



The stellar and dark matter distributions in early-type galaxies measured by weak and strong gravitational lensing

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Introduction

Cold Dark Matter (CDM)

- interactions other than gravity ✗
- collisionless damping ✗



{ large-scale structure ☒
small-scale observations ☐

Small-Scale Challenges

e.g. cusp-core problem

In the central region of the halo,

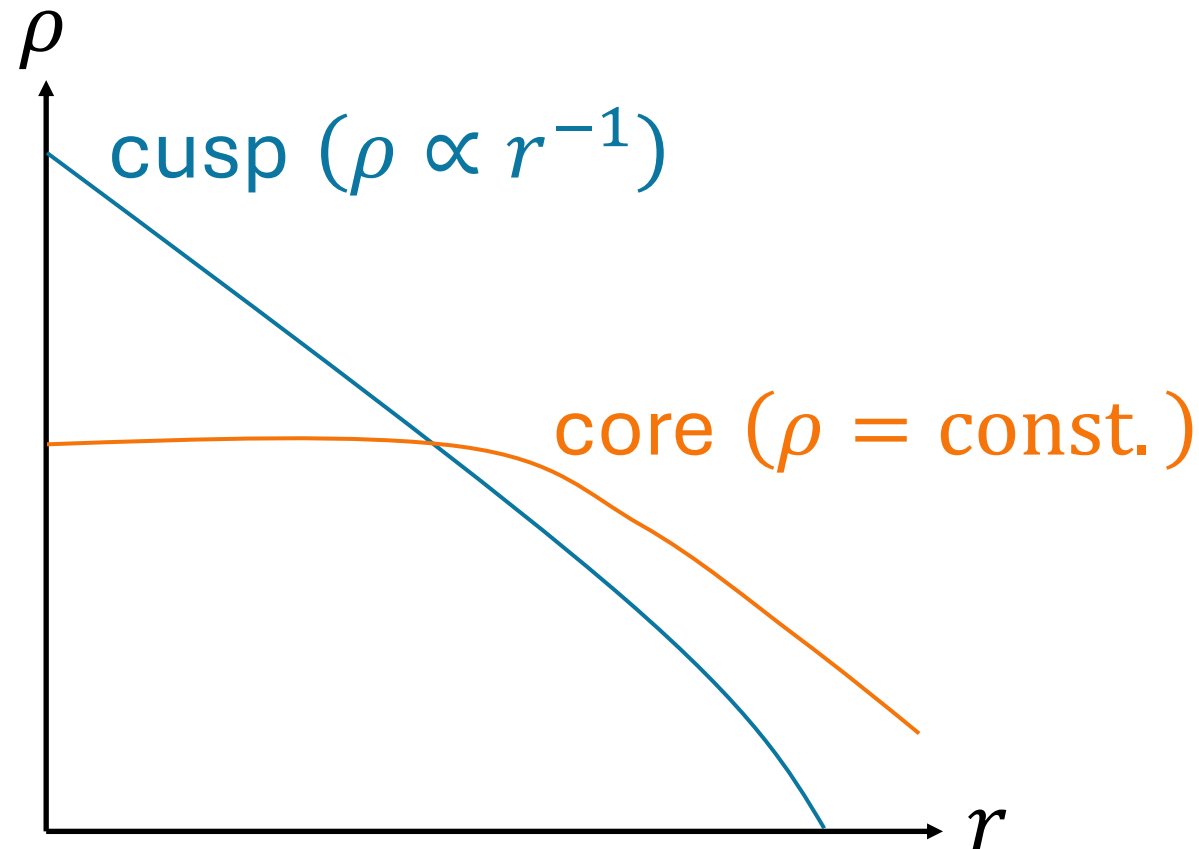
- **CDM**

Navarro-Frenk-White (NFW)

$$\rho(r) = \frac{\rho_s}{\frac{r}{r_s} \left(1 + \frac{r}{r_s}\right)^2}$$

- **some observations**

e.g. rotation curves of
dwarf galaxies



- **Previous researches**

velocity dispersion (Cappellari et al., 2012)

strong gravitational lensing (Treu, 2010 ; Oguri et al., 2014)

➡ the central density profiles of early-type galaxies

- **Advances in observational techniques**

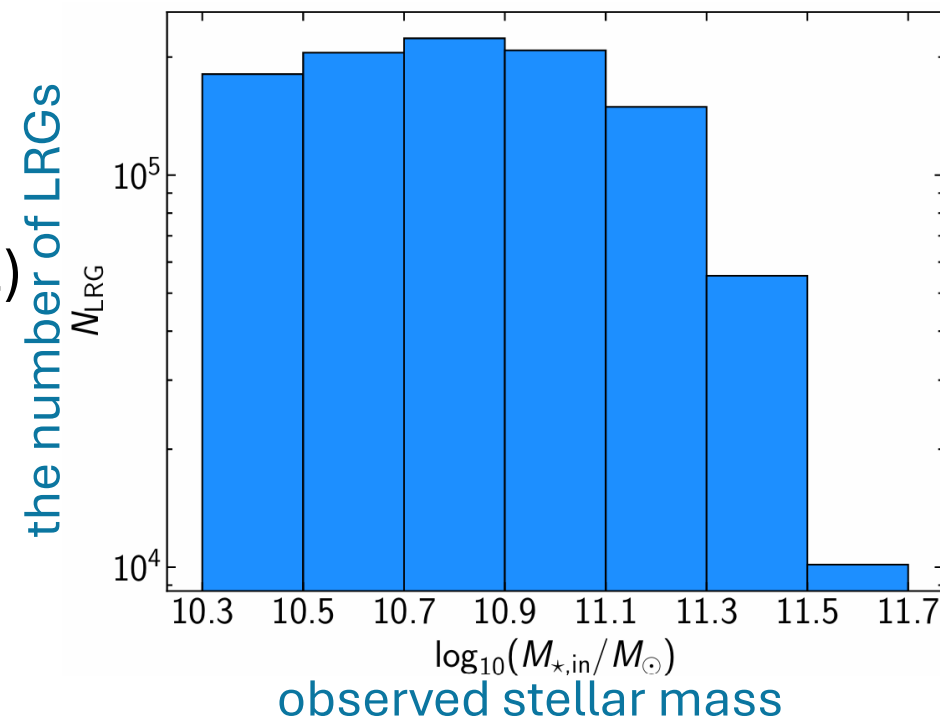
➡ possibility of probing central density distributions of galaxies through weak gravitational lensing

Weak Lensing Analysis

Data

Hyper Suprime-Cam Subaru Strategic Program (HSC-SSP)

- source galaxy
 - public three-year shape galaxy catalog (Li et al., 2022)
 - 36 million galaxies
- lens galaxy
 - final-year photometric Luminous Red Galaxies sample (Oguri et al., 2026)
 - $0.4 < z < 0.6$



Method

measured tangential shear of source galaxy γ_t

→ differential surface mass density of lens galaxy

$$\Delta\Sigma(r) = \gamma_t \times \Sigma_{\text{cr}}$$

Σ_{cr} : critical surface mass density

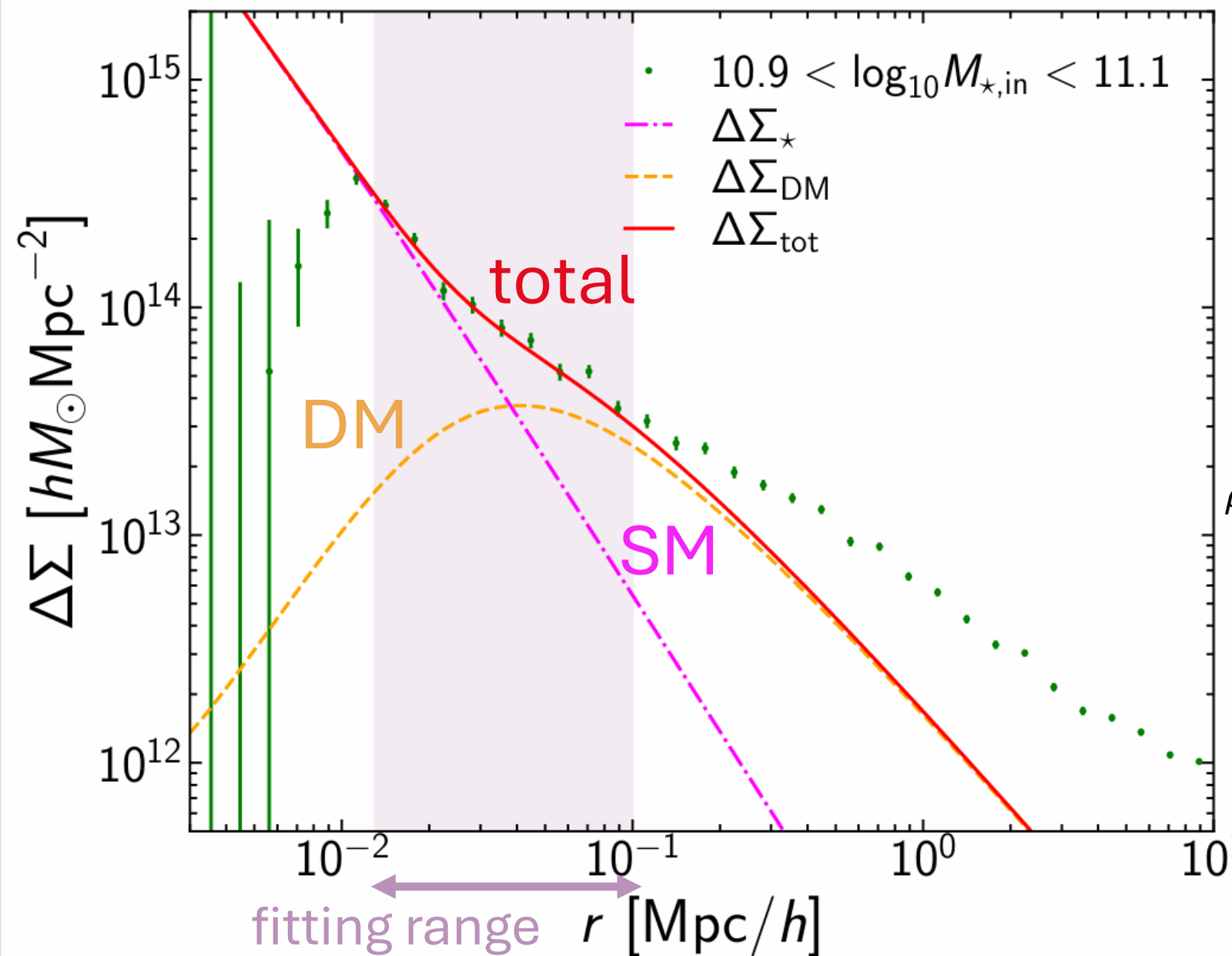
$$= \bar{\Sigma}(< r) - \Sigma(r)$$

$\Sigma(r) = \int_{-\infty}^{\infty} \rho(\mathbf{r}) dZ$: surface mass density

Individual lensing signal is too small

→ stacking a large number of lens galaxies

Inner Profile Fitting



- Model stellar matter (SM)

➡ Hernquist

$$\rho_{\text{SM}}(r) = \frac{M_{\star} a}{2\pi r} \frac{1}{(r + a)^3}$$

dark matter (DM)

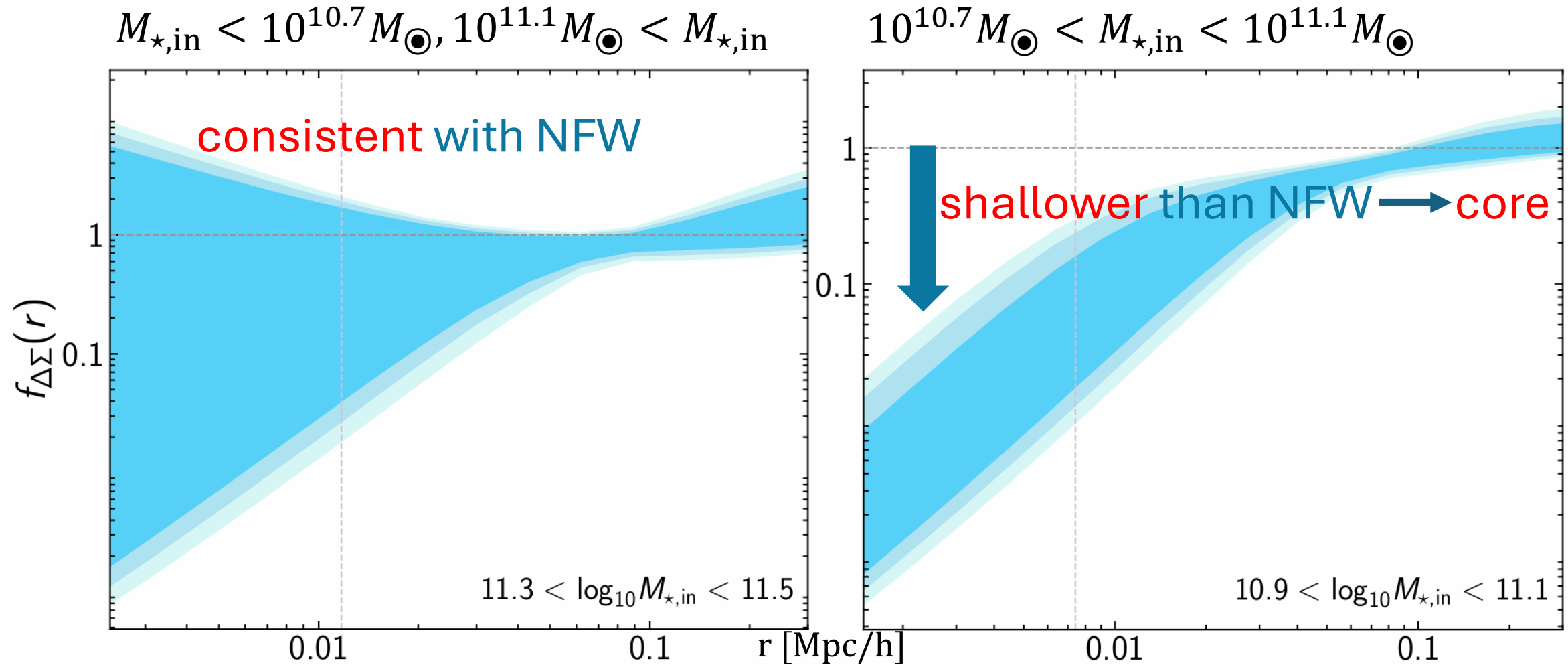
➡ cored power-law

$$\rho_{\text{DM}}(r) = M_{\star} \frac{3 + \gamma}{2\pi^{\frac{3}{2}} r_e^3} \frac{\Gamma\left(-\frac{\gamma}{2}\right)}{\Gamma\left(-\frac{1 + \gamma}{2}\right)} A \left(\frac{r^2 + r_c^2}{r_e^2}\right)^{\frac{\gamma}{2}}$$

