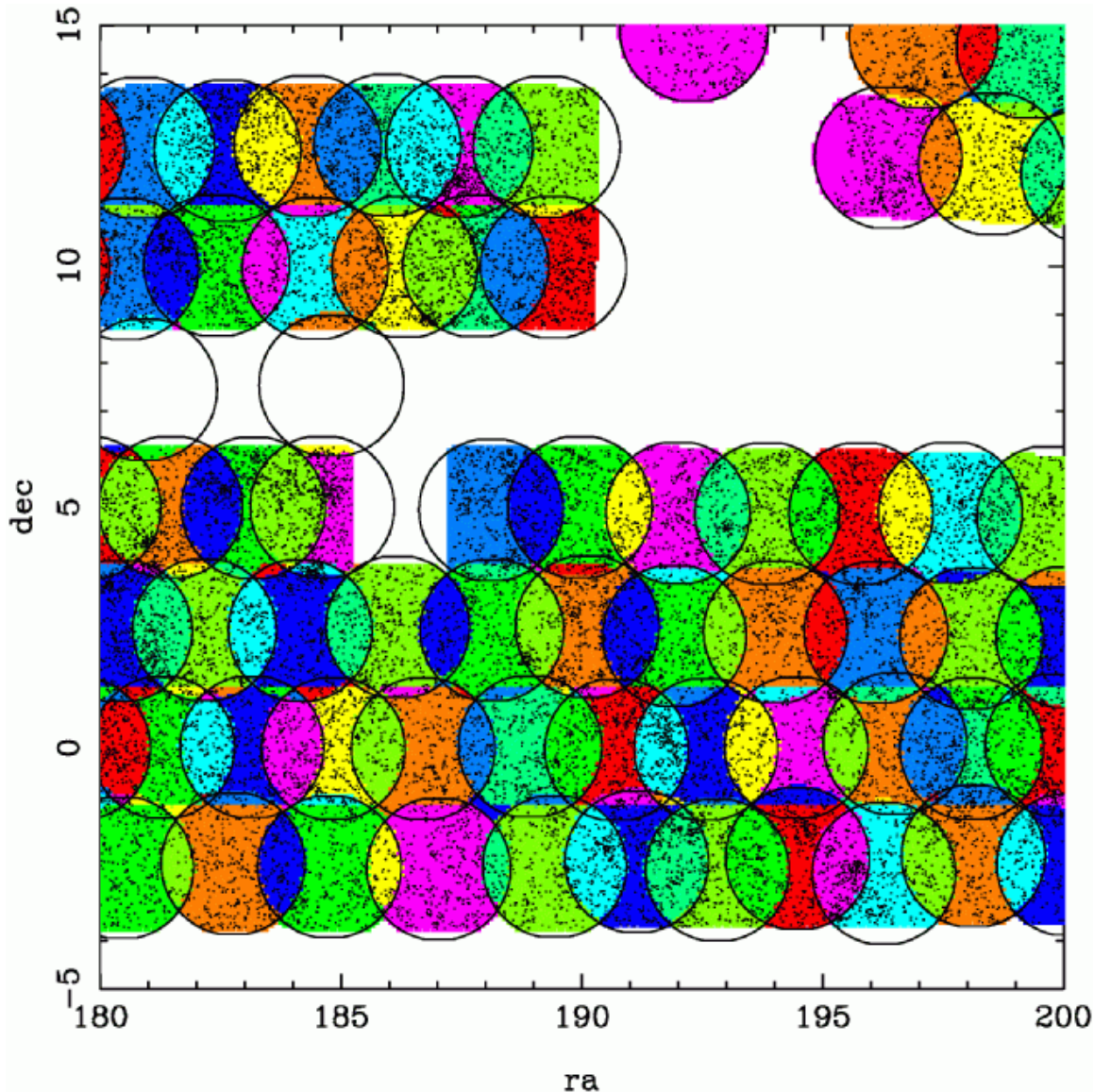


advantage: simplicity, speed

# SDSS DR4 survey geometry



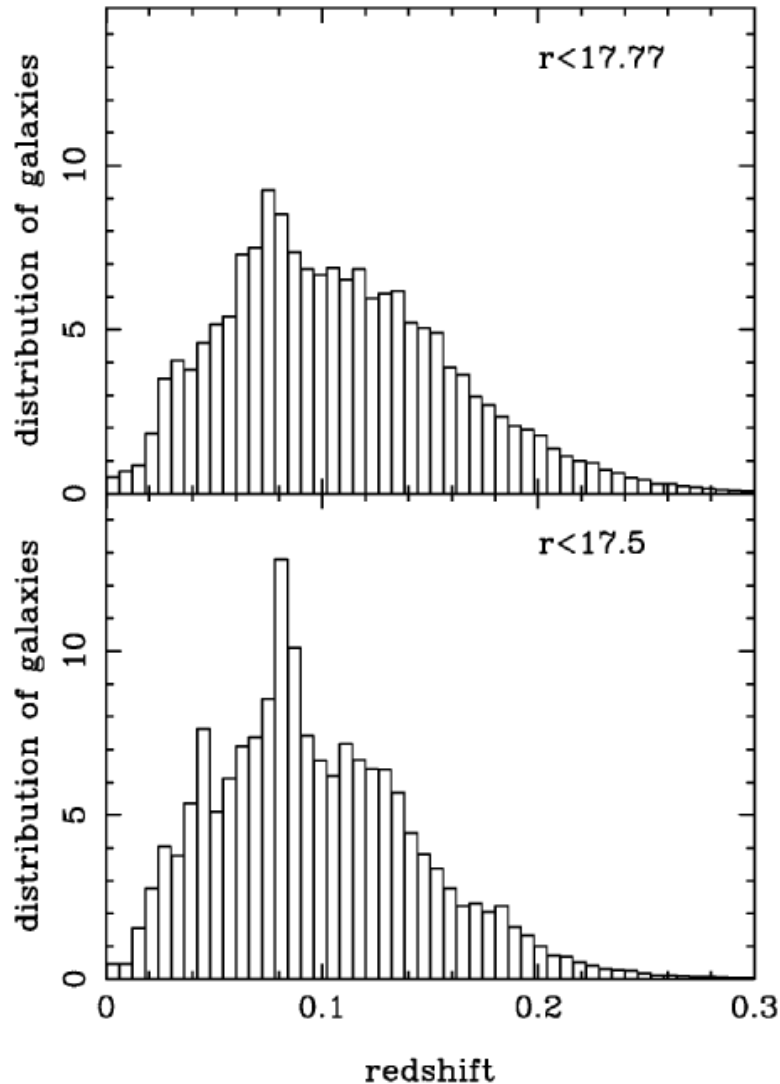
## Need to determine the angular mask



- both SDSS and 2dFGRS use an adaptive tiling strategy
- completeness varies between plate overlap regions
- also need to consider region covered by parent catalogue