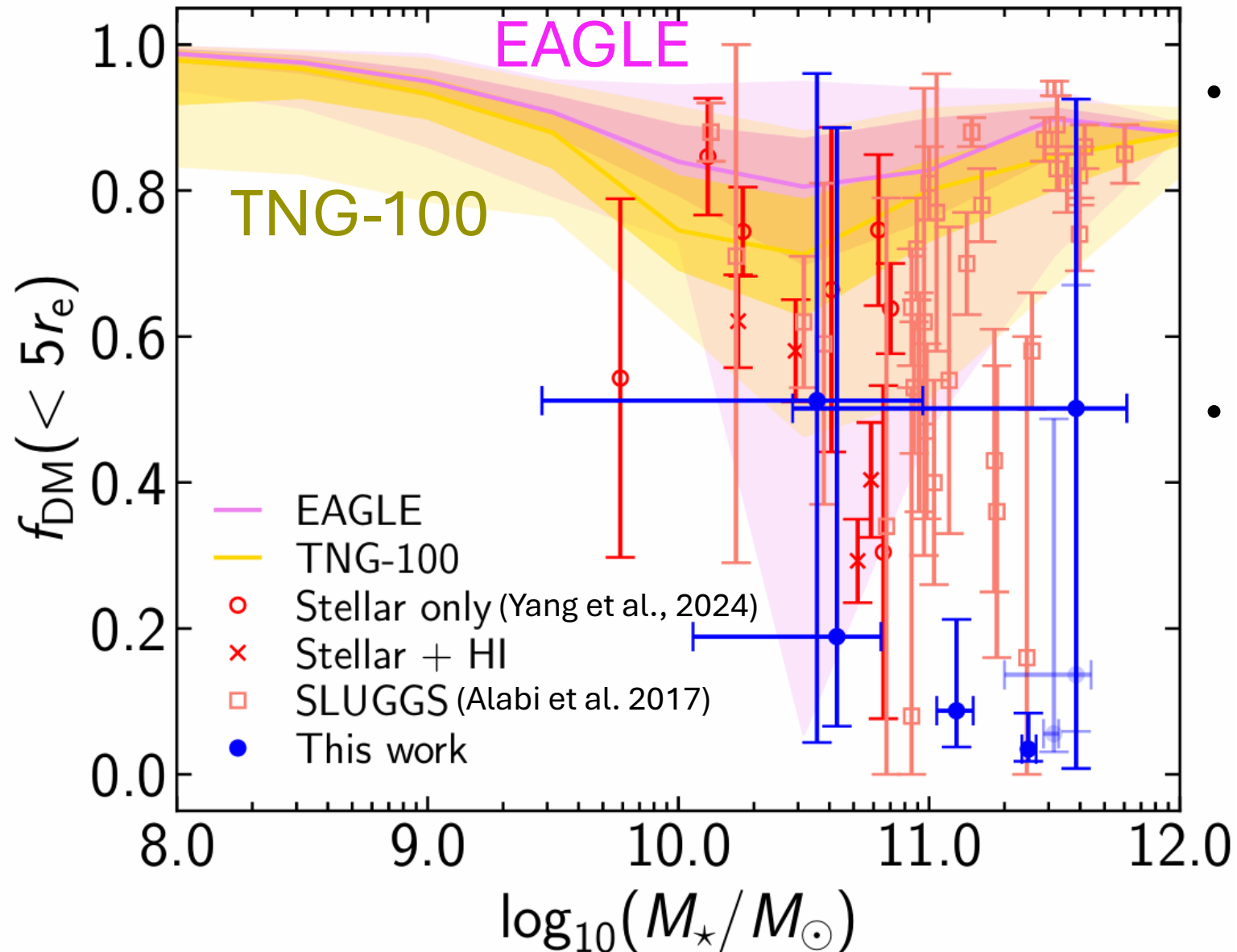
- investigating from observation data **without** assuming a specific dark matter model

Comparison with NFW

- $f_{\Delta\Sigma}(r) = \frac{\Delta\Sigma_{\text{DM}}(r)}{\Delta\Sigma_{\text{NFW}}(r)}$ ← obtained from the outer fitting



Comparison with simulations



- dark matter fraction

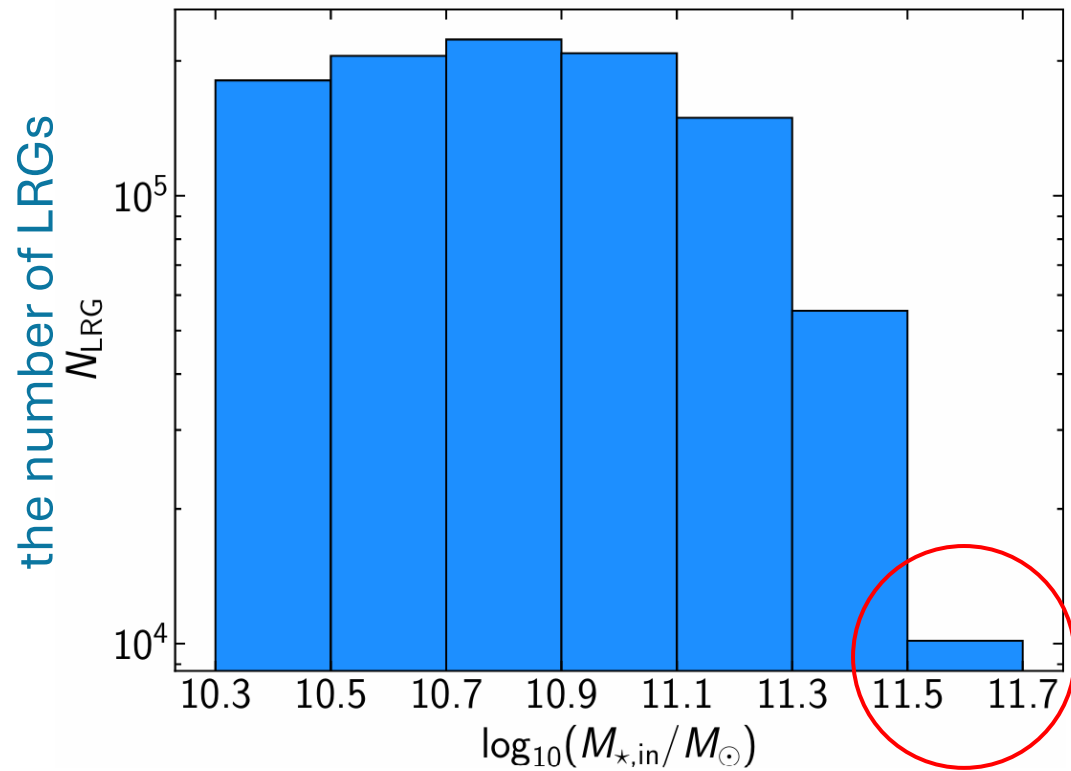
$$f_{\text{DM}}(< 5r_e) = \frac{M_{\text{DM}}(r < 5r_e)}{M_\star(r < 5r_e) + M_{\text{DM}}(r < 5r_e)}$$

(r_e : the half-light radius)

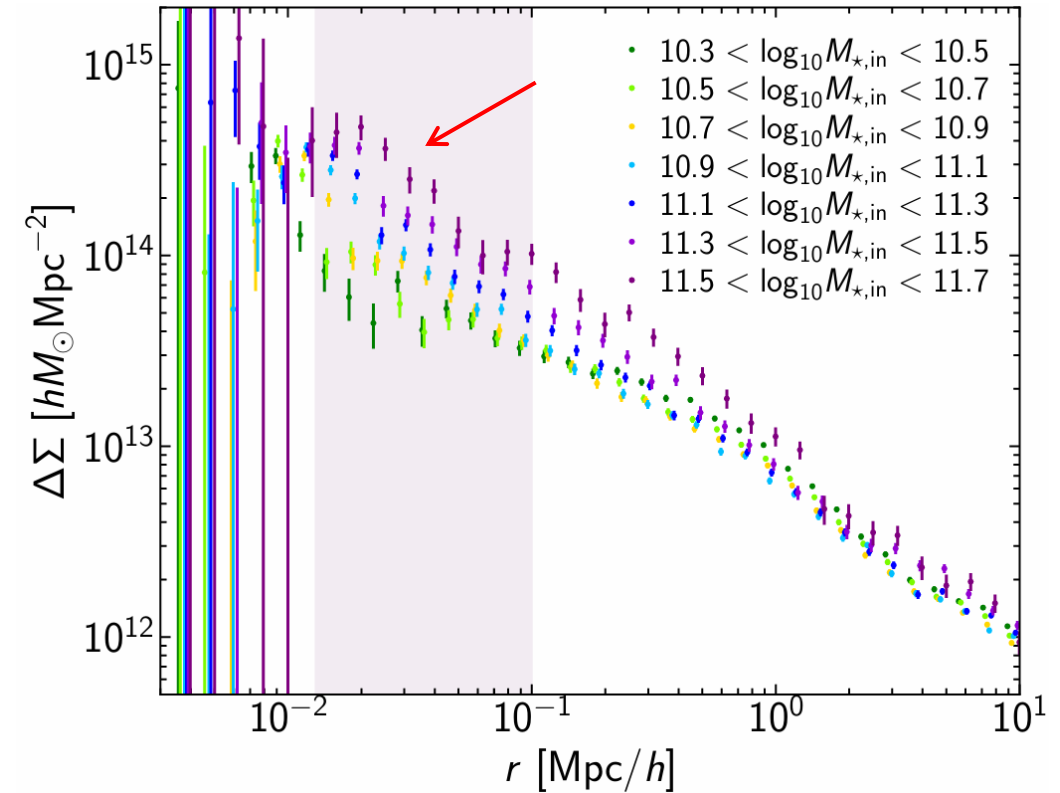
- For $10^{10.7} M_\odot < M_{\star, \text{in}} < 10^{11.1} M_\odot$,
lower than the values predicted from
hydrodynamical simulations

➡ actual feedback effect
may be **stronger**

Limitation of Weak Lensing Analysis



For the highest stellar mass bin,
small number of lens galaxies



large statistical uncertainty
(intrinsic shape noise)

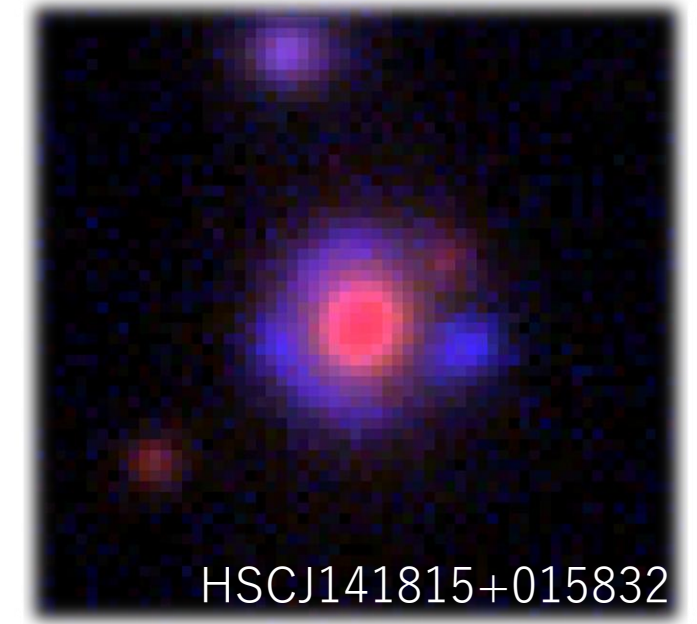
combining weak and **strong** lensing
to obtain **tighter constraints** in the highest stellar mass bin

Strong Lensing Analysis

Data

14 strong lens systems with spec-z from

- Survey of Gravitationally-lensed Objects in HSC Imaging (SuGOHI; Sonnenfeld et al. 2019; Gawade et al. 2025)
- Strong Lensing Legacy Survey (SL2S; Gavazzi et al. 2012; Tan et al. 2024)
- BOSS Emission-Line Lens Survey (BELLS; Brownstein et al. 2011; Tan et al. 2024)



Method

- Einstein radius θ_{Ein}
- spec-z of lens and source galaxy

➡ $M_{2D}(< \theta_{\text{Ein}}) = \pi D_{\text{ol}}^2 \theta_{\text{Ein}}^2 \Sigma_{\text{cr}}$

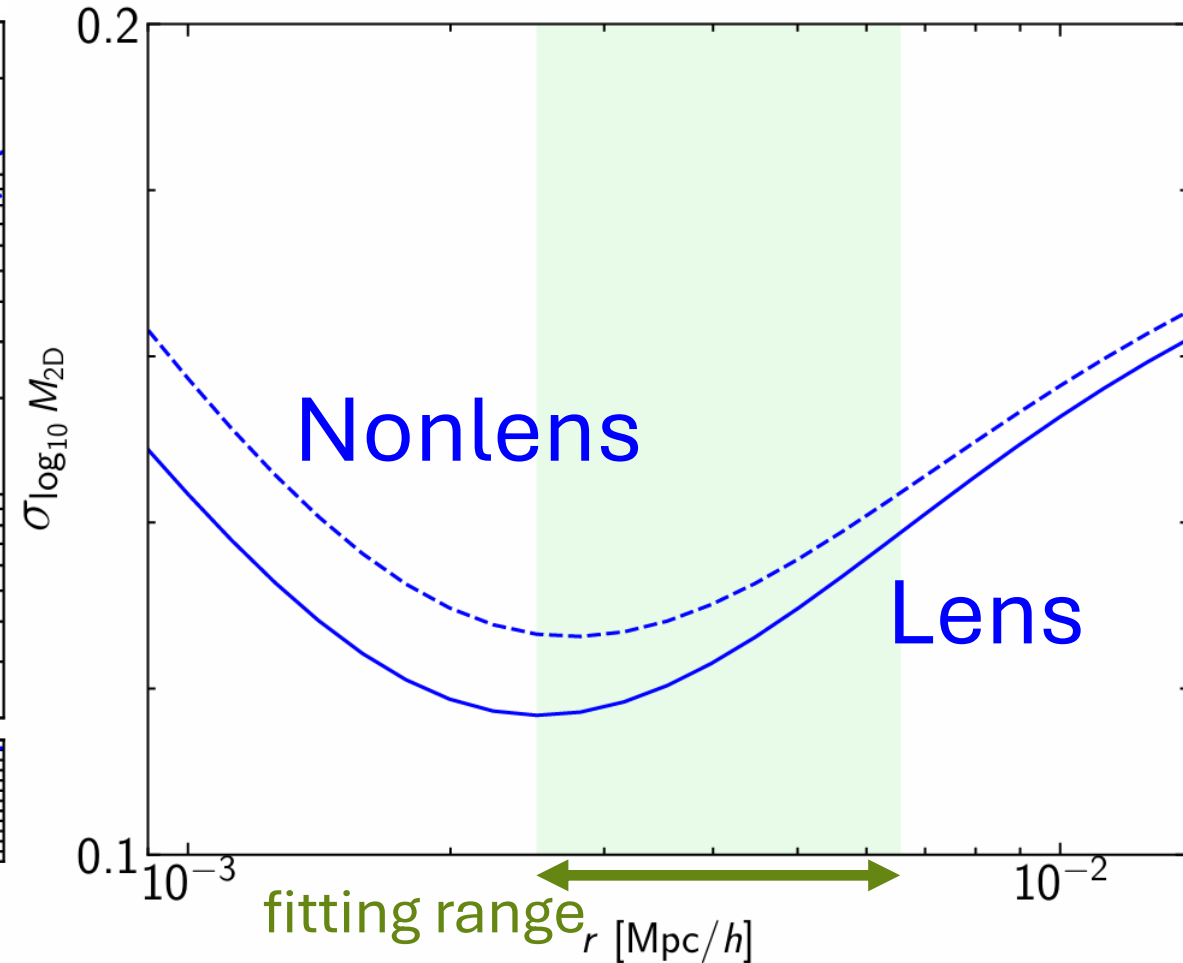
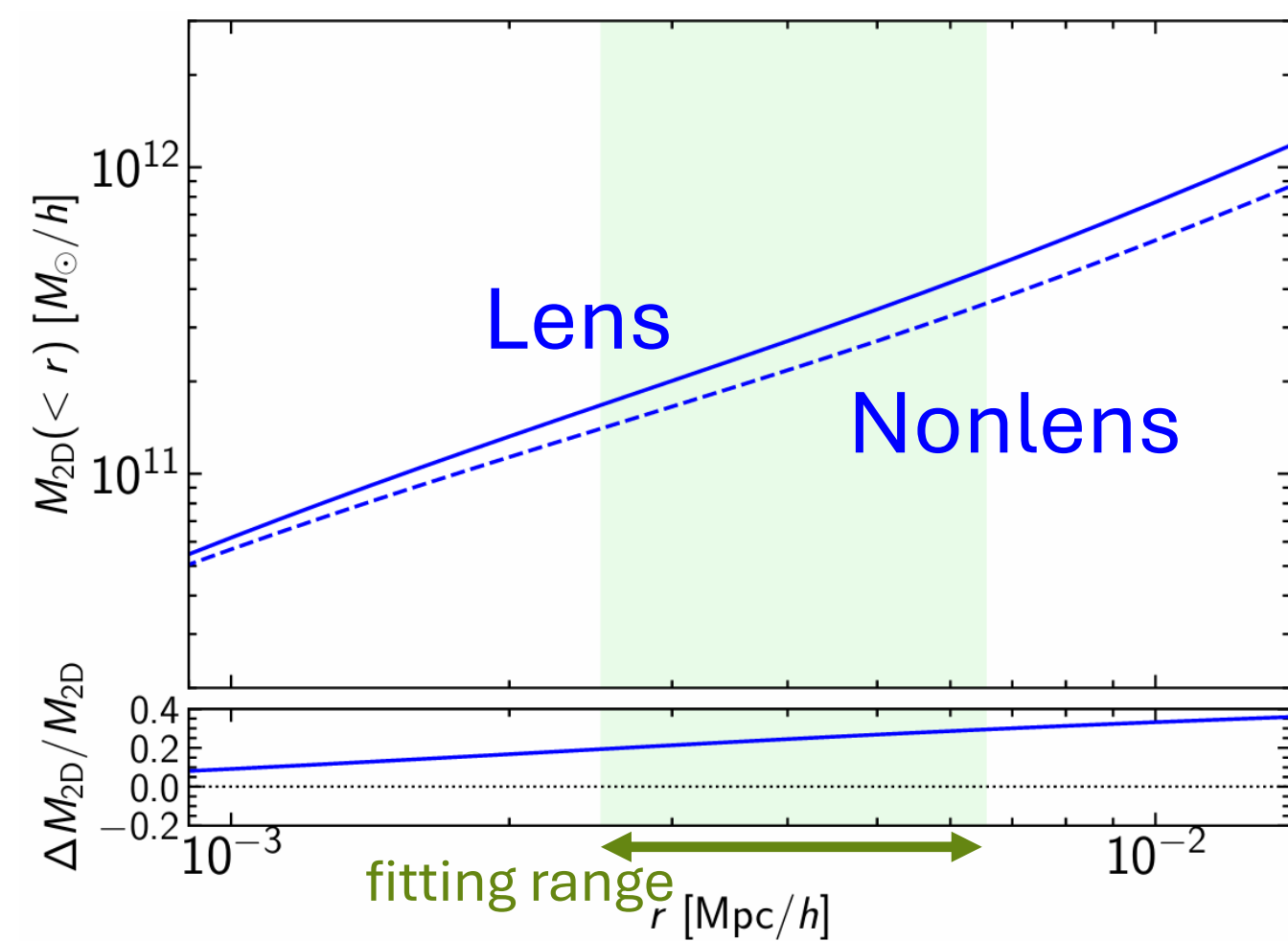
D_{ol} : angular diameter distance between the observer and the lens galaxy

Σ_{cr} : critical surface mass density

applying to multiple lens galaxies

➡ average $M_{2D}(< r)$

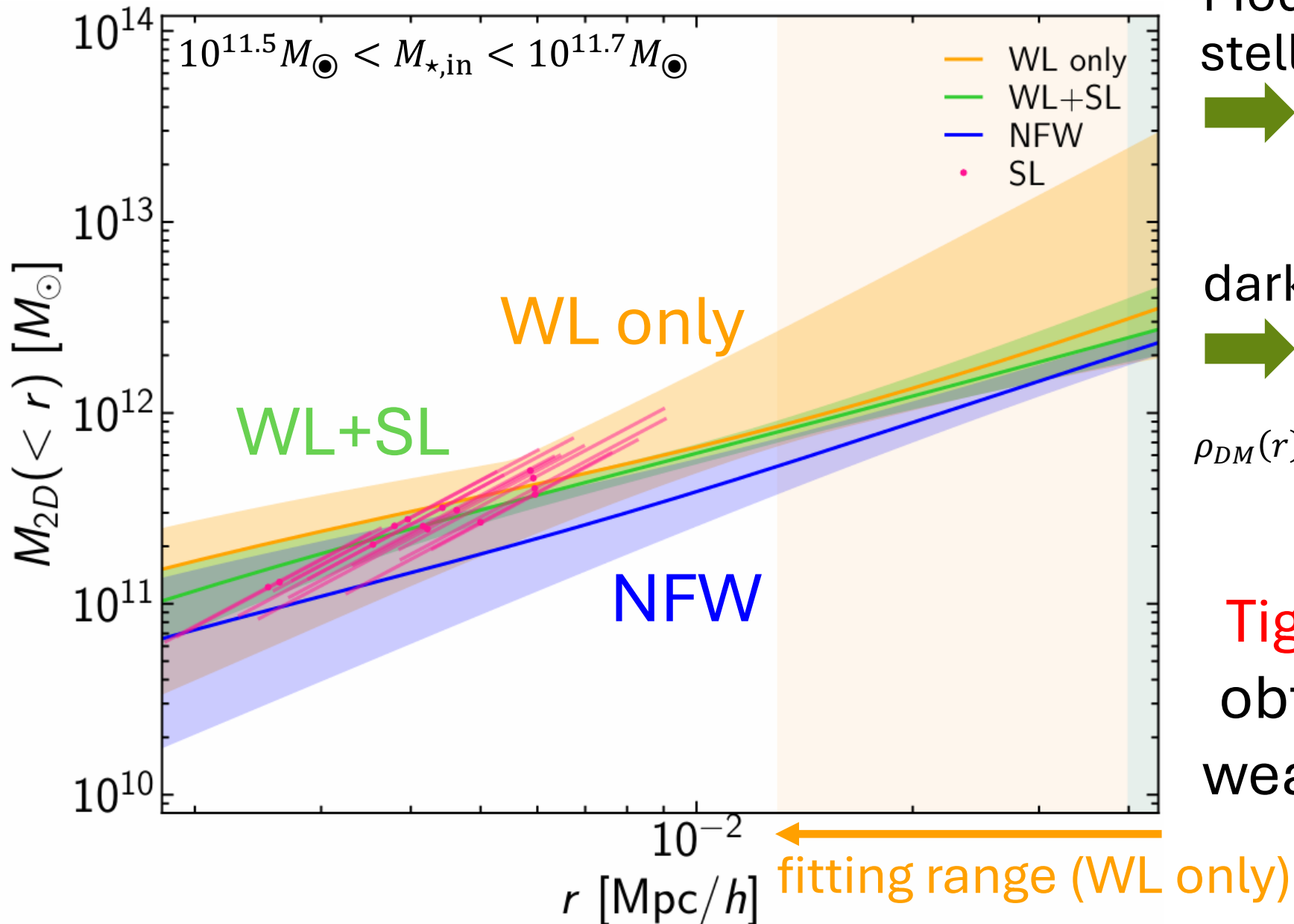
Strong-lensing selection bias and intrinsic scatter



- correcting for strong-lensing selection bias using a mock catalog (Abe et al. 2025)

- intrinsic scatter from mock $\sigma_{\log_{10} M_{2D}} \sim 0.14$

Inner Profile Fitting (WL+SL)



• Model

stellar matter (SM)

➡ Hernquist

$$\rho_{\text{SM}}(r) = \frac{M_{\star} a}{2\pi r} \frac{1}{(r+a)^3}$$

dark matter (DM)

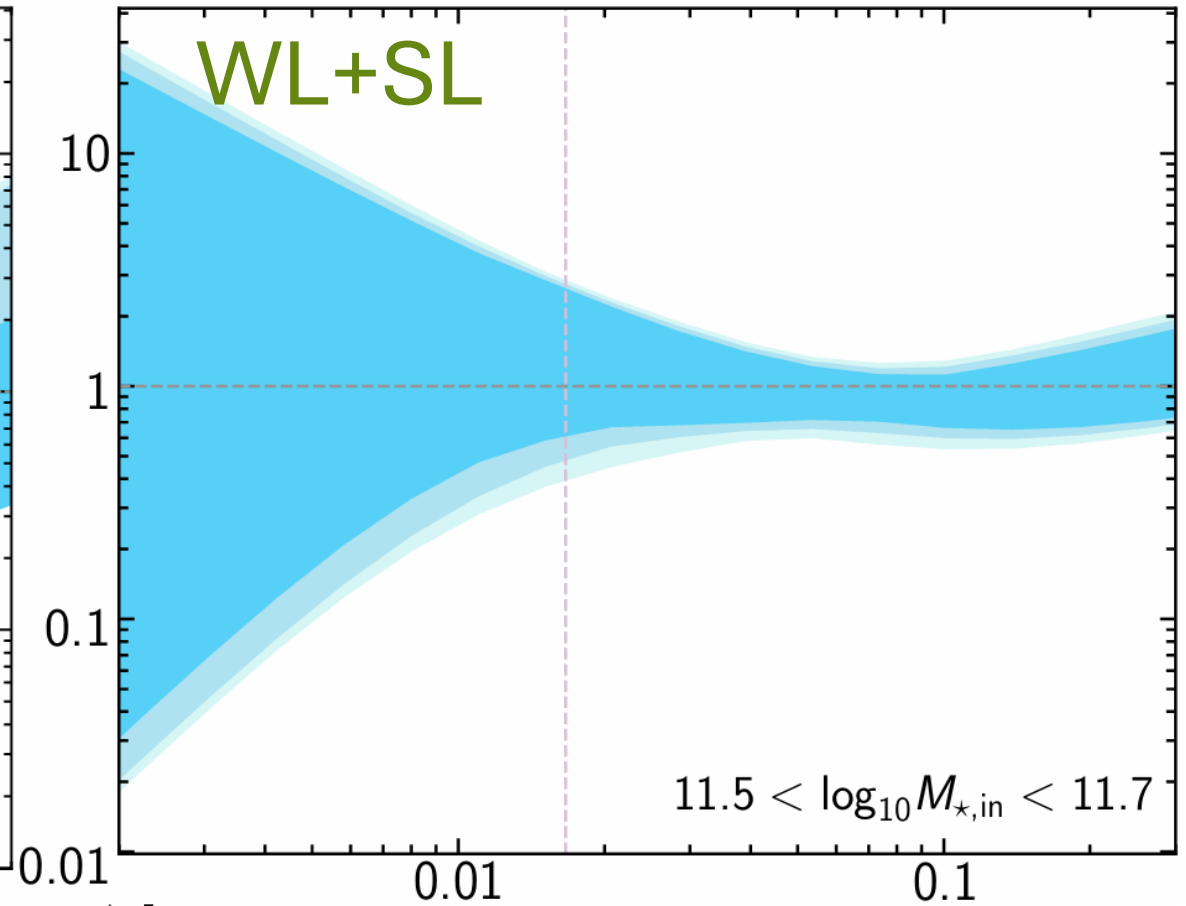
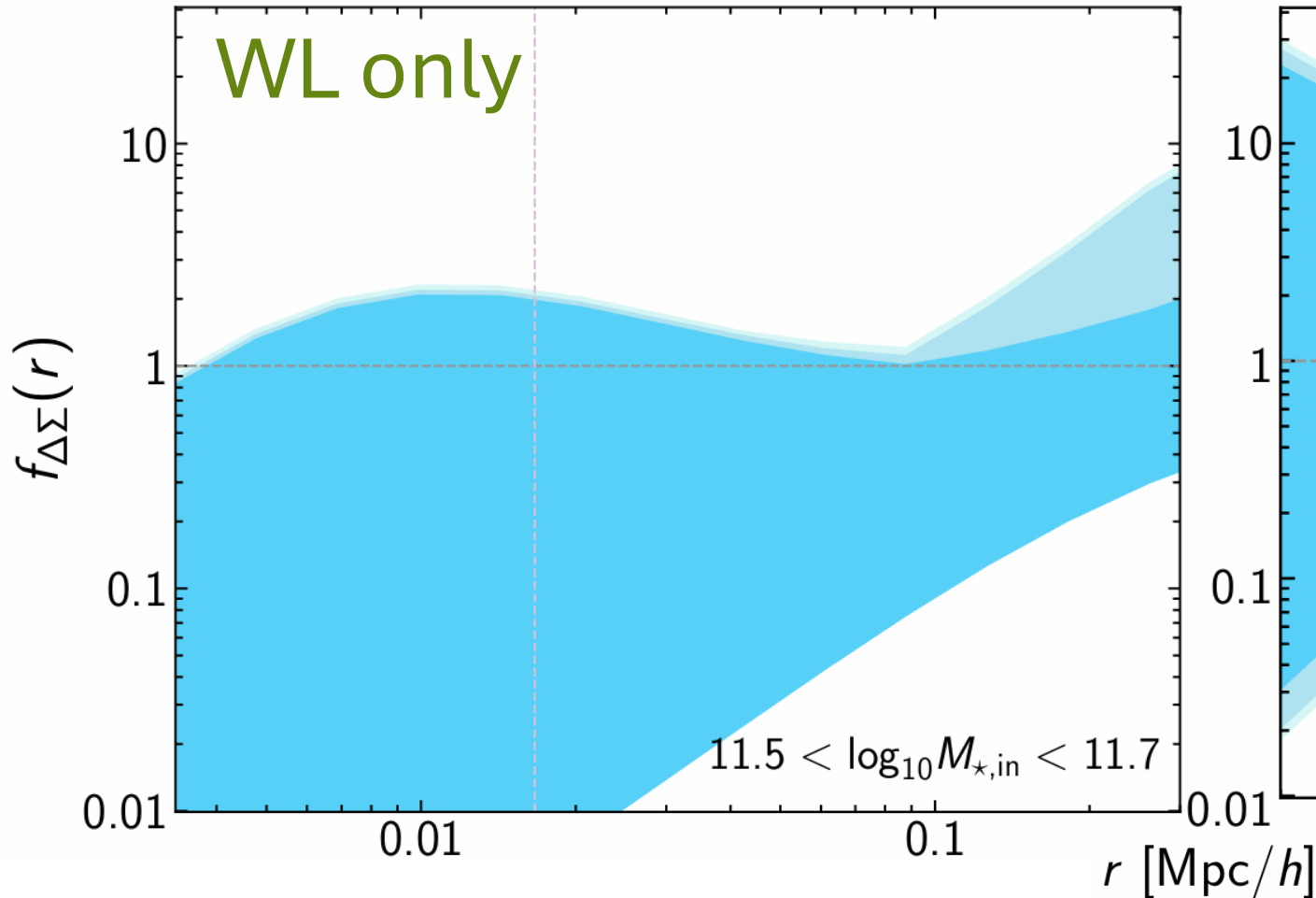
➡ cored power-law

$$\rho_{\text{DM}}(r) = M_{\star} \frac{3+\gamma}{2\pi^{\frac{3}{2}} r_e^3} \frac{\Gamma(-\frac{\gamma}{2})}{\Gamma(-\frac{1+\gamma}{2})} A \left(\frac{r^2 + r_c^2}{r_e^2} \right)^{\frac{\gamma}{2}}$$