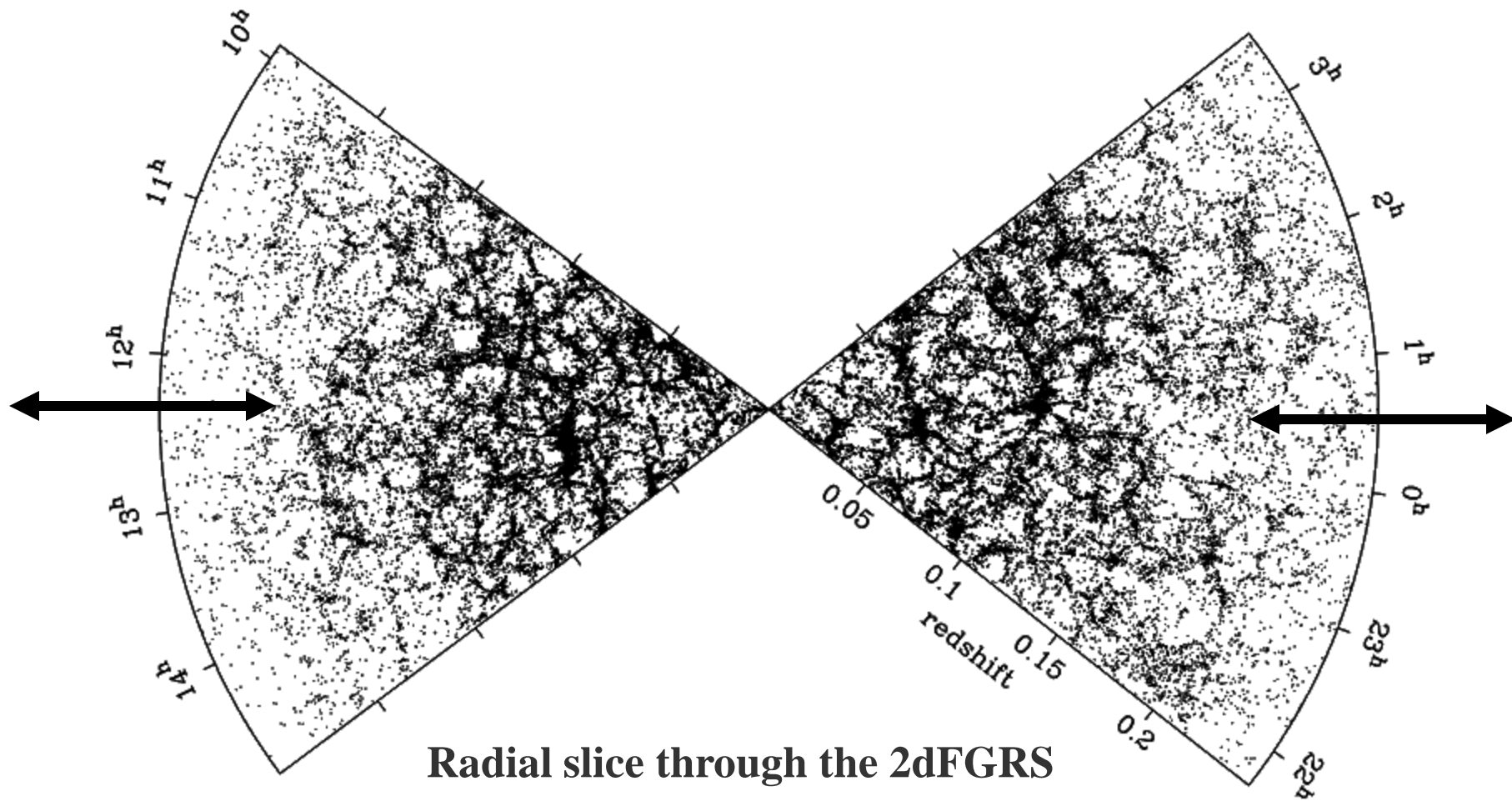


# Need to determine the radial galaxy distribution

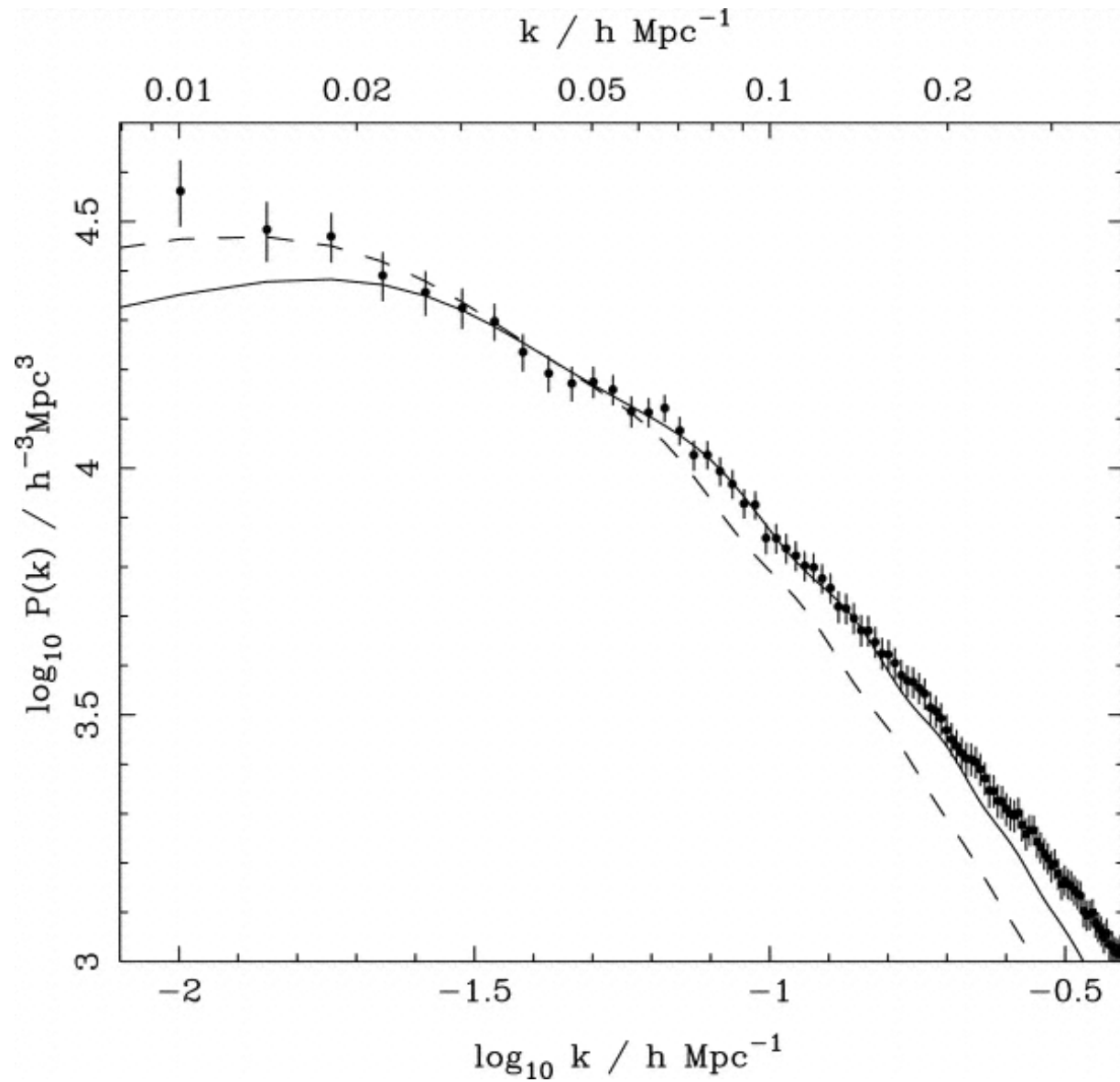


- for both the 2dFGRS and SDSS the magnitude limit changes with angular position
- Best approach - fit absolute magnitude function (allowing for K+E corrections)
- possible to also just fit to redshift distribution

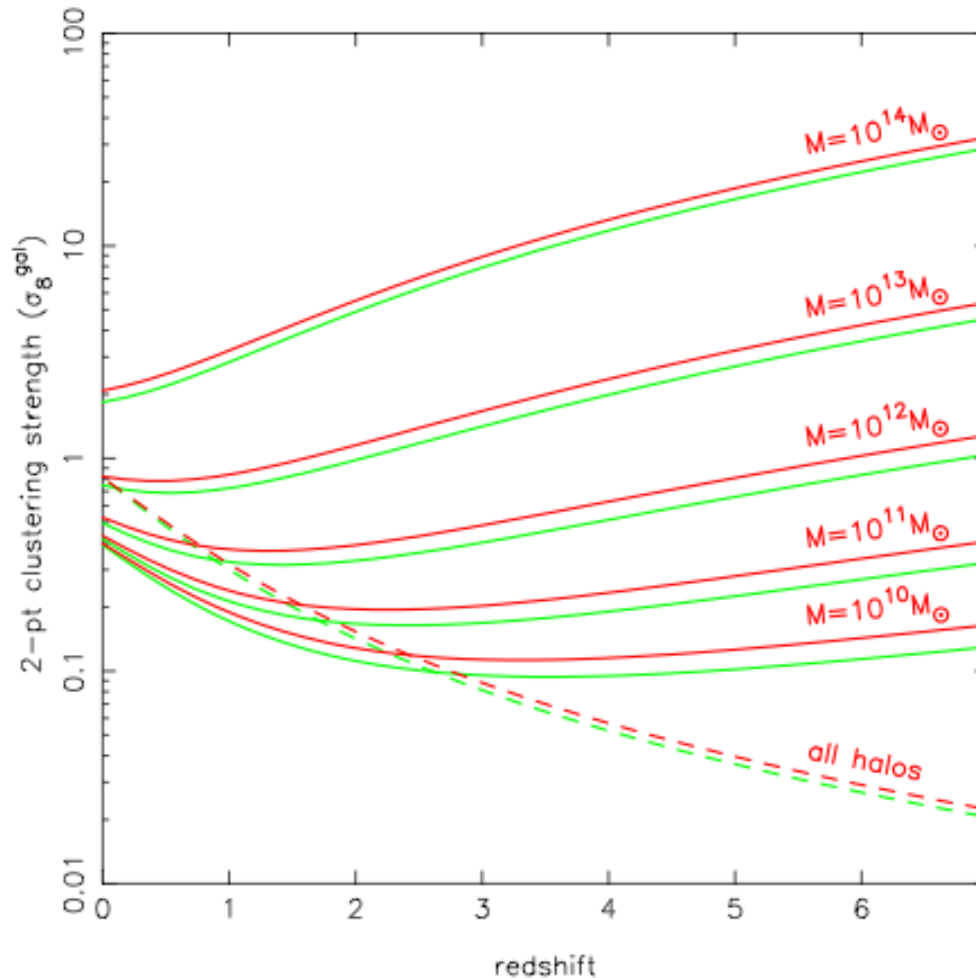
# Galaxy surveys probe DE through geometry & structure growth



# Latest power spectrum from SDSS



# Amplitude of clustering on large scales



$$\Omega_m = 0.25, \Omega_\Lambda = 0.75$$

$$\Omega_m = 0.3, \Omega_\Lambda = 0.7$$

Need to accurately know galaxy bias before we can get cosmological constraints - need to understand astrophysics of galaxy formation

# Main practical problem: galaxies do NOT sample the mass

observed redshift-space galaxy clustering power

galaxies might not trace the mass:  
scale dependent bias?

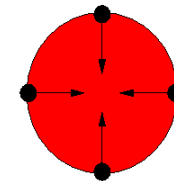
$$\frac{P_{\text{gal}}^s}{P_{\text{mass}}} = \frac{P_{\text{gal}}^s}{P_{\text{gal}}^r} \times \frac{P_{\text{gal}}^r}{P_{\text{mass}}}$$

linear matter power spectrum

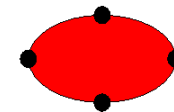
redshift-space distortions

Linear infall

random motions



Actual shape



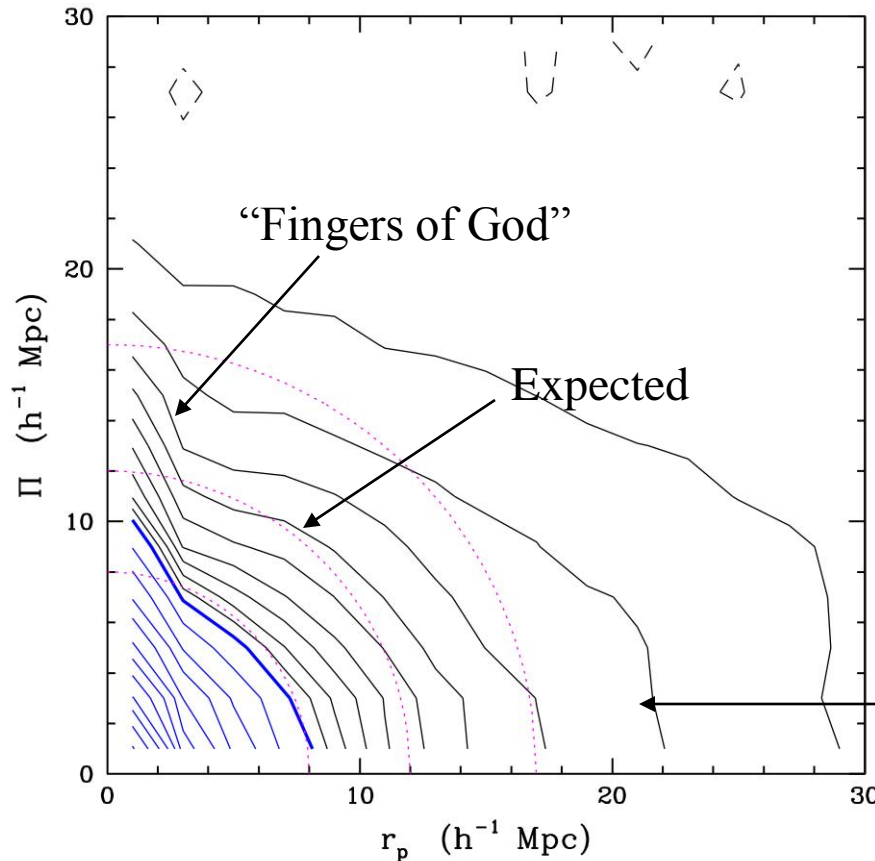
Apparent shape from below

At large distances, redshift-space distortions affect the power spectrum through:

$$P_s = P_r (1 + \beta \mu^2)^2 (1 + k^2 \mu^2 \sigma_p^2 / 2)^{-1}$$

# Redshift-space distortions

We only measure redshifts not distances

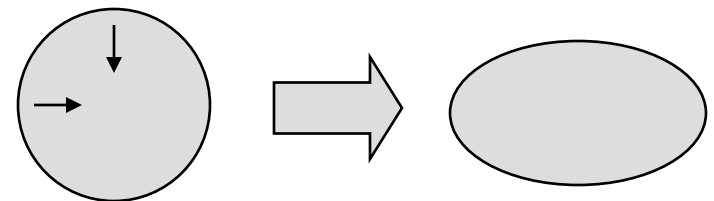


Therefore we usually quote  $\xi(r_p)$  as the "redshift-space" correlation function, and  $\xi(r_p)$  as the "real-space" correlation function.