Tighter constraints are obtained by combining weak and strong lensing

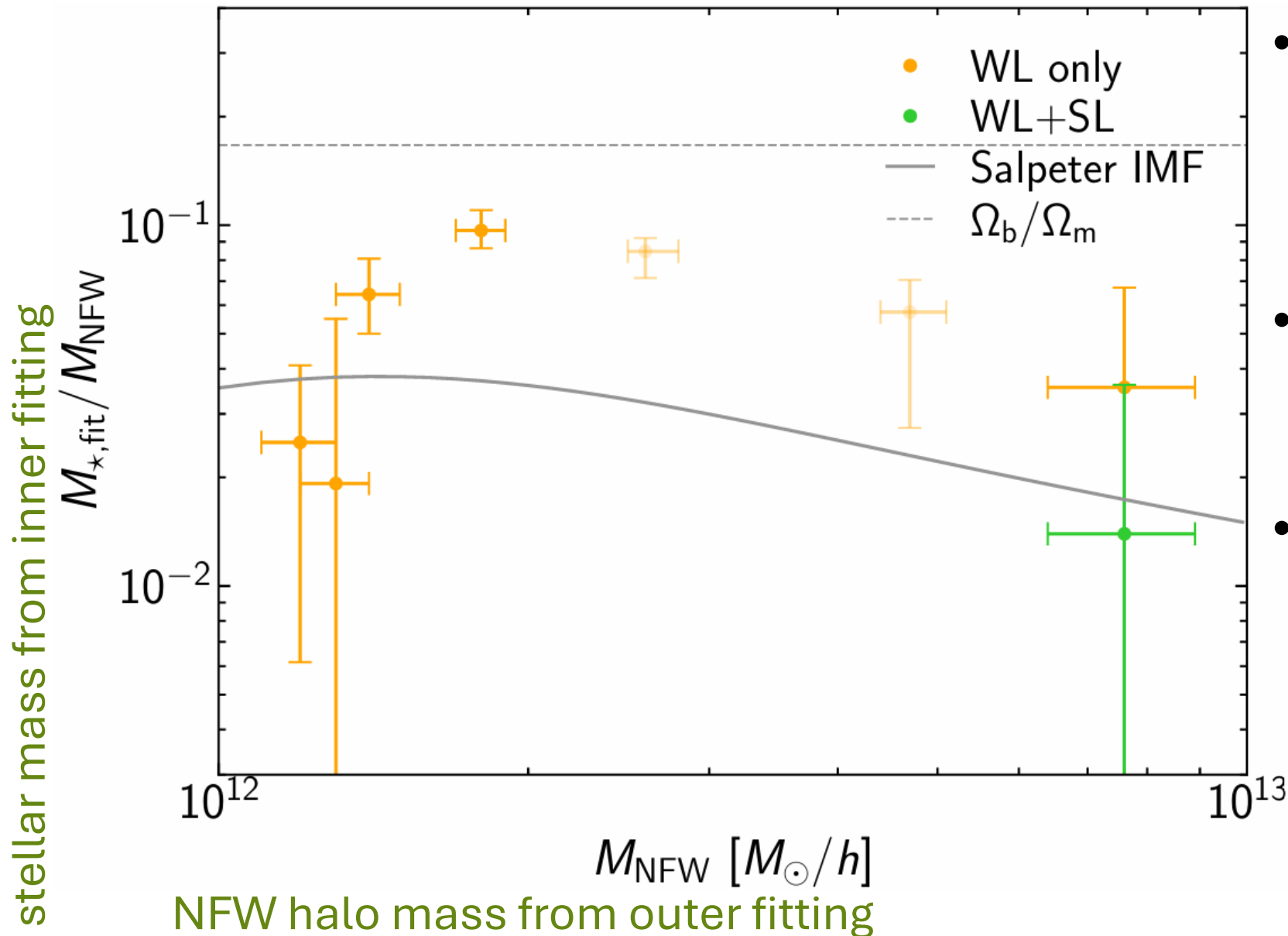
Comparison with NFW (WL+SL)

- $f_{\Delta\Sigma}(r) = \frac{\Delta\Sigma_{\text{DM}}(r)}{\Delta\Sigma_{\text{NFW}}(r)}$ ← obtained from the outer fitting



More tightly consistent with NFW

Constraint on Stellar-to-halo Mass Relation (SHMR)



- constraining SHMR **without** relying on $M_{\star}/L$ or IMF assumption
 - For the highest mass bin, consistent w/ Salpeter IMF
 - For lower mass bins, higher $M_{\star}$ than expected from Salpeter IMF
- ➡ possibility of **more bottom-heavy IMF**

Summary

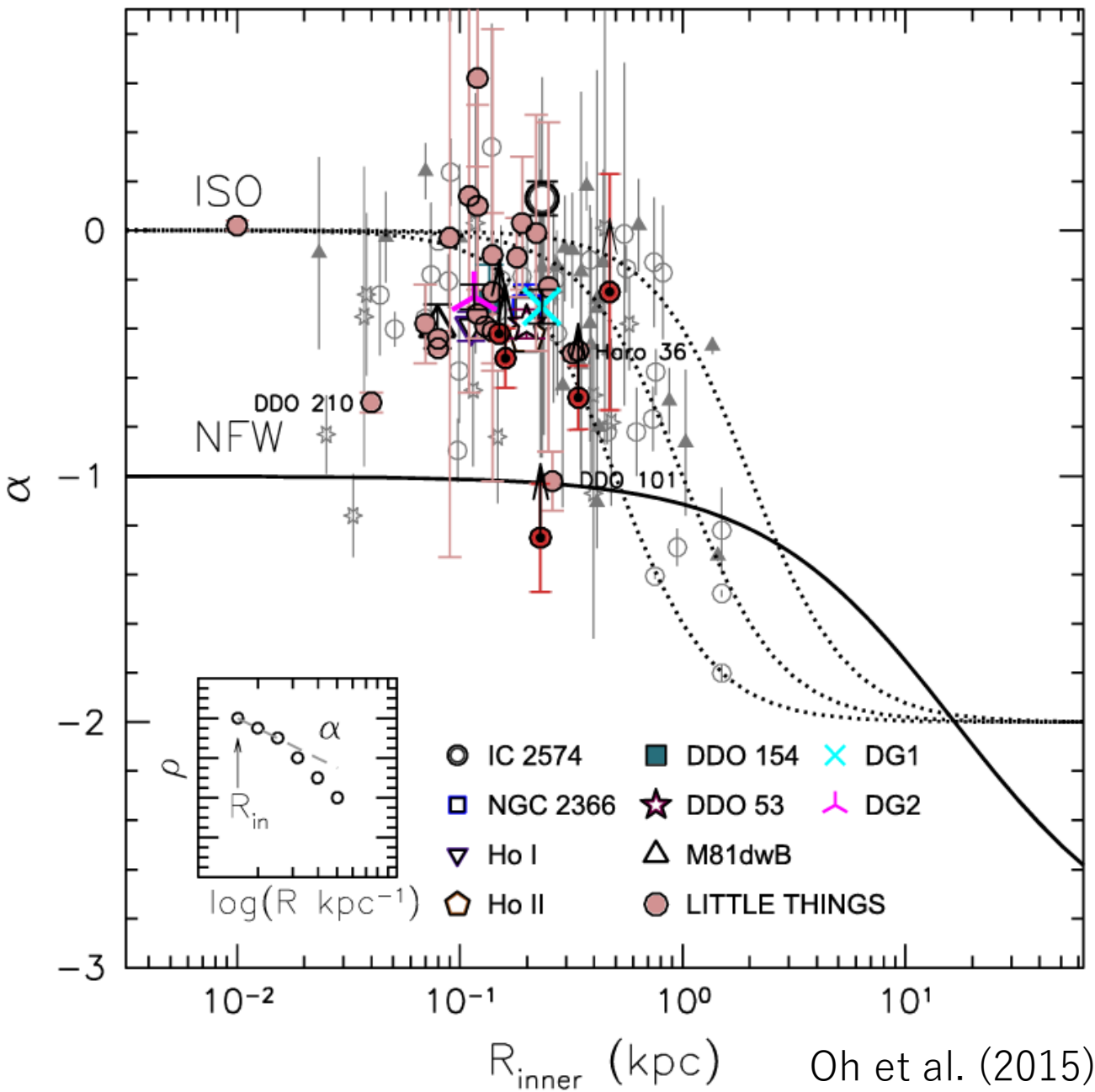
- ✓ We investigate **central dark matter distributions** of early-type galaxies by **combining weak and strong** lensing analysis
- ✓ We provide new constraints on
 - central dark matter profiles
 - **cored** distributions are favored in intermediate mass bins
 - the SHMR
 - the stellar IMF
 - more **bottom-heavy** than Salpeter IMF in intermediate mass bins

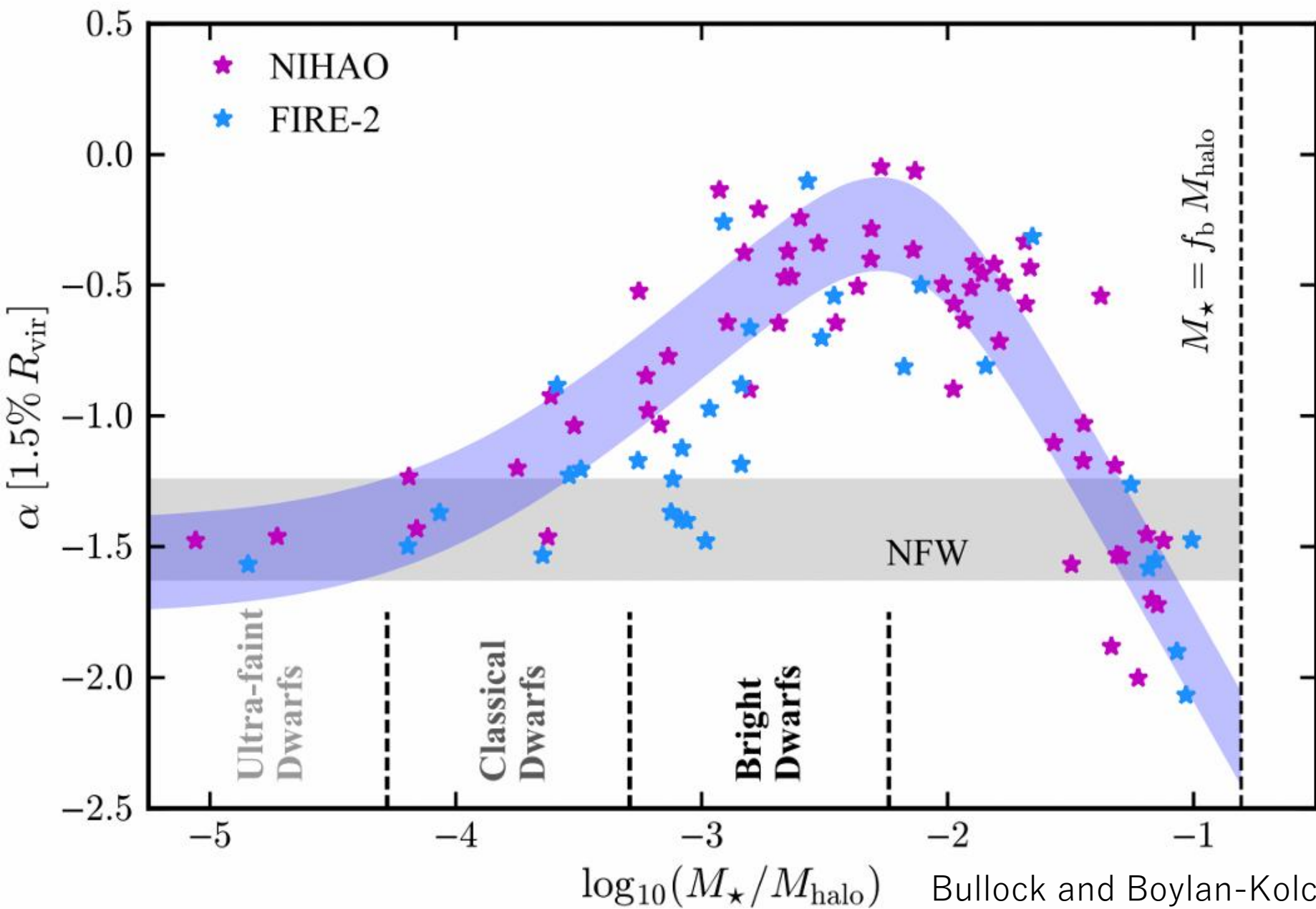
Future Work

- considering **more flexible** dark matter profile model
- investigating **the redshift dependence**
- researching **total mass profile**