We can compute the 2D correlation function  $\xi(r_p, \pi)$  then

$$w(r_p) = 2 \int_0^{\pi_{\max}} \xi(r_p, \pi) d\pi$$

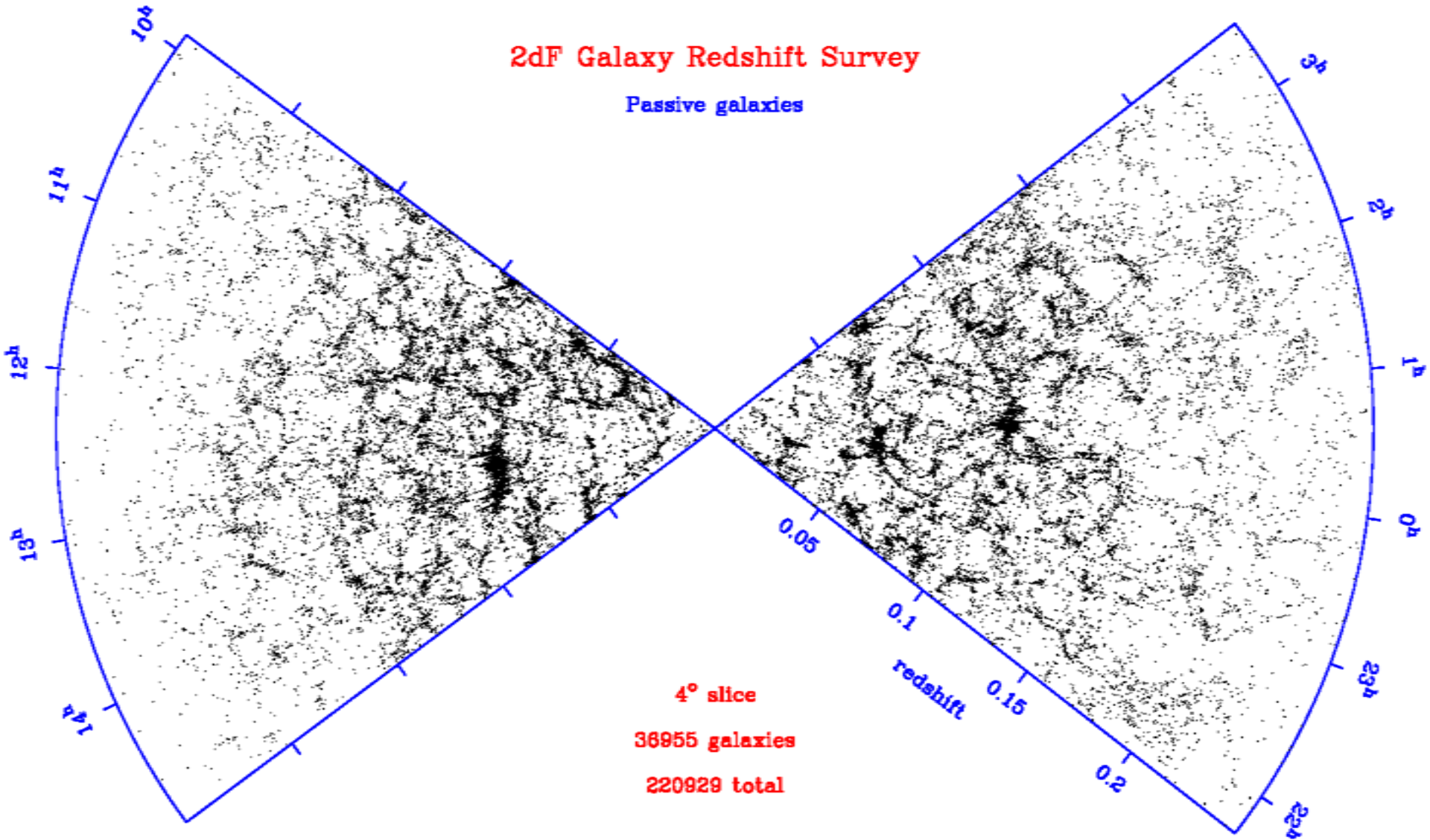
Infall around clusters



# Galaxy bias : Red galaxies

2dF Galaxy Redshift Survey

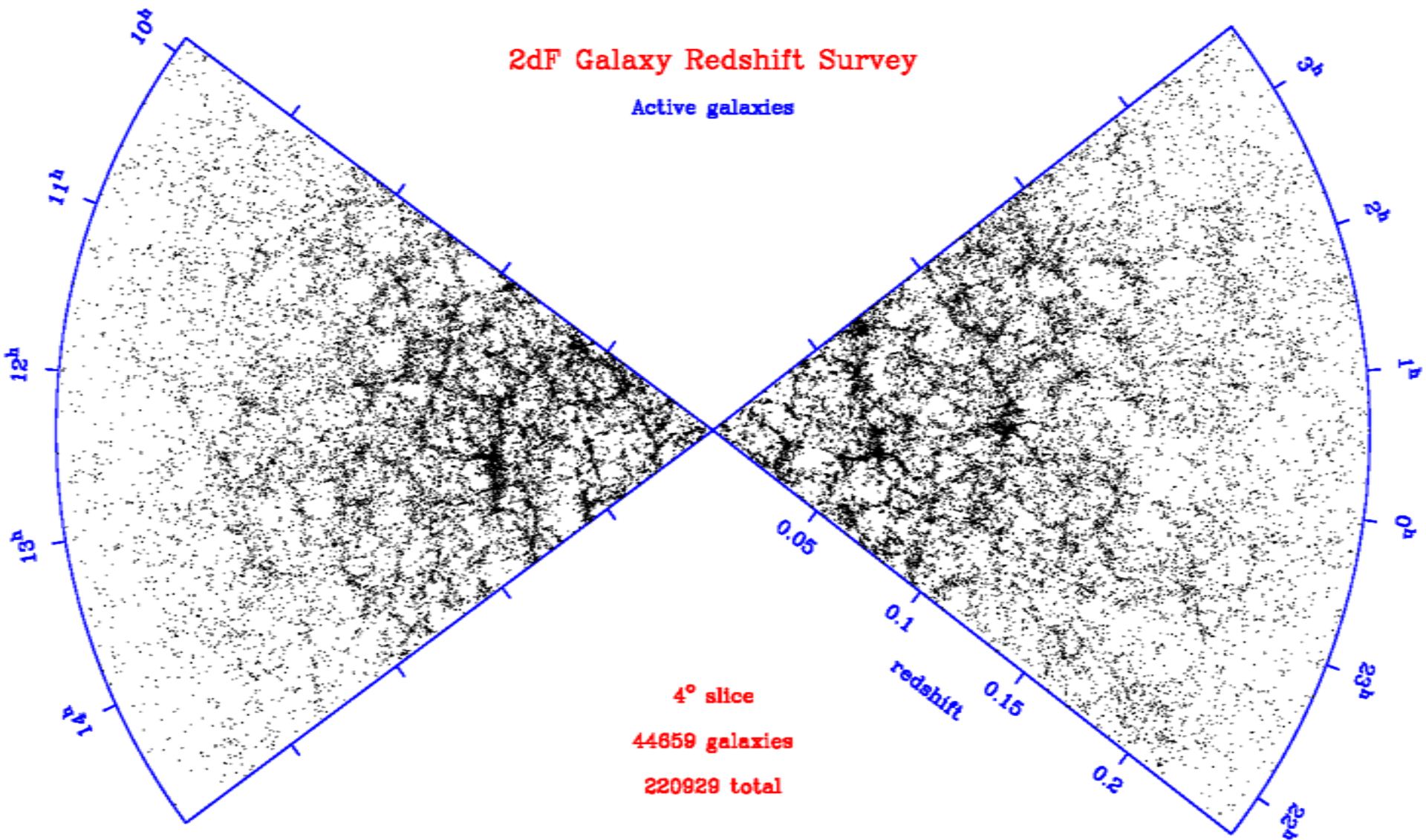
Passive galaxies



# Galaxy bias : Blue galaxies

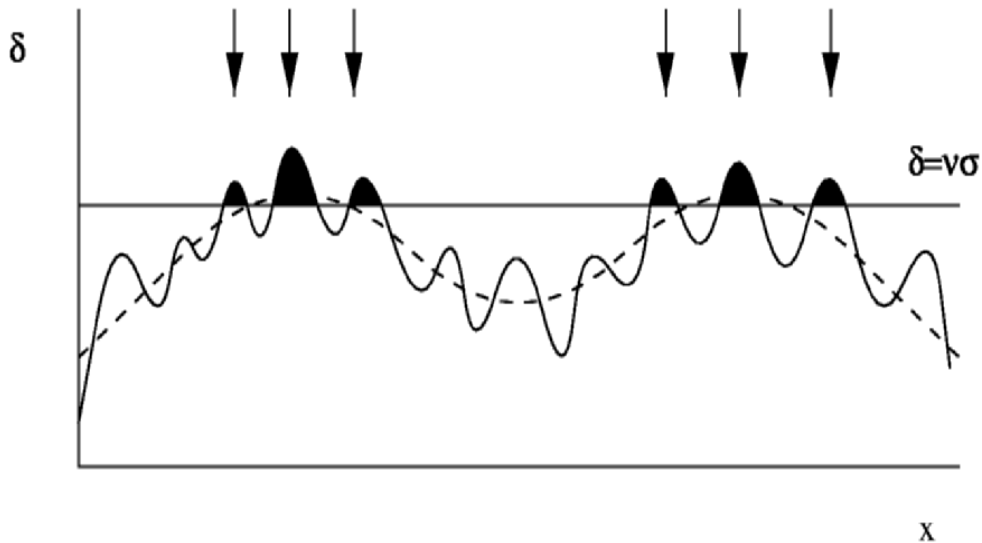
2dF Galaxy Redshift Survey

Active galaxies





# Large-scale bias is inevitable for rare systems



Cole-Kaiser-Mo-White:

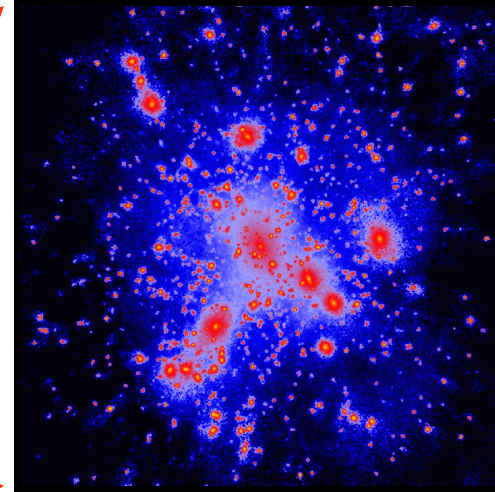
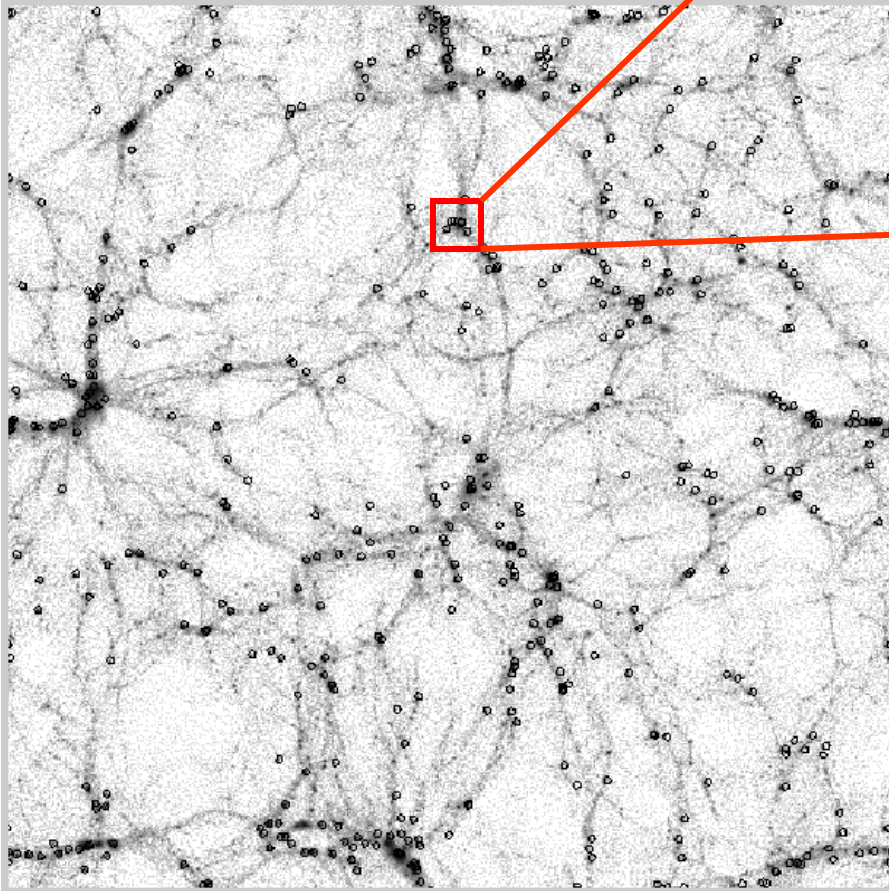
$$b(M) = 1 + (\nu^2 - 1)/\delta_c$$
$$\nu \equiv \delta_c/\sigma(M)$$

**Peak-background split:**  $\delta_c \rightarrow \delta_c - \varepsilon$ ;

$n(m) \rightarrow n(m) + (dn/dn)(dn/d\varepsilon) \varepsilon = n(m) [1 + b\varepsilon]$

**bias:**  $\xi \rightarrow b^2\xi$  depends on halo mass

# Small-scale bias is inevitable from halo profiles



N-body gives halo profile:

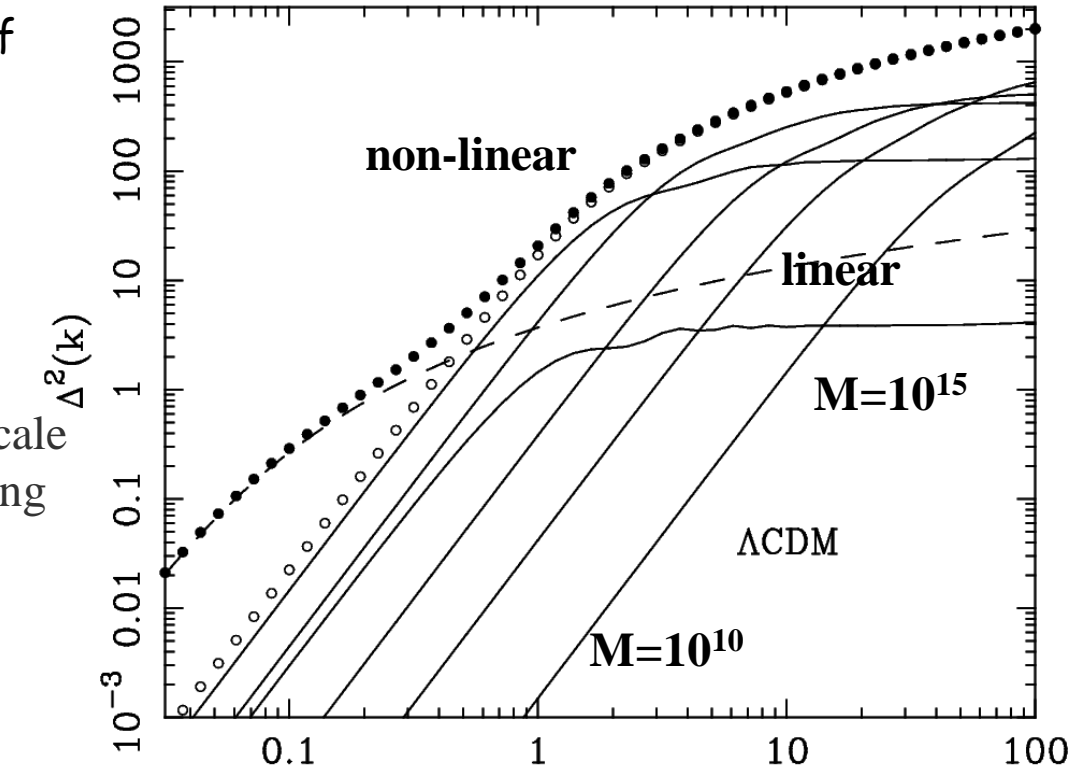
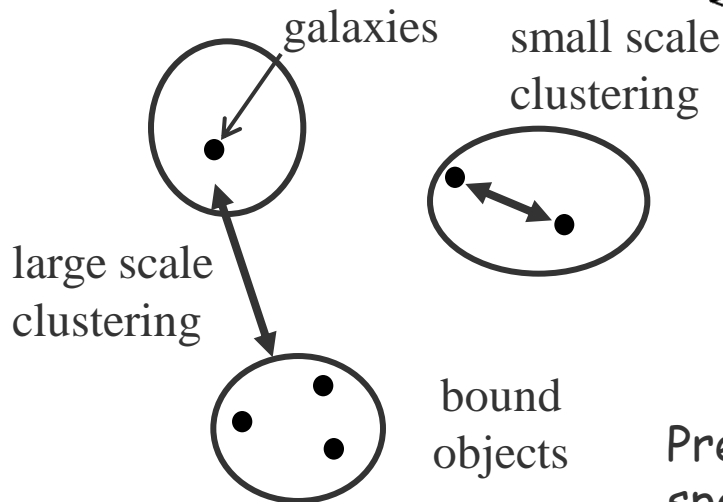
$$r = [y(1+y)^2]^{-1}; \quad y = r/r_c \quad (\text{NFW})$$

$$r = [y^{3/2}(1+y^{3/2})]^{-1}; \quad y = r/r_c \quad (\text{Moore})$$

(cf. Isothermal sphere  $r = 1/y^2$ )

# The halo model

- Simple model which splits galaxy clustering into 2 components
  - Small scale clustering of galaxies within a single halo
  - Large scale clustering between halos