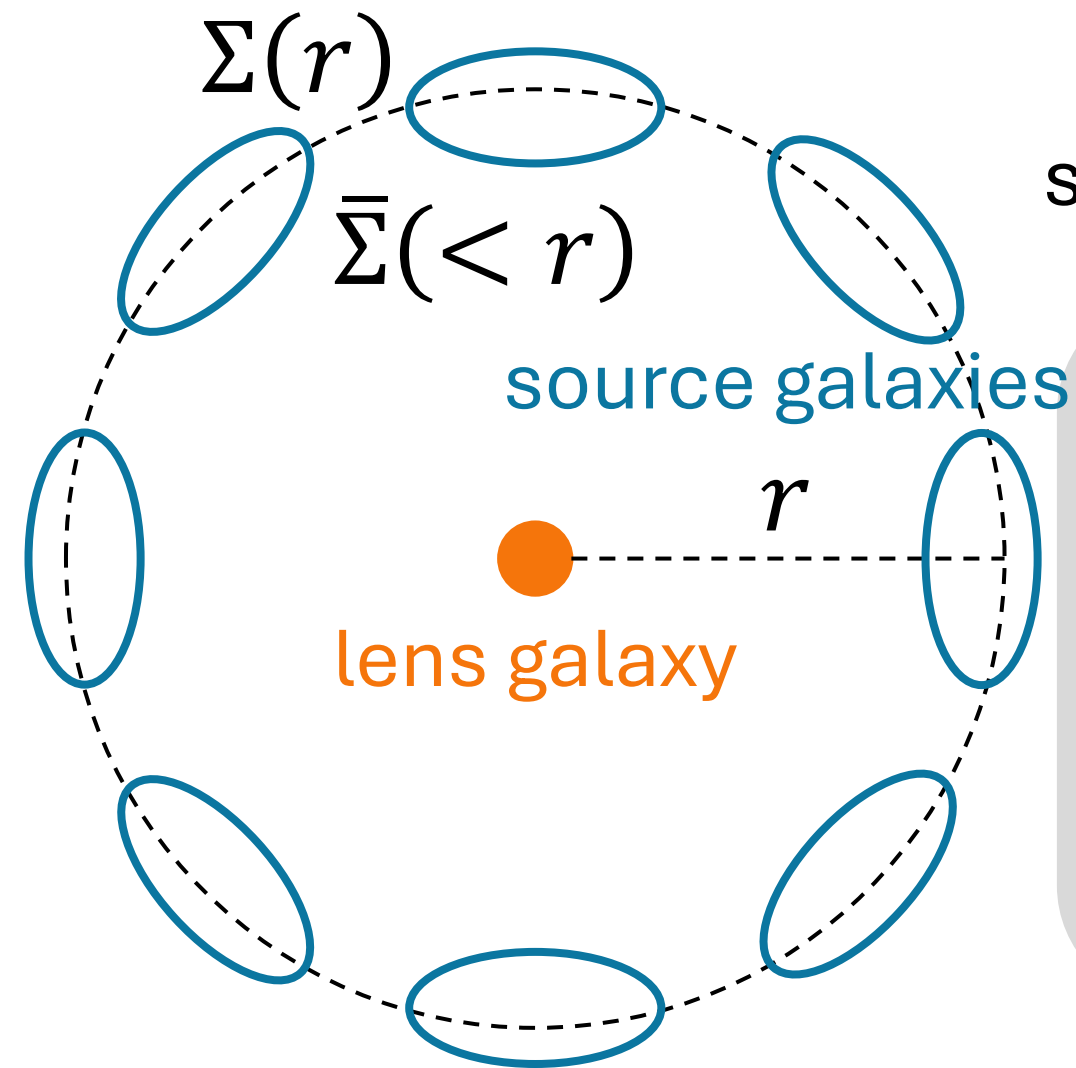


Backup Slides





Weak Gravitational Lensing



surface mass density $\Sigma(r) = \int_{-\infty}^{\infty} \rho(\mathbf{r}) dZ$

measuring tangential shear γ_t



differential surface mass density

$$\Delta\Sigma(r) = \gamma_t \times \Sigma_{\text{cr}}$$

$$= \bar{\Sigma}(< r) - \Sigma(r)$$

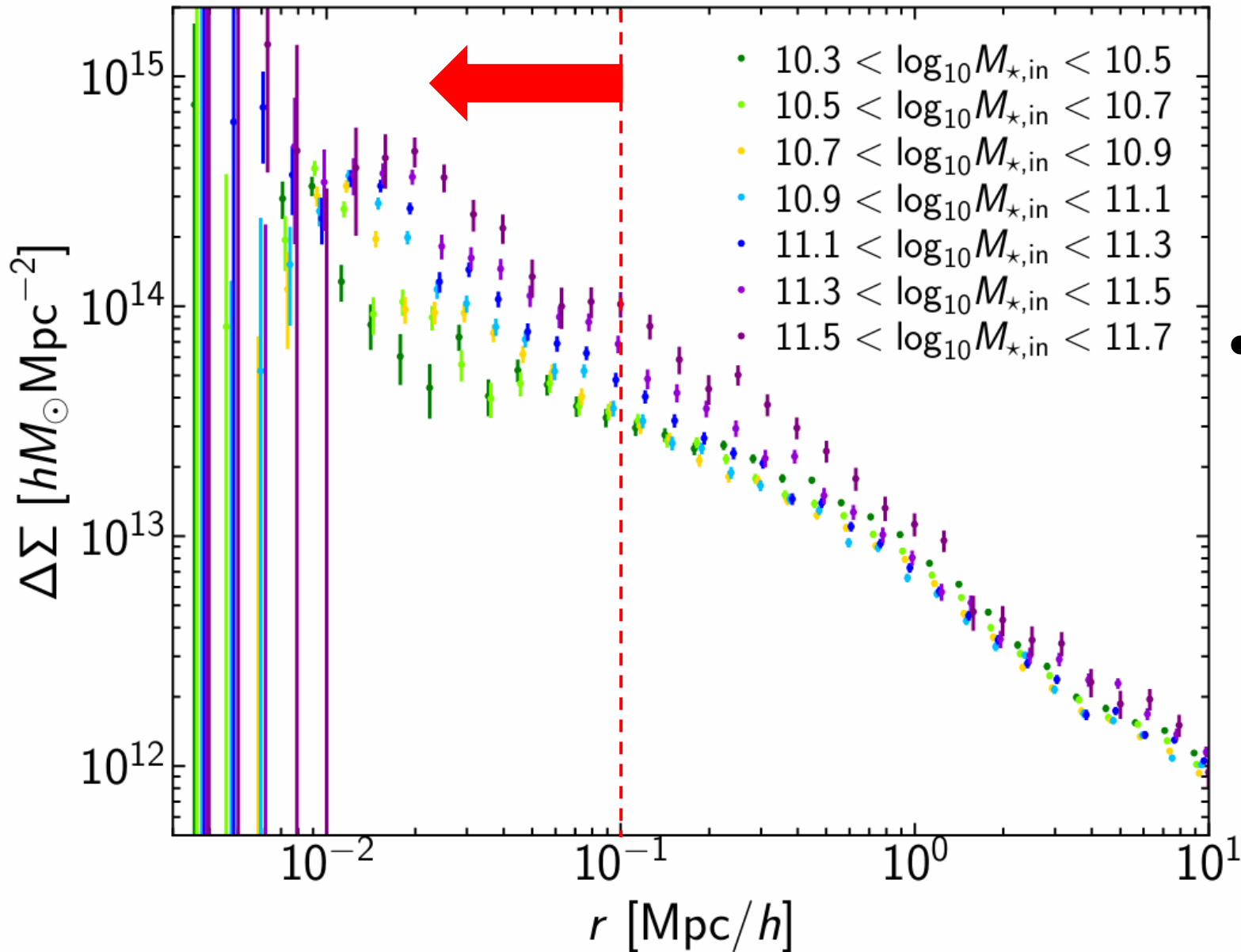
(Σ_{cr} : critical surface mass density)

Individual lensing signal
is too small

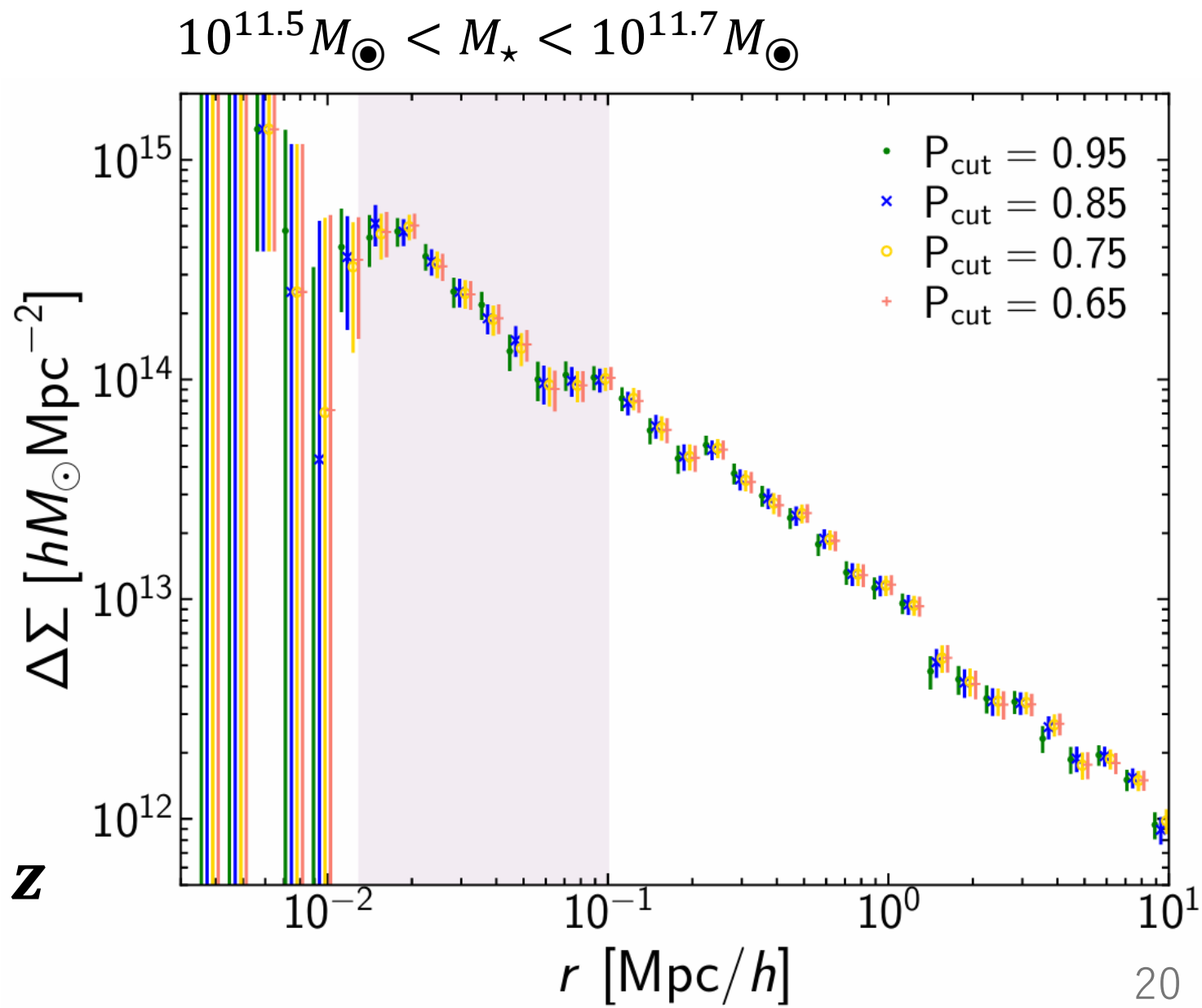
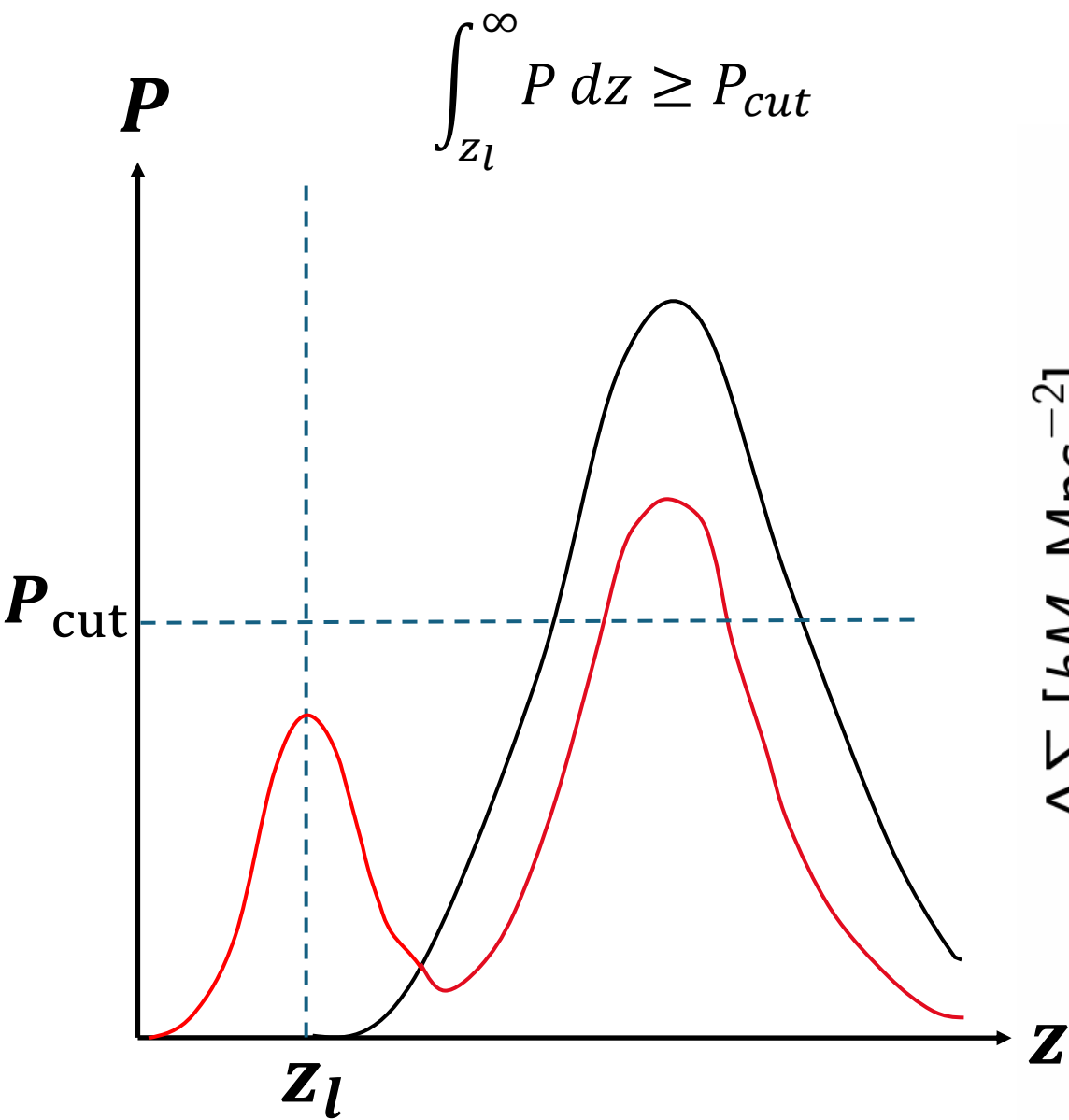