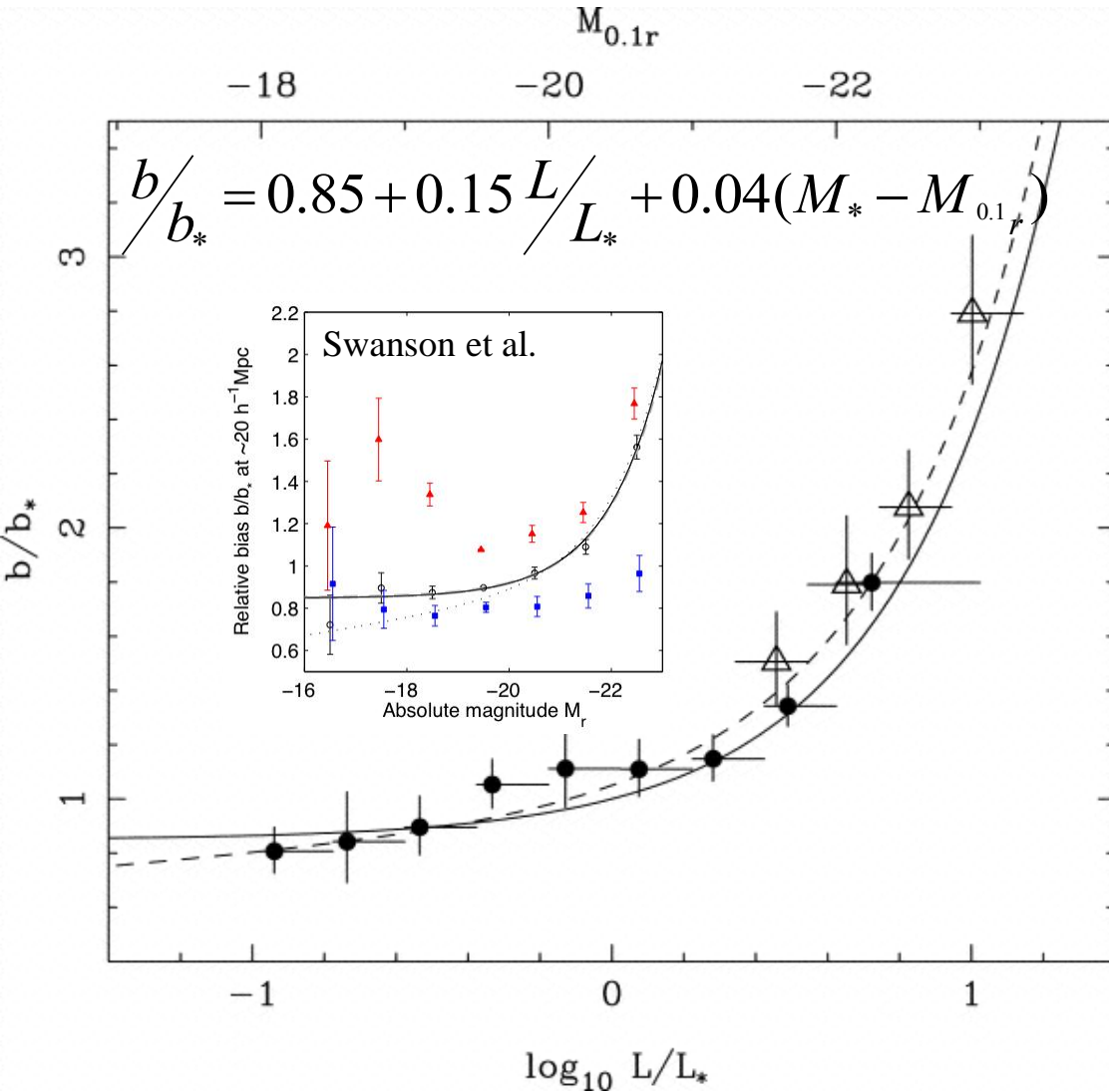


Predicts power spectrum of the form

$$P(k)_{\text{obs}} = b^2(k)P(k)_{\text{lin}} + P(k)_{\text{extra}}$$

# Observed amplitude of galaxy biasing

We see galaxies not dark matter



Maximal ignorance

$$\delta_{gal} = b \delta_{dm}$$

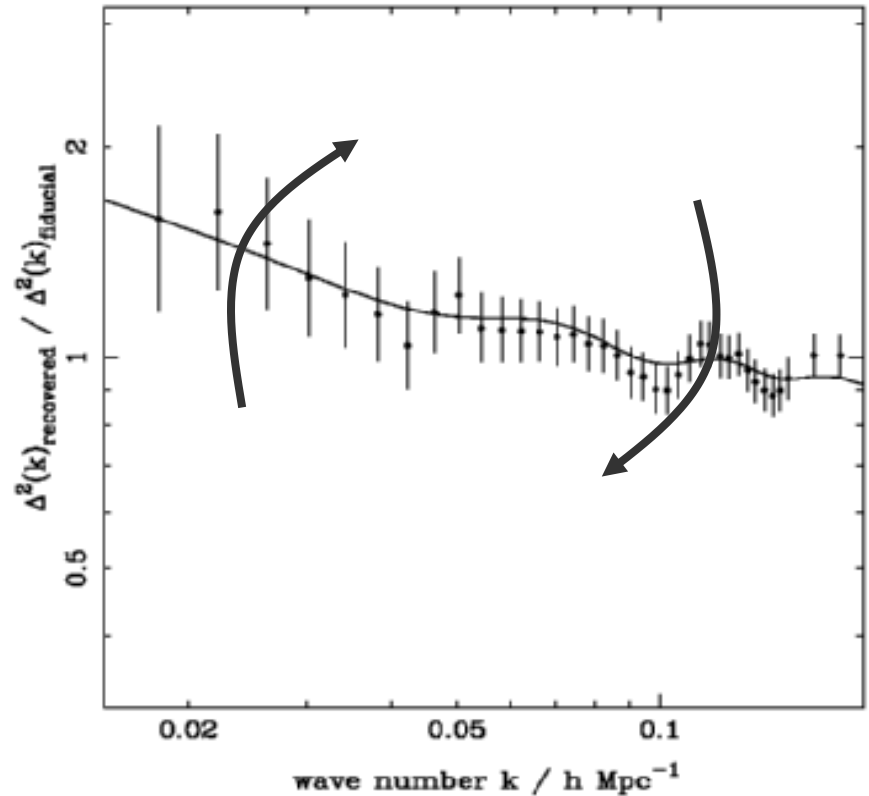
$$P(k)_{gal} = b^2 P(k)_{dm}$$

However, we know it depends on colour & L

*Is there also a scale dependence?*

# The problem with not correcting for bias

- assume that galaxies have luminosity-dependent bias on the large-scales of interest, with  $\langle b/b_* \rangle = 0.85 + 0.15(L/L_*)$  (Norberg et al. 2001)
- survey geometry means that larger scales are traced by more luminous galaxies
- leads to a potential tilt in the power
- can be corrected given model of bias

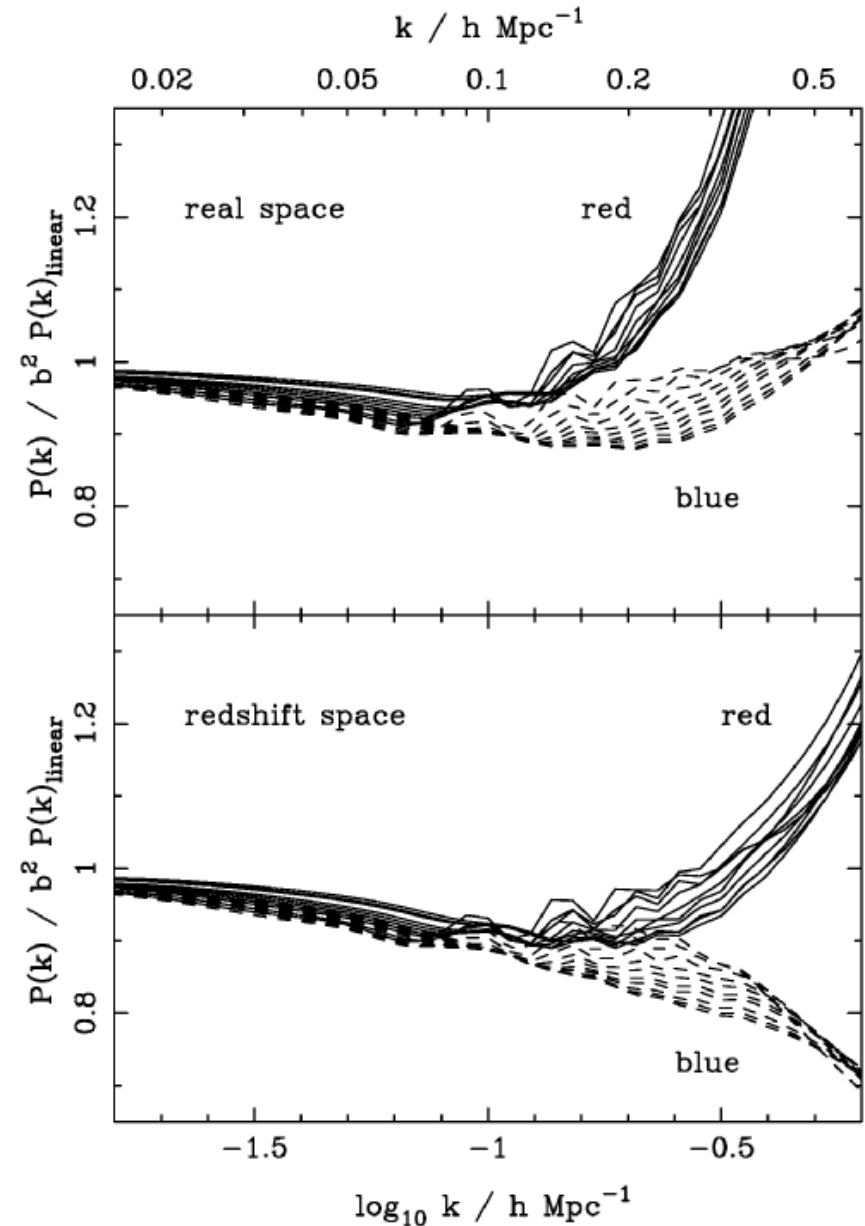


# Scale-dependent bias (from the halo model)

- cosmological dependence of bias is weak, so can adopt a fitting formula for all (reasonable) power spectra

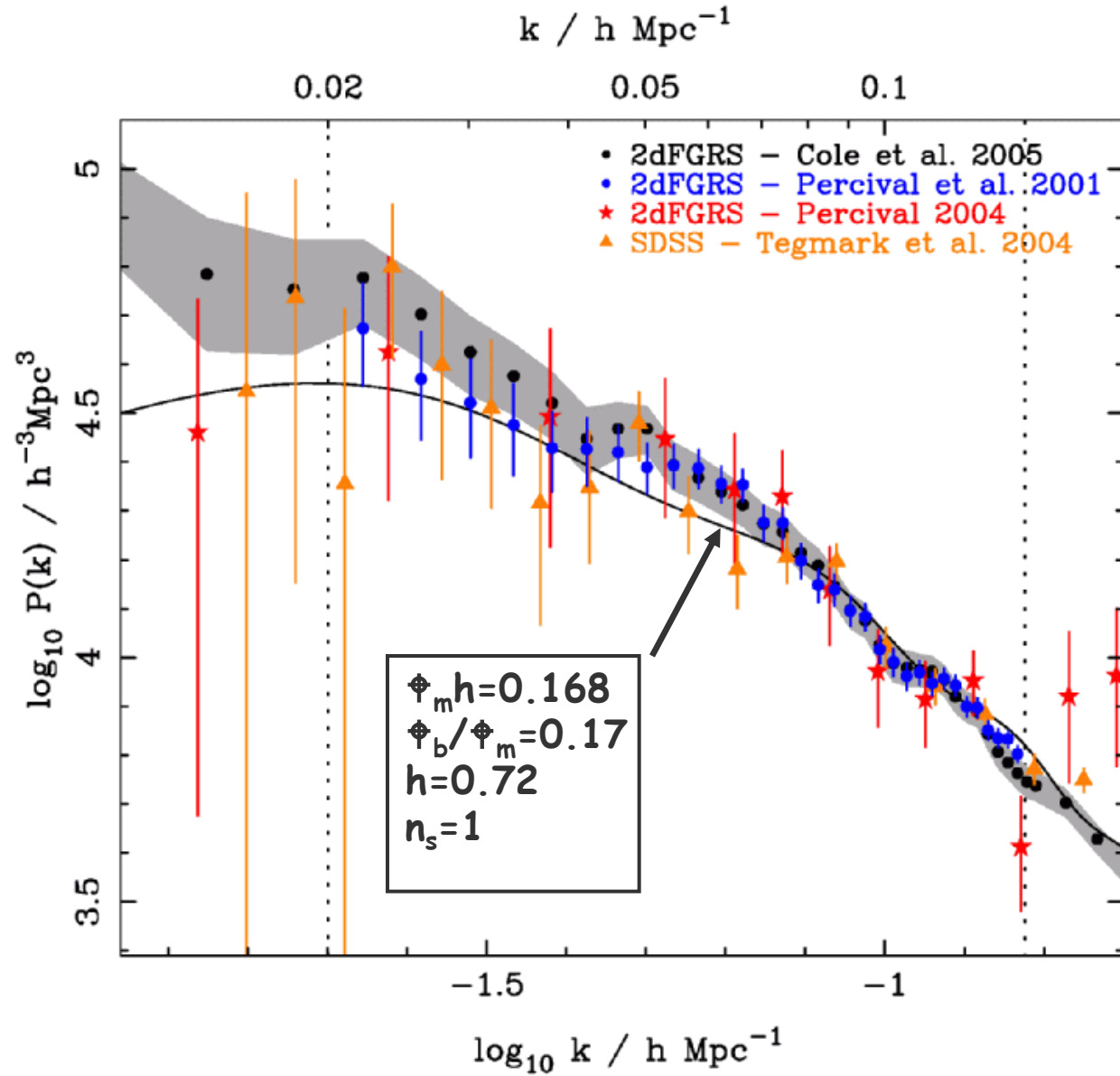
$$P_{\text{gal}}^r = \frac{1+Qk^2}{1+Ak} P_{\text{lin}}$$

- $A=1.4$  from halo model.  $Q$  is allowed to vary to cover lack of knowledge of small-scale effects.



# Cosmology

# Pre-2006 power spectra from SDSS and 2dFGRS





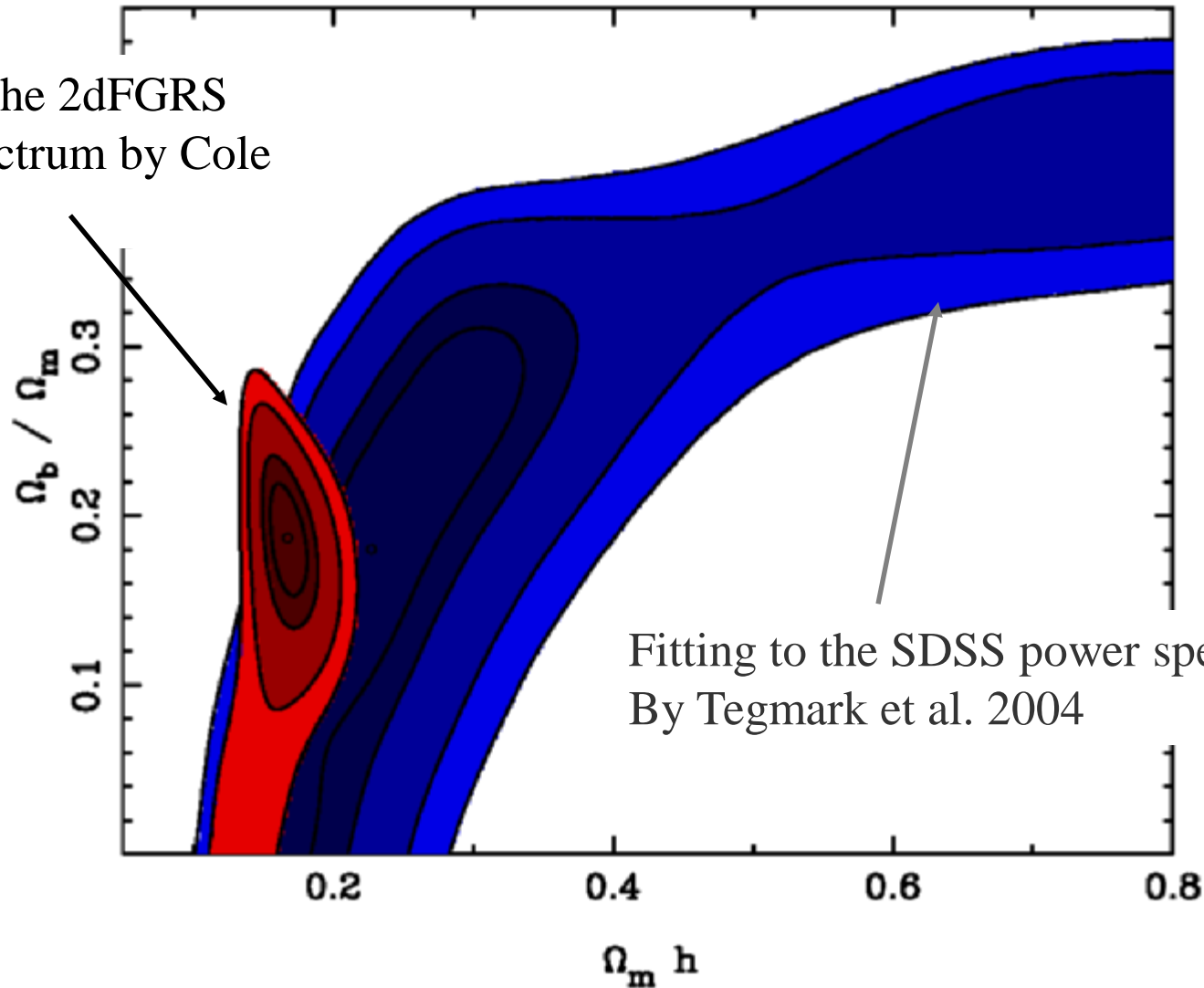
## Pre-2006 constraints from P(k)

SURVEY	publication	redshifts	method	$\Omega_m h$	$f_b$	$\Omega_m h$ $f_b=0.17$
2dFGRS	Percival et al. 2001	166,490	Fourier analysis	0.20 $\pm 0.03$	0.15 $\pm 0.07$	0.206 $\pm 0.023$
2dFGRS	Percival et al. 2004	142,756	Spherical Harmonics			0.215 $\pm 0.035$
2dFGRS	Cole et al. 2005	221,414	Fourier analysis	0.168 $\pm 0.016$	0.185 $\pm 0.046$	0.172 $\pm 0.014$
SDSS	Pope et al. 2004	205,484	KL analysis	0.264 $\pm 0.043$	0.286 $\pm 0.065$	0.207 $\pm 0.030$
SDSS	Tegmark et al. 2004	205,443	Spherical Harmonics			0.225 $\pm 0.040$
SDSS LRGs	Eisenstein et al 2005	46,748	correlation function			0.185 $\pm 0.015^*$

\*uses  $\Omega_b h^2=0.024$ , rather than  $f_b=0.17$

## 2dFGRS vs SDSS likelihood contours

Fitting to the 2dFGRS  
power spectrum by Cole  
et al. 2005



Fitting to the SDSS power spectrum  
By Tegmark et al. 2004

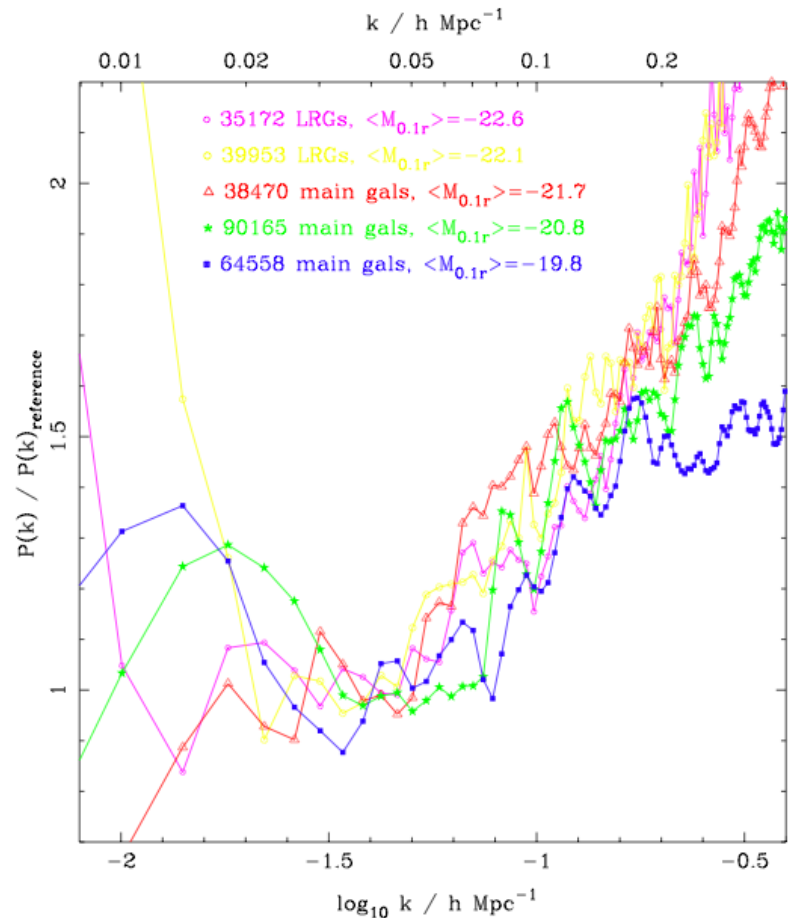
# WMAP 3-year analysis found a discrepancy