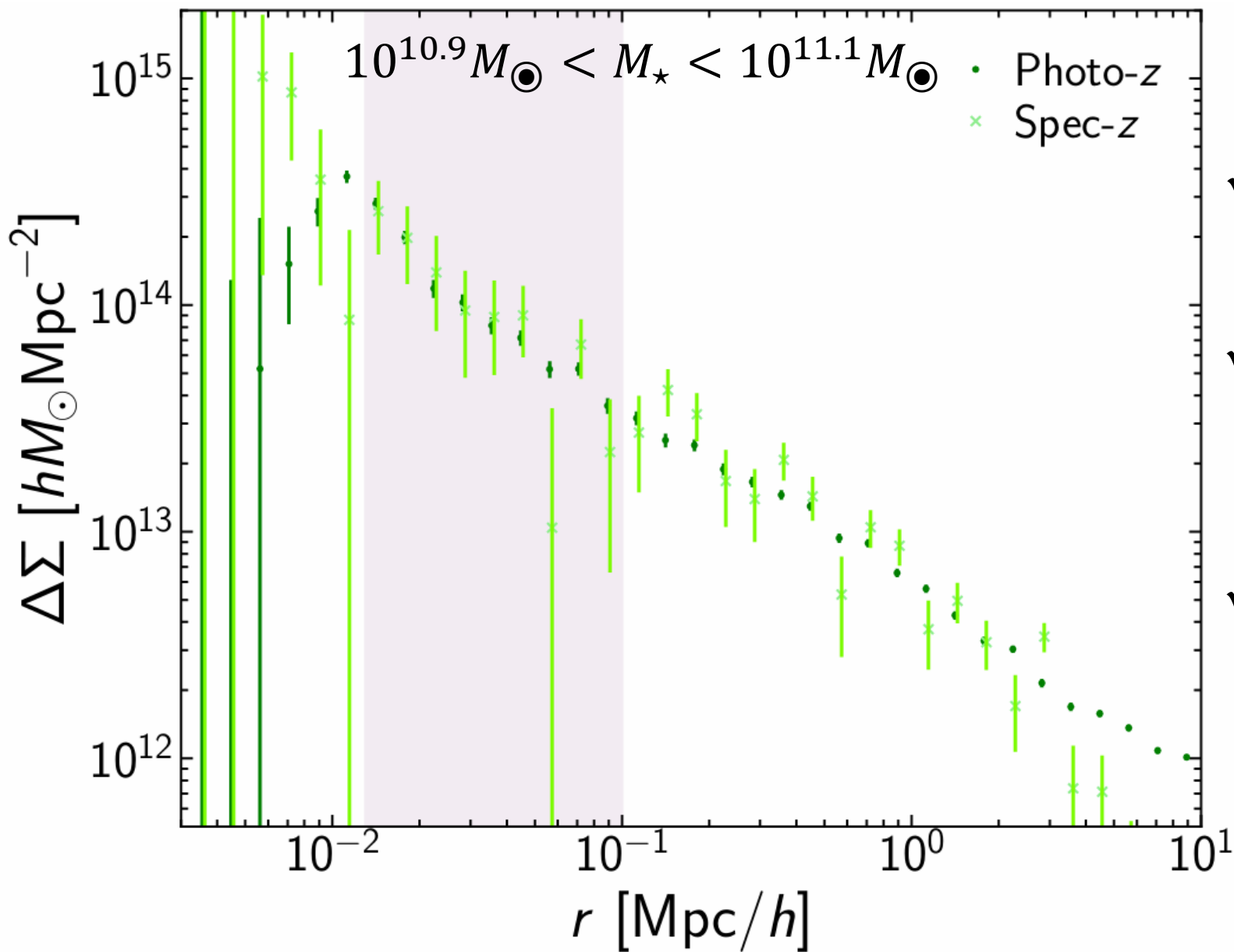
stacking a large number of lens galaxies

Measurement



- we want to know the **central** dark matter distribution

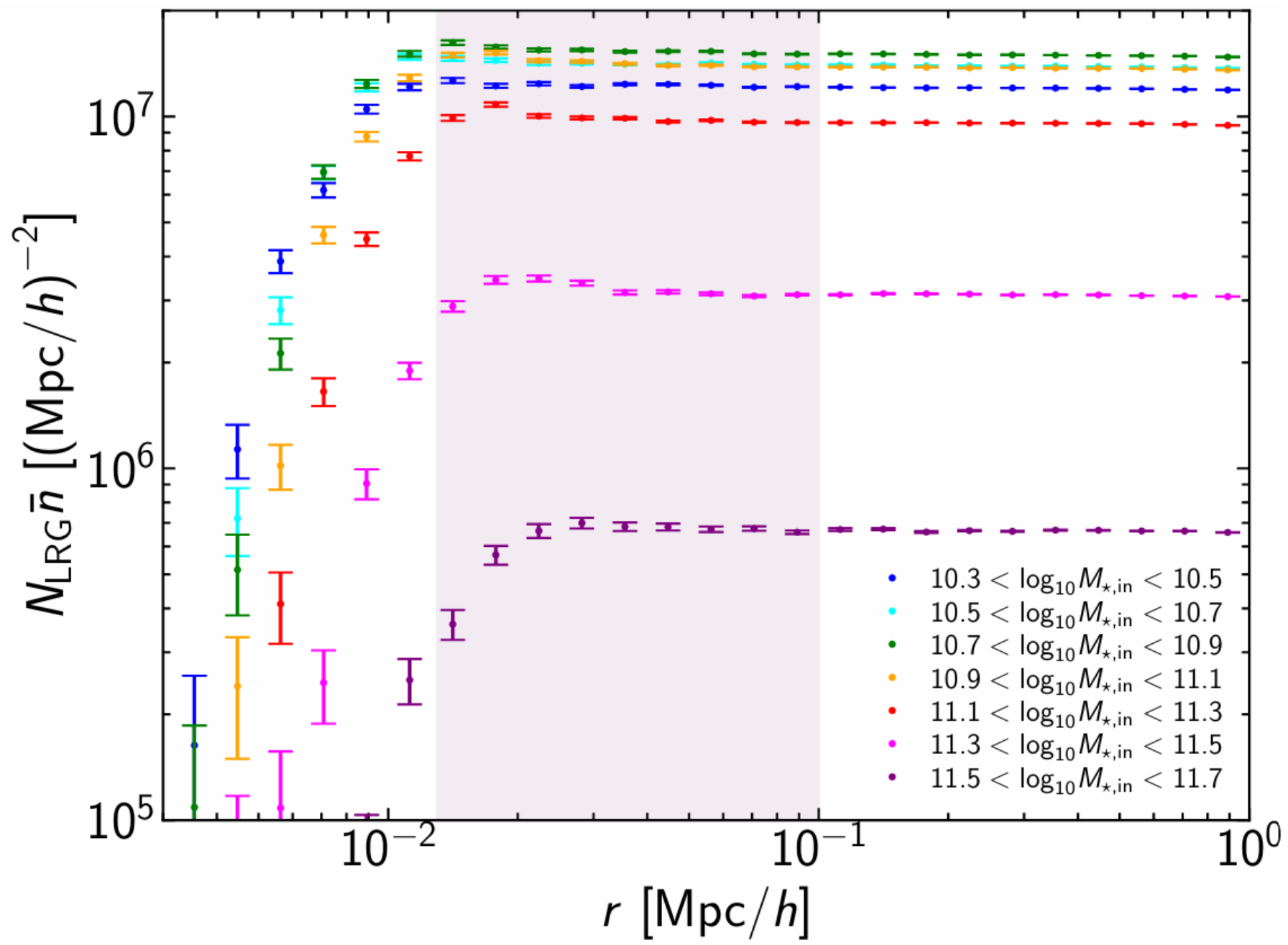




$$\chi^2 = \sum \frac{(\Delta\Sigma_{spec} - \Delta\Sigma_{photo})^2}{\sigma_{spec}^2 + \sigma_{photo}^2}$$

✓ For $10^{11.3}M_{\odot} < M_{\star} < 10^{11.5}M_{\odot}$,
 χ^2 falls outside the 95%
 confidence interval ($2.7 \lesssim \chi^2 \lesssim 19.0$)

✓ For the other mass bins,
 χ^2 is within the 95% confidence
 interval



- ✓ stellar matter (SM) component  Hernquist (parameters M_* , r_e)
- ✓ dark matter (DM) component  **cored power-law**

$$\rho_{DM}(r) = M_* \frac{3 + \gamma}{2\pi^{\frac{3}{2}} r_e^3} \frac{\Gamma\left(-\frac{\gamma}{2}\right)}{\Gamma\left(-\frac{1 + \gamma}{2}\right)} A \left(\frac{r^2 + r_c^2}{r_e^2} \right)^{\frac{\gamma}{2}}$$

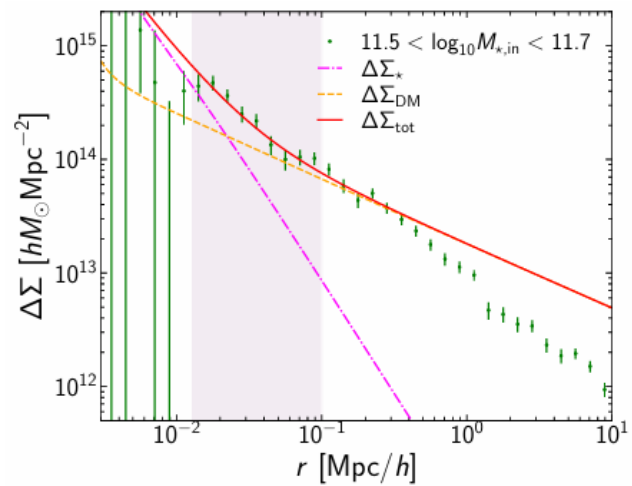
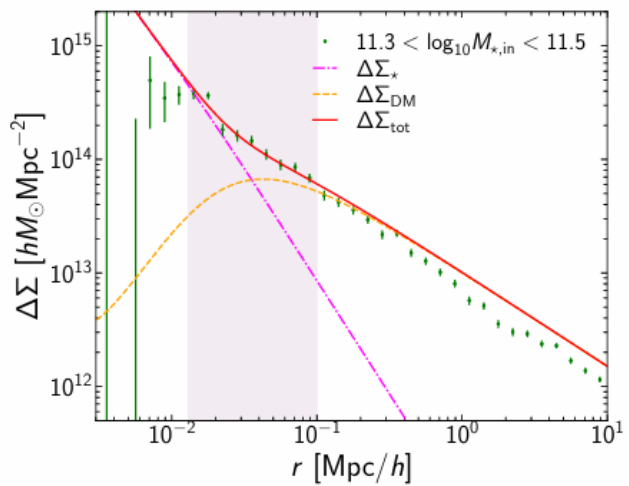
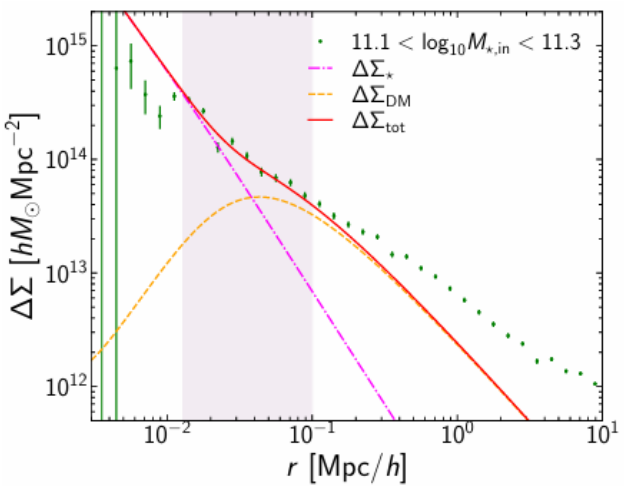
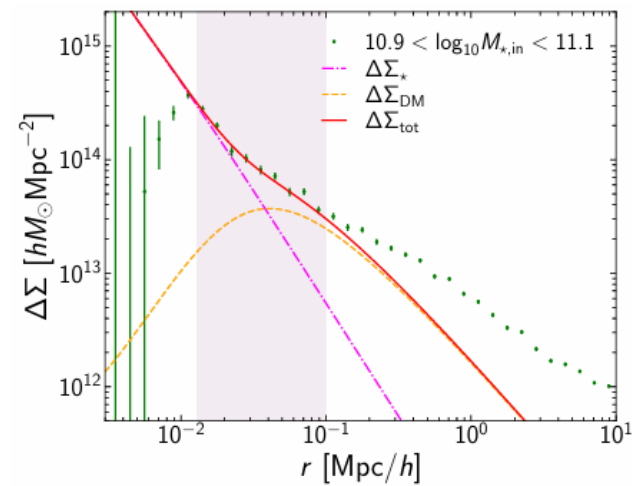
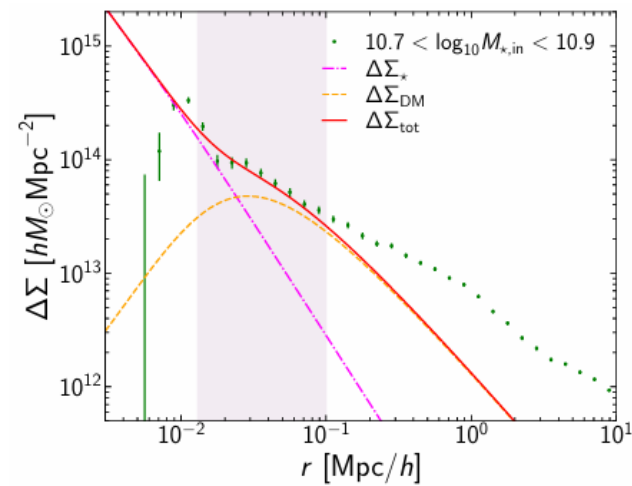
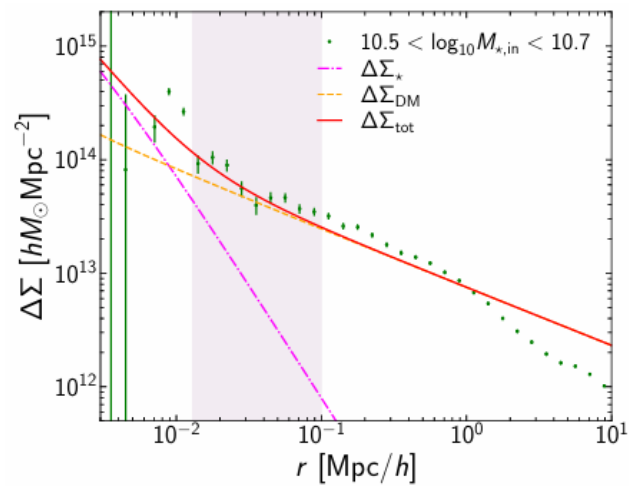
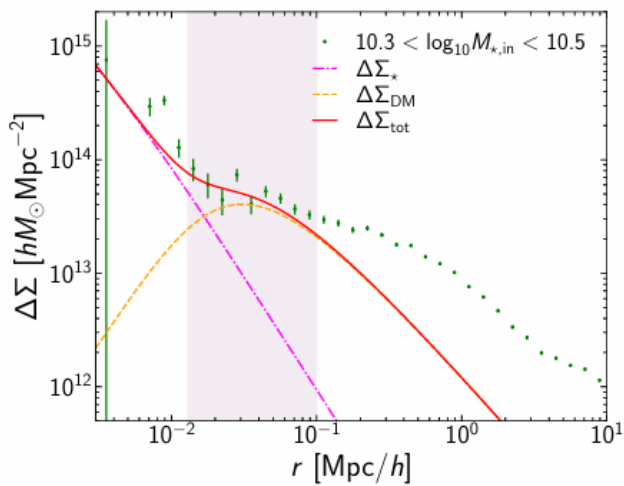
$$\Sigma_{DM}(r) = \int_{-\infty}^{\infty} \rho_{DM}(\sqrt{r^2 + Z^2}) dZ$$