Parameter	WMAP Only	WMAP +CBI+VSA	WMAP+ACBAR +BOOMERanG	WMAP + 2dFGRS
$100\Omega_b h^2$	$2.233^{+0.072}_{-0.091}$	$2.203^{+0.072}_{-0.090}$	$2.228^{+0.066}_{-0.082}$	$2.223^{+0.066}_{-0.083}$
$\Omega_m h^2$	$0.1268^{+0.0073}_{-0.0128}$	$0.1238^{+0.0066}_{-0.0118}$	$0.1271^{+0.0070}_{-0.0128}$	$0.1262^{+0.0050}_{-0.0103}$
$h$	$0.734^{+0.028}_{-0.038}$	$0.738^{+0.028}_{-0.037}$	$0.733^{+0.030}_{-0.038}$	$0.732^{+0.018}_{-0.025}$
$A$	$0.801^{+0.043}_{-0.054}$	$0.798^{+0.047}_{-0.057}$	$0.801^{+0.048}_{-0.056}$	$0.799^{+0.042}_{-0.051}$
$\tau$	$0.088^{+0.028}_{-0.034}$	$0.084^{+0.031}_{-0.038}$	$0.084^{+0.027}_{-0.034}$	$0.083^{+0.027}_{-0.031}$
$n_s$	$0.951^{+0.015}_{-0.019}$	$0.945^{+0.015}_{-0.019}$	$0.949^{+0.015}_{-0.019}$	$0.948^{+0.014}_{-0.018}$
$\sigma_8$	$0.744^{+0.050}_{-0.060}$	$0.722^{+0.044}_{-0.056}$	$0.742^{+0.045}_{-0.057}$	$0.737^{+0.033}_{-0.045}$
$\Omega_m$	$0.238^{+0.027}_{-0.045}$	$0.229^{+0.026}_{-0.042}$	$0.239^{+0.025}_{-0.046}$	$0.236^{+0.016}_{-0.029}$

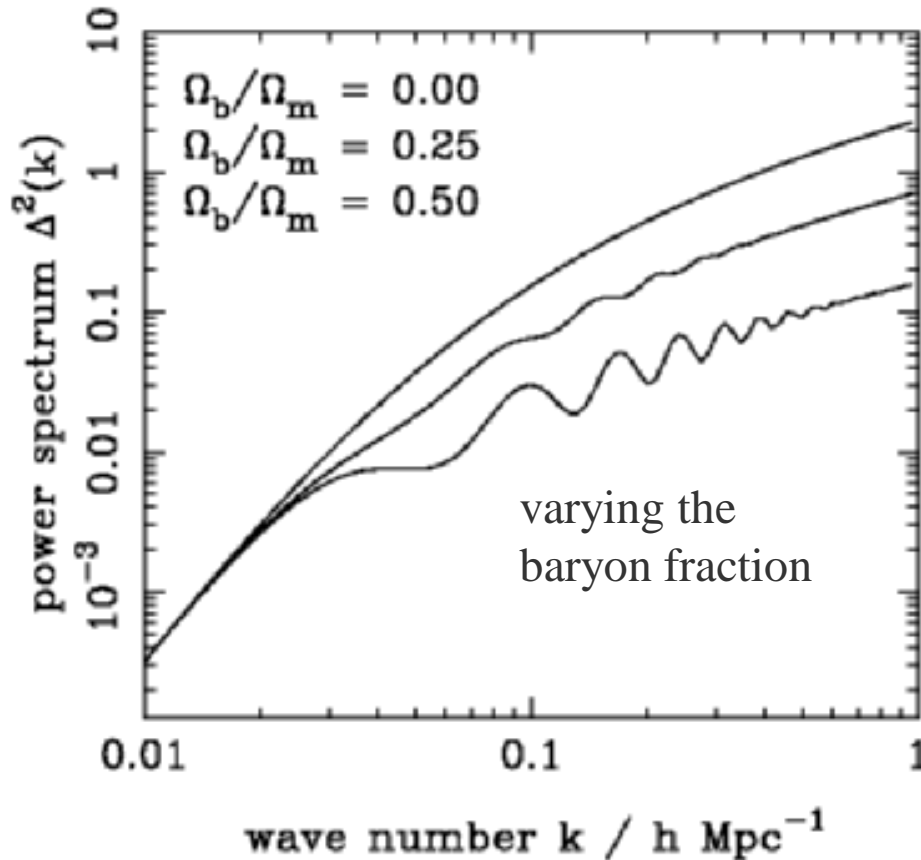
Parameter	WMAP+ SDSS	WMAP+ LRG	WMAP+ SNLS	WMAP + SN Gold	WMAP+ CFHTLS
$100\Omega_b h^2$	$2.233^{+0.062}_{-0.086}$	$2.242^{+0.062}_{-0.084}$	$2.233^{+0.069}_{-0.088}$	$2.227^{+0.065}_{-0.082}$	$2.247^{+0.064}_{-0.082}$
$\Omega_m h^2$	$0.1329^{+0.0057}_{-0.0109}$	$0.1337^{+0.0047}_{-0.0098}$	$0.1295^{+0.0055}_{-0.0106}$	$0.1349^{+0.0054}_{-0.0106}$	$0.1410^{+0.0042}_{-0.0094}$
$h$	$0.709^{+0.024}_{-0.032}$	$0.709^{+0.016}_{-0.023}$	$0.723^{+0.021}_{-0.030}$	$0.701^{+0.020}_{-0.026}$	$0.686^{+0.017}_{-0.024}$
$A$	$0.813^{+0.042}_{-0.052}$	$0.816^{+0.042}_{-0.049}$	$0.808^{+0.044}_{-0.051}$	$0.827^{+0.045}_{-0.053}$	$0.852^{+0.036}_{-0.047}$
$\tau$	$0.079^{+0.029}_{-0.032}$	$0.082^{+0.028}_{-0.033}$	$0.085^{+0.028}_{-0.032}$	$0.079^{+0.028}_{-0.034}$	$0.088^{+0.021}_{-0.031}$
$n_s$	$0.948^{+0.015}_{-0.018}$	$0.951^{+0.014}_{-0.018}$	$0.950^{+0.015}_{-0.019}$	$0.946^{+0.015}_{-0.019}$	$0.950^{+0.015}_{-0.019}$
$\sigma_8$	$0.772^{+0.036}_{-0.045}$	$0.781^{+0.032}_{-0.045}$	$0.758^{+0.038}_{-0.052}$	$0.784^{+0.035}_{-0.049}$	$0.826^{+0.023}_{-0.035}$
$\Omega_m$	$0.266^{+0.025}_{-0.040}$	$0.267^{+0.017}_{-0.029}$	$0.249^{+0.023}_{-0.034}$	$0.276^{+0.022}_{-0.036}$	$0.301^{+0.018}_{-0.031}$

# Is there large-scale scale dependent bias?

- SDSS data show a shape change caused by scale dependent bias dependent on r-band luminosity
- Obvious change on scales  $k > 0.2 h \text{Mpc}^{-1}$
- Inconclusive on large scales, but there may be something there
- This effect is far less significant than change in overall bias amplitude (curves corrected in plot) with luminosity



# Baryon oscillations in the large-scale matter power spectrum



“Wavelength” of baryonic acoustic oscillations is determined by the comoving sound horizon at recombination

$$k_{\text{bao}} = 2\pi/s$$

At early times can ignore dark energy, so comoving sound horizon is given by

$$s = \frac{1}{H_0 \Omega_m^{1/2}} \int_0^{a_*} da \frac{c_s}{(a + a_{\text{eq}})^{1/2}}$$

Sound speed  $c_s$

Gives the comoving sound horizon  $\sim 110h^{-1}\text{Mpc}$ , and BAO wavelength  $0.06h\text{Mpc}^{-1}$

# BAO in the galaxy power spectrum

Linear baryon acoustic oscillations are ratio of linear matter power spectrum to a smooth fit

$$B_{\text{lin}} = \frac{P(k)_{\text{lin}}}{\bar{P}(k)_{\text{lin}}}$$

Suppose that we measure an observed power that is related to the linear power by (halo model)

$$P_{\text{obs}}(k) = b^2(k)P(k)_{\text{lin}} + P(k)_{\text{extra}}$$

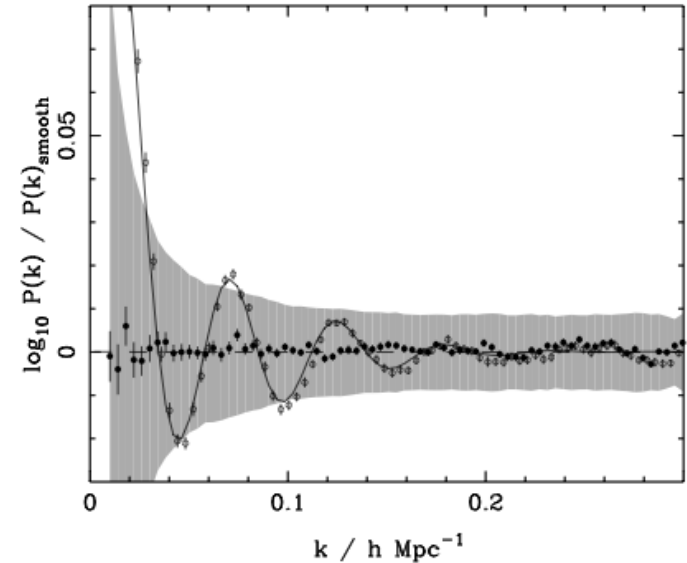
Then observed oscillations are related to linear BAO by

$$B_{\text{obs}} = \frac{P(k)_{\text{obs}}}{\bar{P}(k)_{\text{obs}}} = g(k)B_{\text{lin}} + [1 - g(k)]$$

No change in position of oscillations, just a damping term. Eisenstein, Seo & White (2006) argued that this was well fitted by a Gaussian.