$$M_{2D}(< r) = \int_0^r 2\pi r \Sigma_{DM}(r) dr$$

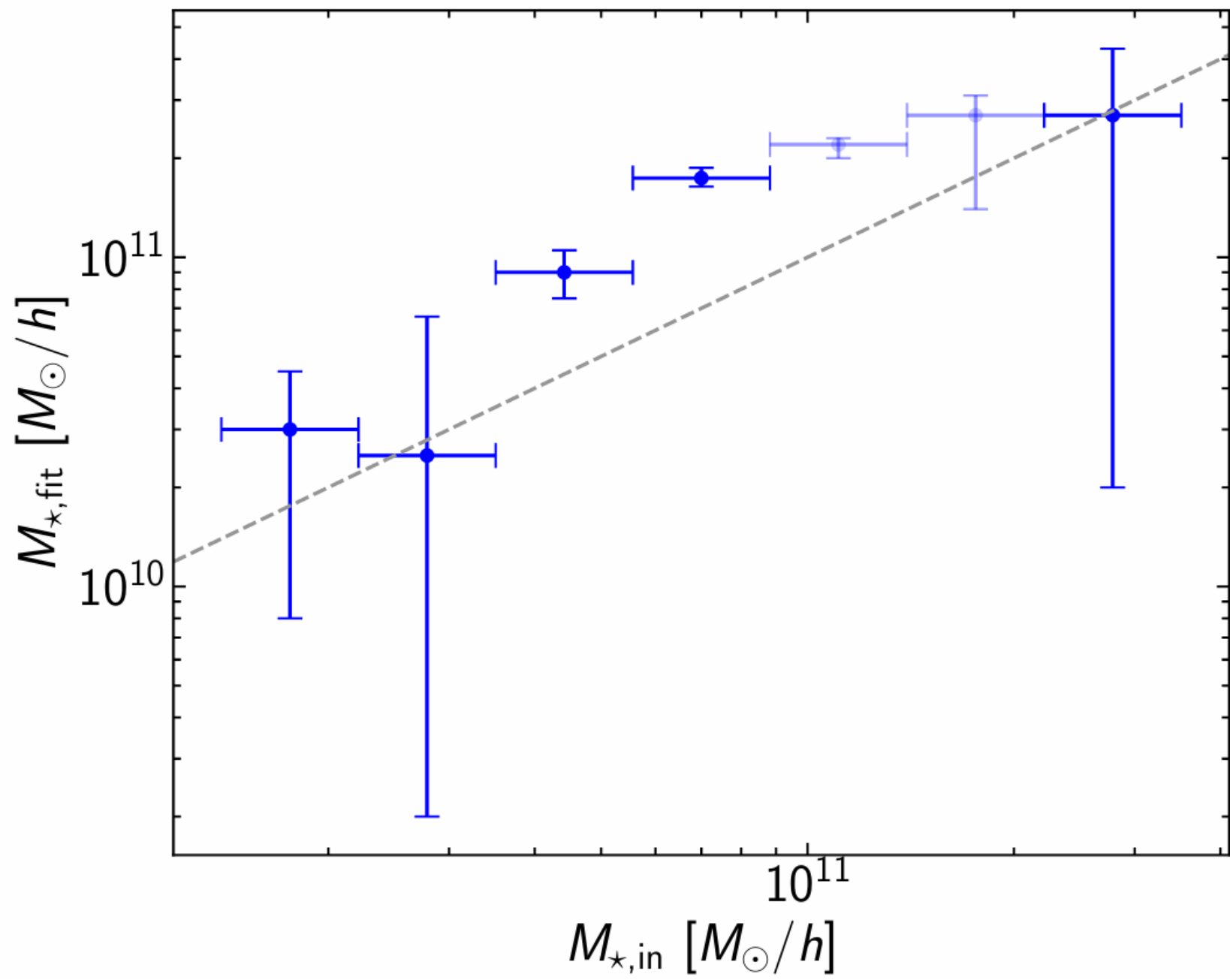
$$\bar{\Sigma}_{DM}(< r) = \frac{M_{2D}(< r)}{\pi r^2}$$

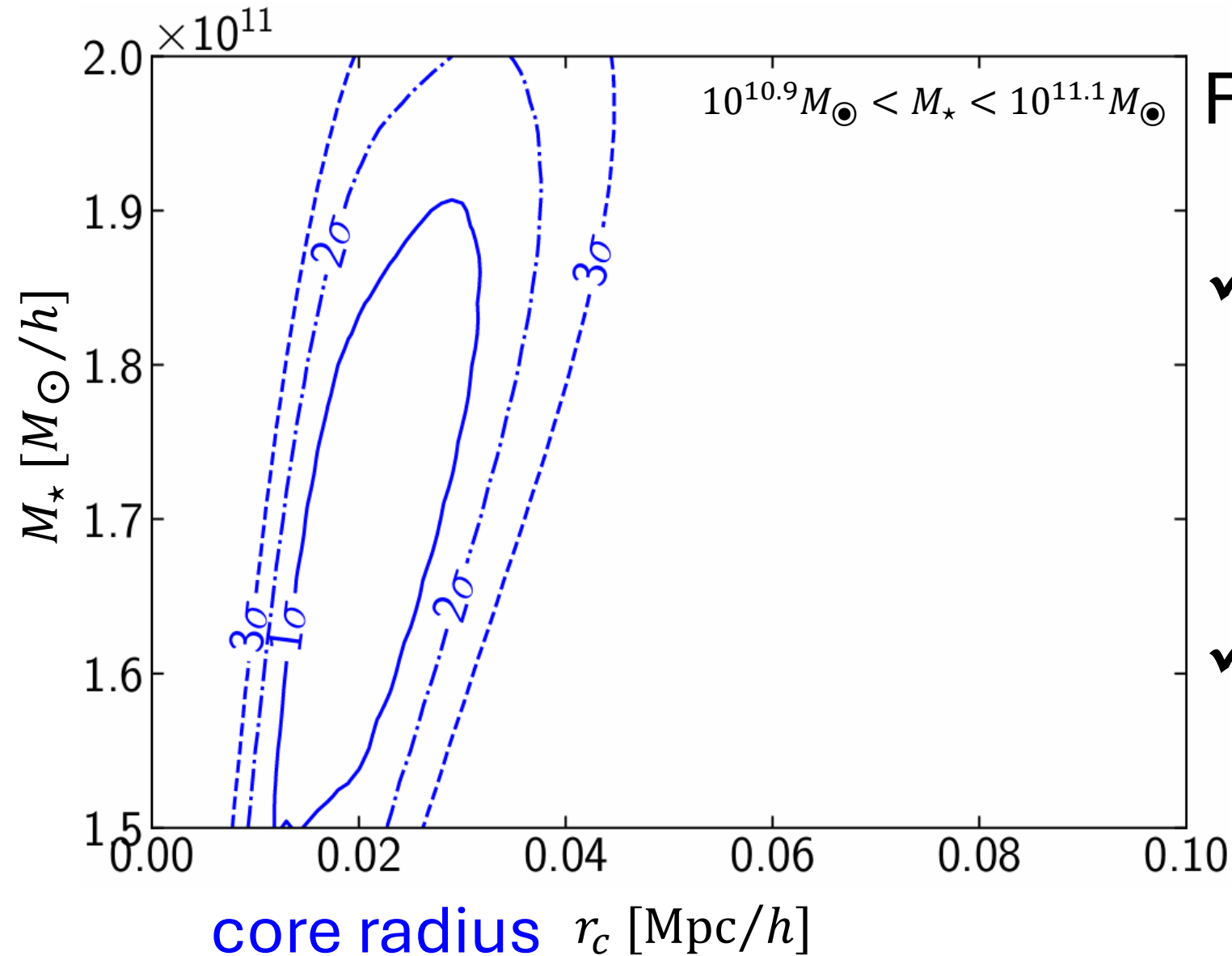
$$\Delta\Sigma_{DM} = \bar{\Sigma}_{DM}(< r) - \Sigma_{DM}(r)$$

 total mass $\Delta\Sigma_{tot} = \Delta\Sigma_{SM} + \Delta\Sigma_{DM}$



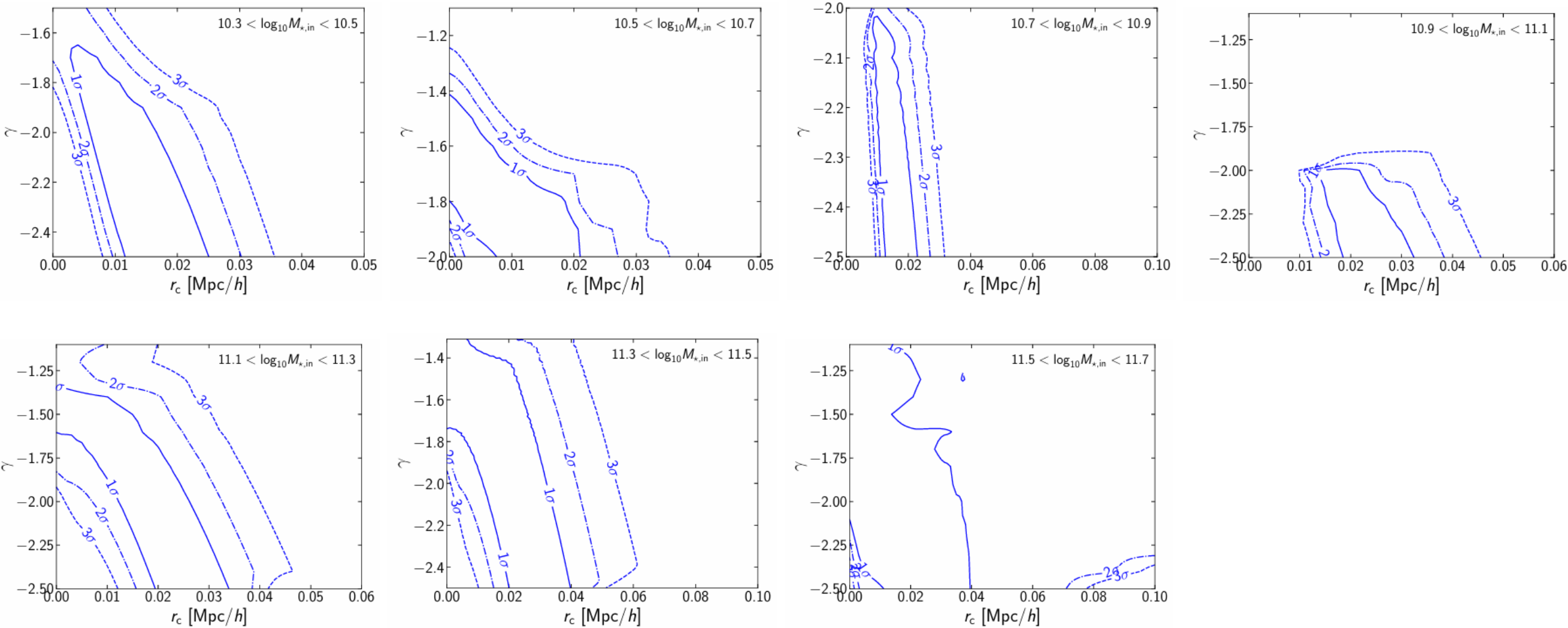
$\log_{10}(M_{\star,\text{in}}[M_{\odot}])$	N_{LRG}	r_e [Mpc/ h]	A	γ	r_c [Mpc/ h]	$M_{\star,\text{fit}}$ [$M_{\odot}/h$]	$\chi^2_{\text{in}}/\text{dof}$
10.3–10.5	1.81×10^5	1.4×10^{-3}	$7.5^{+12.0}_{-6.0}$	$-2.50^{+0.50}_{-0.00}$	$1.8^{+0.4}_{-0.9} \times 10^{-2}$	$3.0^{+1.5}_{-2.2} \times 10^{10}$	9.4/5
10.5–10.7	2.05×10^5	1.4×10^{-3}	$0.2^{+4.0}_{-0.0}$	$-1.51^{+0.06}_{-0.29}$	$0.0^{+1.5}_{-0.0} \times 10^{-2}$	$2.5^{+4.1}_{-2.3} \times 10^{10}$	10.2/5
10.7–10.9	2.23×10^5	1.4×10^{-3}	$2.7^{+0.4}_{-2.1}$	$-2.50^{+0.33}_{-0.00}$	$1.7^{+0.3}_{-0.4} \times 10^{-2}$	$9.0^{+1.5}_{-1.5} \times 10^{10}$	11.8/5
10.9–11.1	2.08×10^5	1.5×10^{-3}	$1.9^{+0.3}_{-1.6}$	$-2.50^{+0.41}_{-0.00}$	$2.4^{+0.5}_{-0.6} \times 10^{-2}$	$1.7^{+0.2}_{-0.1} \times 10^{11}$	8.8/5
11.1–11.3	1.49×10^5	1.8×10^{-3}	$1.9^{+0.7}_{-1.8}$	$-2.46^{+0.76}_{-0.04}$	$2.5^{+0.5}_{-1.3} \times 10^{-2}$	$2.2^{+0.1}_{-0.2} \times 10^{11}$	19.2/5
11.3–11.5	5.54×10^4	2.3×10^{-3}	$0.2^{+3.9}_{-0.1}$	$-1.83^{+0.52}_{-0.67}$	$1.8^{+1.7}_{-1.8} \times 10^{-2}$	$2.7^{+0.4}_{-1.3} \times 10^{11}$	11.1/5
11.5–11.7	1.02×10^4	3.3×10^{-3}	$0.2^{+8.0}_{-0.1}$	$-1.56^{+0.55}_{-0.52}$	$1^{+16}_{-1} \times 10^{-3}$	$2.7^{+1.6}_{-2.5} \times 10^{11}$	6.4/5





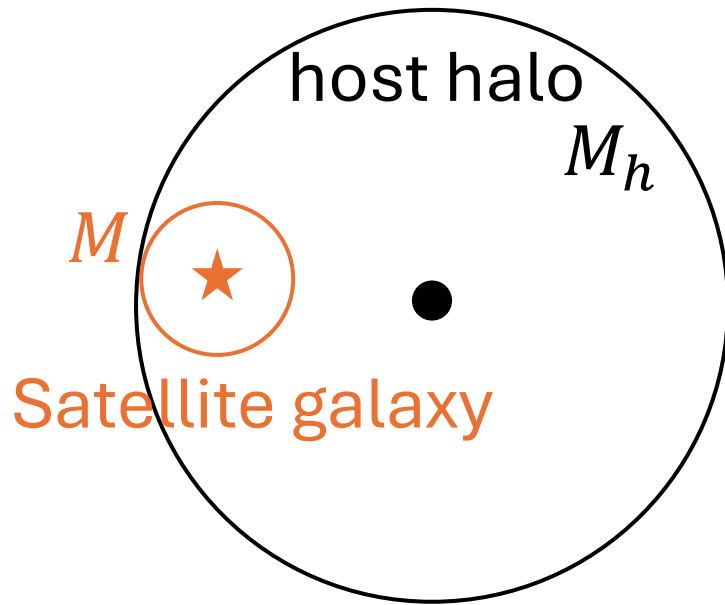
For $10^{10.7} M_{\odot} < M_{\star} < 10^{11.1} M_{\odot}$,

- ✓ r_c is **inconsistent** with zero within 3σ
 cored profile
- ✓ Because of the baryon feedback?