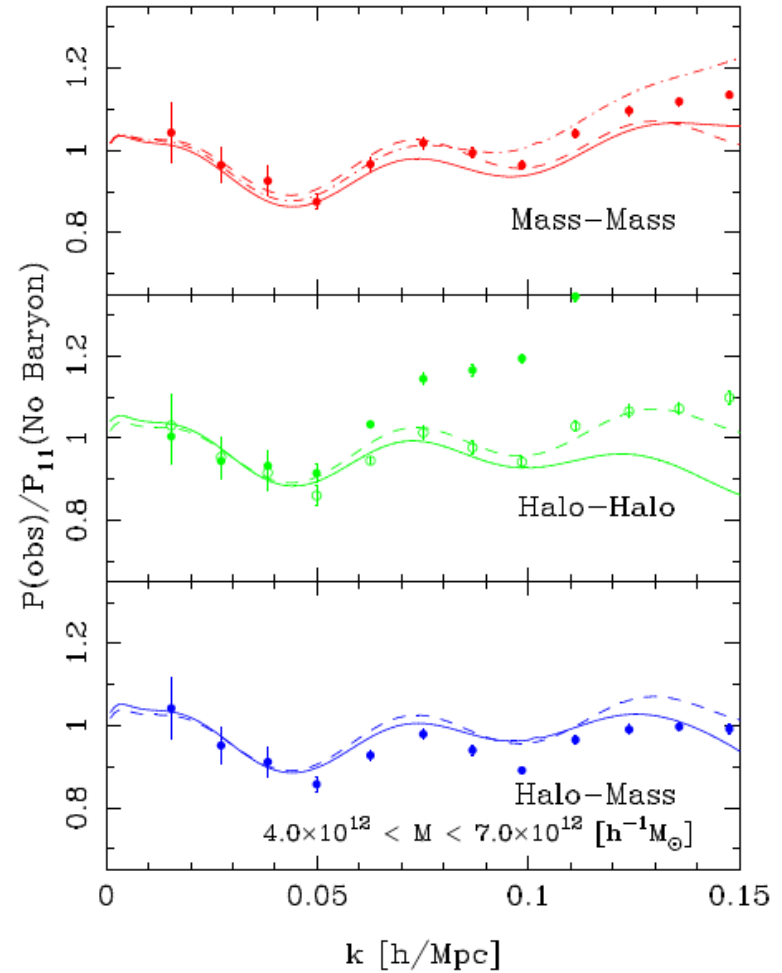
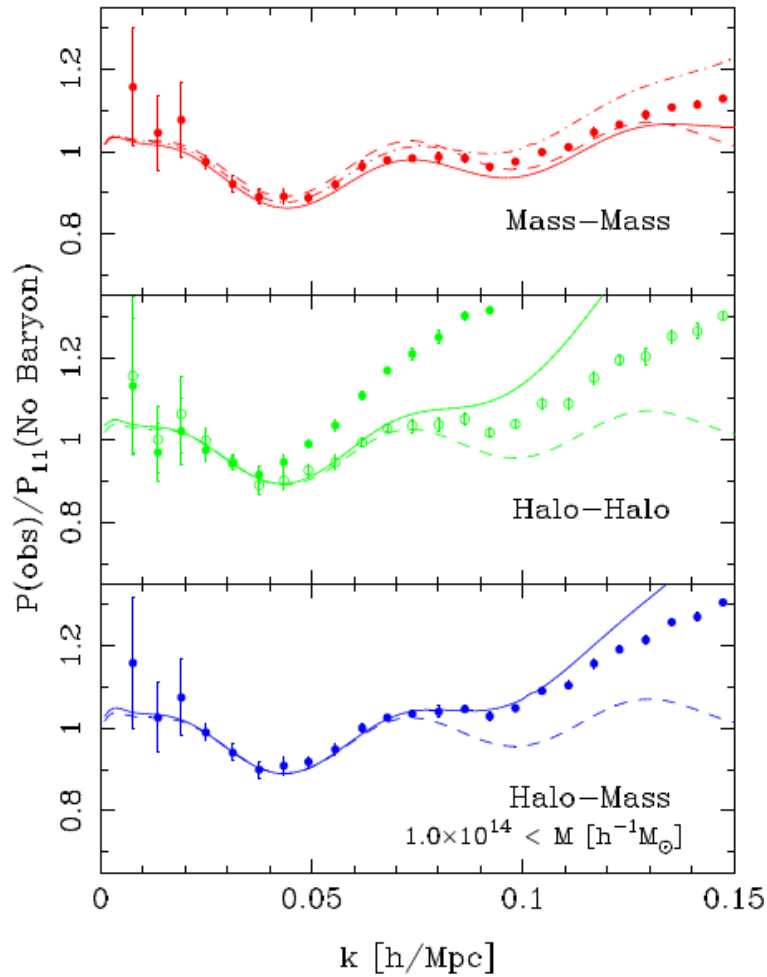
$$g(k) = \frac{b^2(k)\bar{P}(k)_{\text{lin}}}{\bar{P}(k)_{\text{obs}}}$$

To change the observed positions of BAO, we need sharp features in the observed power?



fit data with a 2-component model comprising a smooth spline (node separation  $0.05h\text{Mpc}^{-1}$ ), and the sinusoidal (in the transfer function) multiplicative BAO component usually applied to a CDM model. The ability of this model to fit linear CDM power spectra is good.

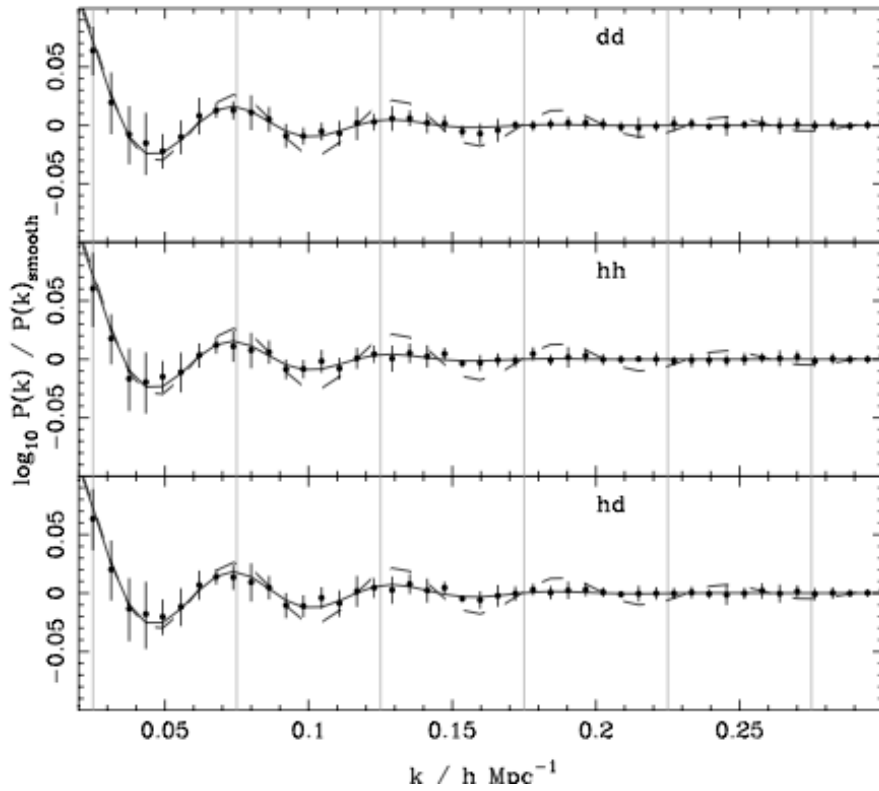
# “systematic errors” in BAO measurements



Plots from  
Smith, Scoccimarro & Sheth 2006, astro-ph/0609547

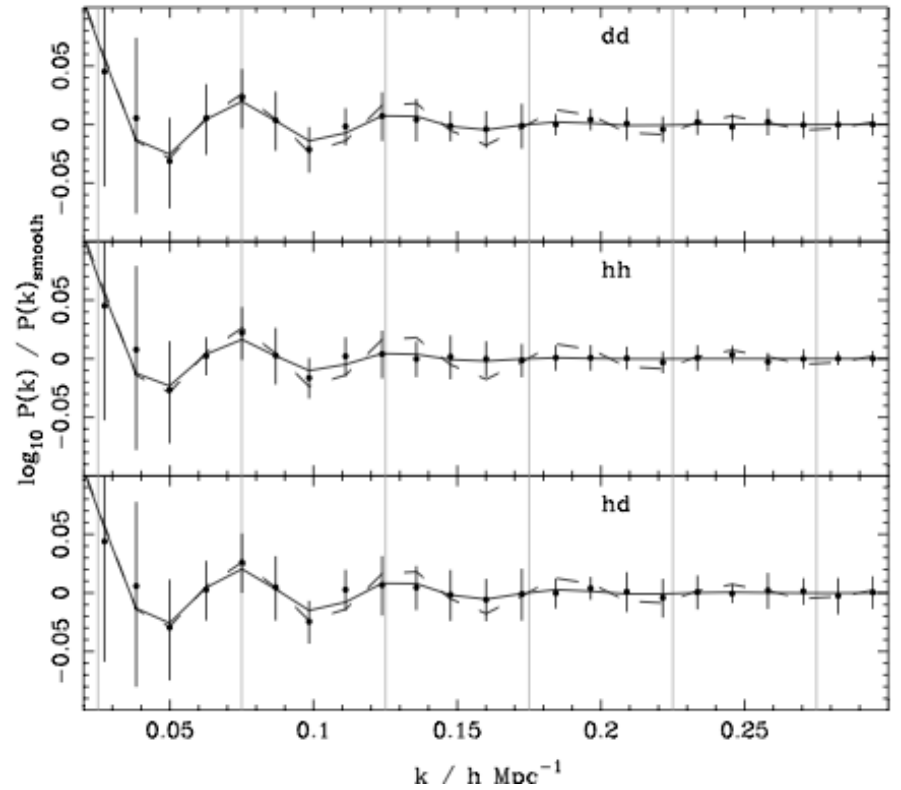
Errors in distance scale of up to 5% claimed

# BAO in simulations



High mass  
halos

Data from simulations of  
Smith, Scoccimarro & Sheth 2006, astro-ph/0609547



low mass halos

Fit with spline  $\times$  BAO model: no evidence  
for distance scale errors



# Summary

- The matter power spectrum generated from galaxy redshift surveys is a useful probe of the cosmological parameters, including those relevant to the dark energy
- However, there are many systematic sources of error that have to be carefully treated, including:
  - convolution with the window function
  - correct treatment of the bias
  - redshift space distortions, etc
- In the future, Baryon Acoustic Oscillations may work very well as a systematic free measurement of the angular diameter distance

## Answer

- The answer to my question is (a) Sean Connery
- Although I will also accept (g) Daniel Craig