✓ $\Delta\Sigma(r) = \Delta\Sigma_{NFW}(M) + f_{sat}\Delta\Sigma_h(M_h) + \Delta\Sigma_{2h}(M, M_h)$

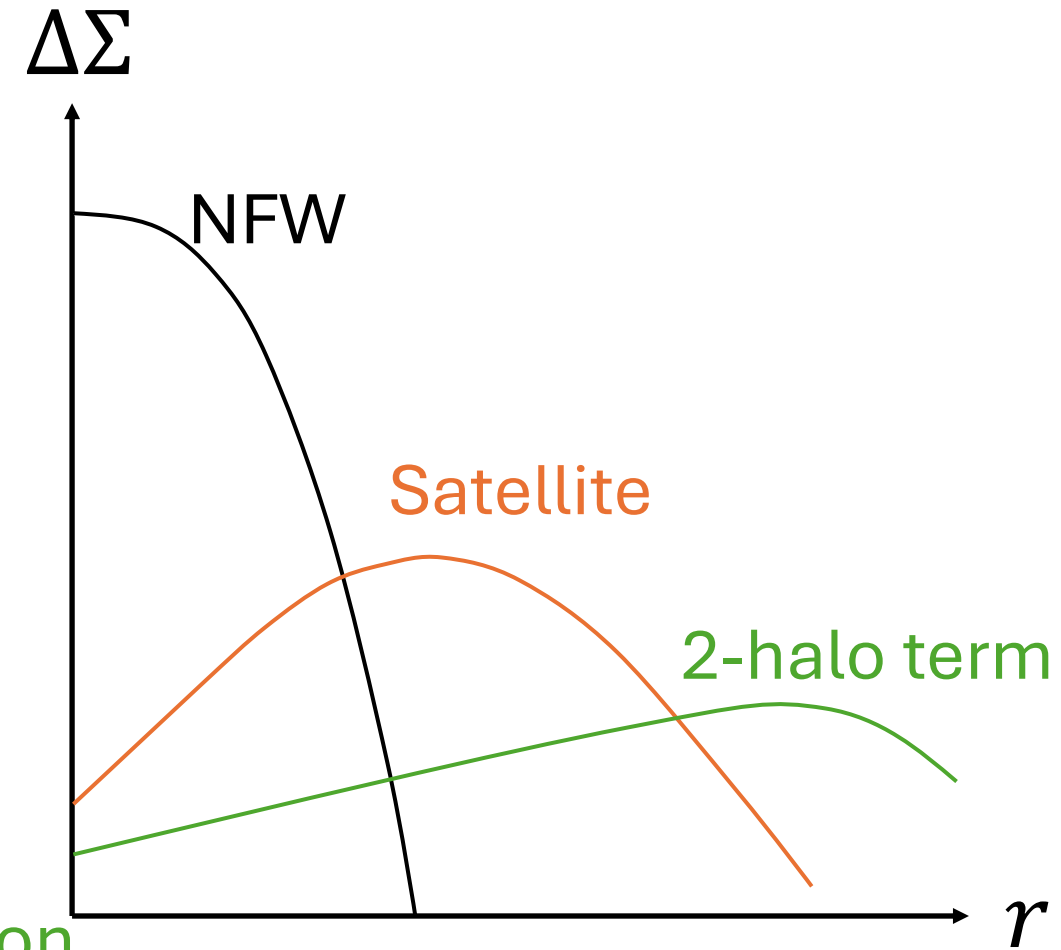
✓ Satellite galaxy

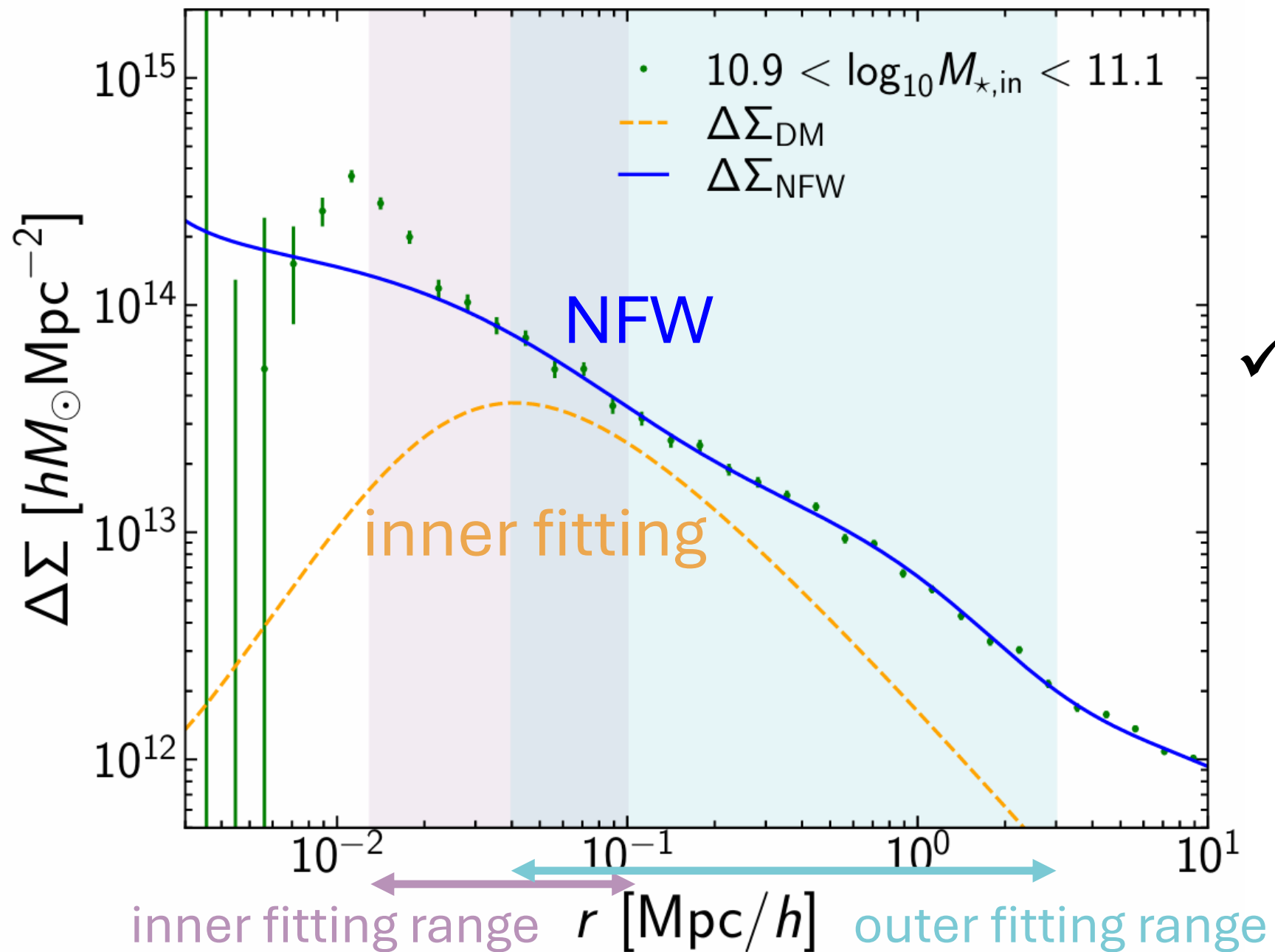


✓ 2-halo term

$$\Delta\Sigma_{2h}(M, M_h) \propto \underbrace{b(M, M_h)}_{\text{halo bias}} \times \underbrace{\xi_m}_{\text{correlation function}}$$

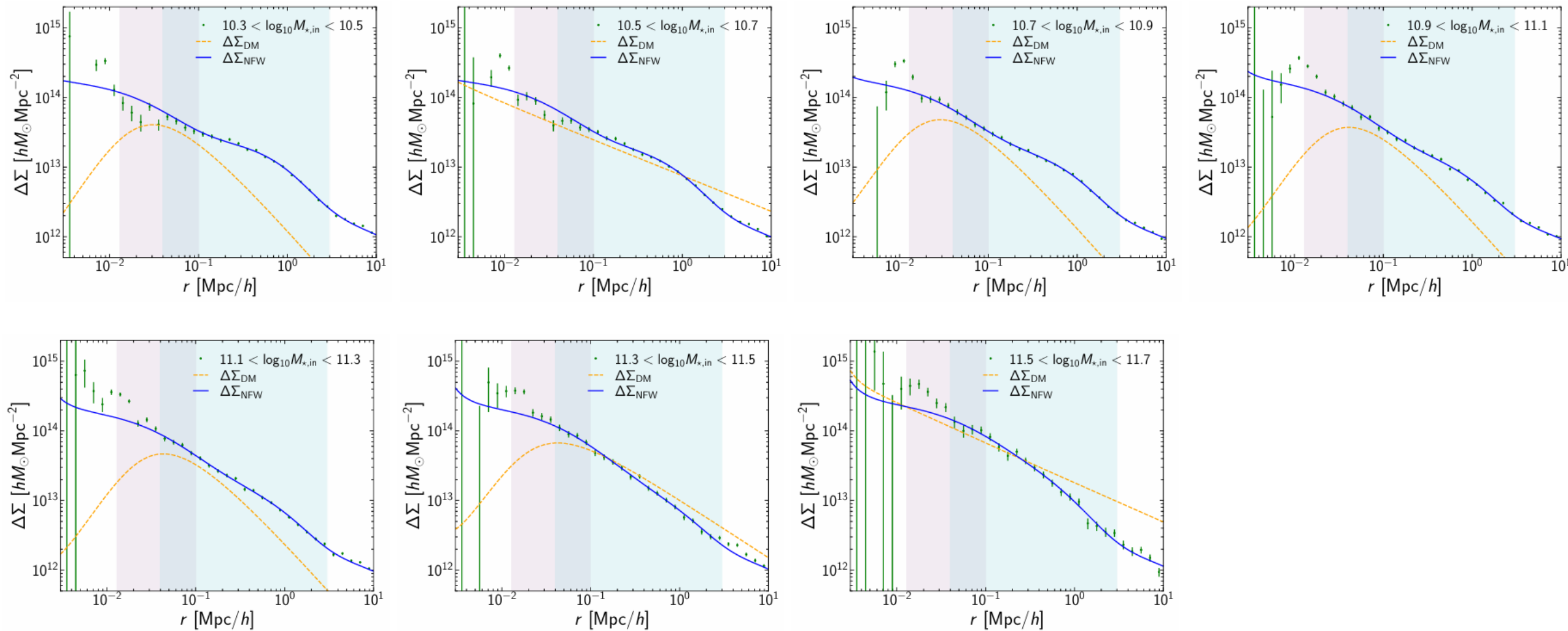
halo bias correlation function



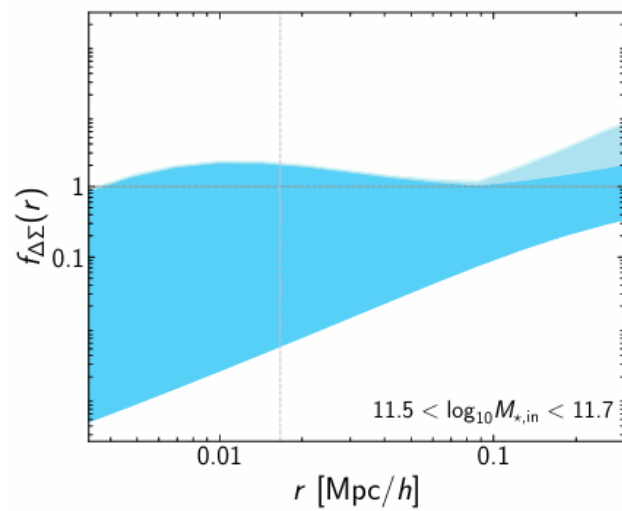
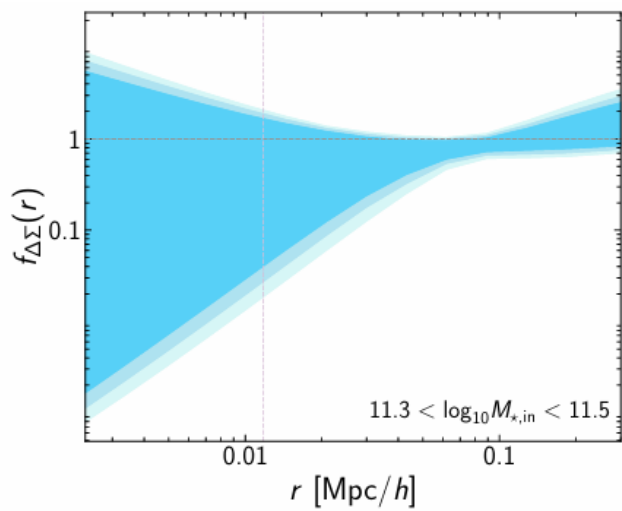
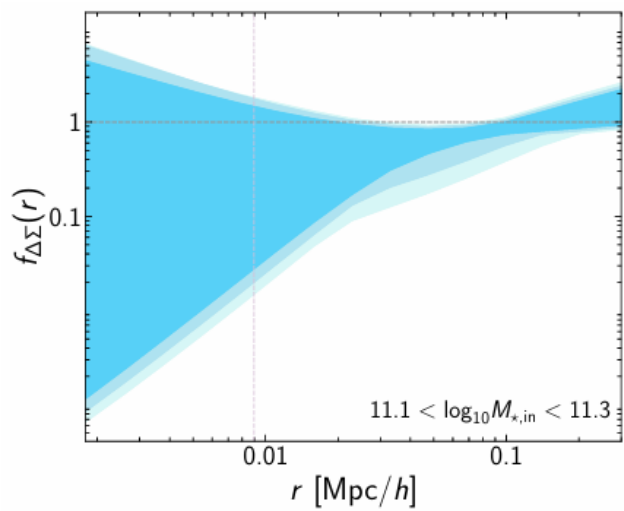
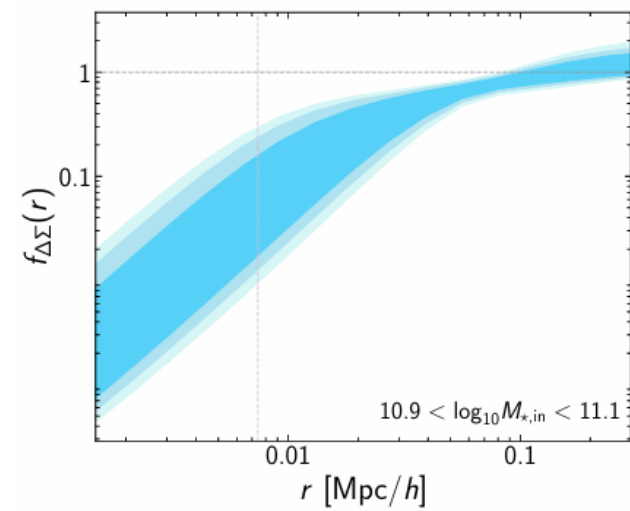
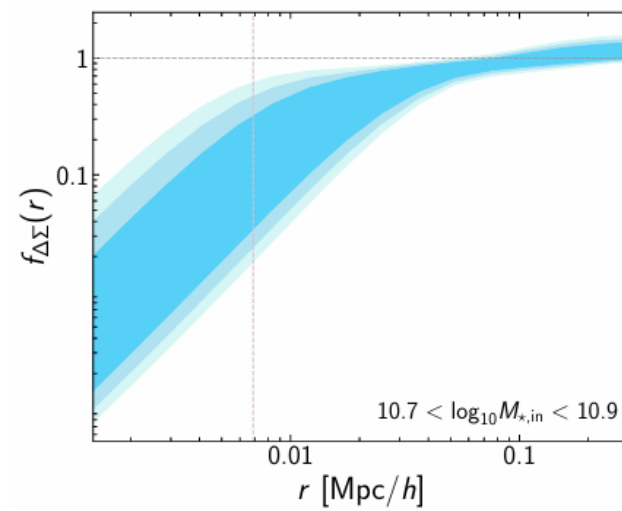
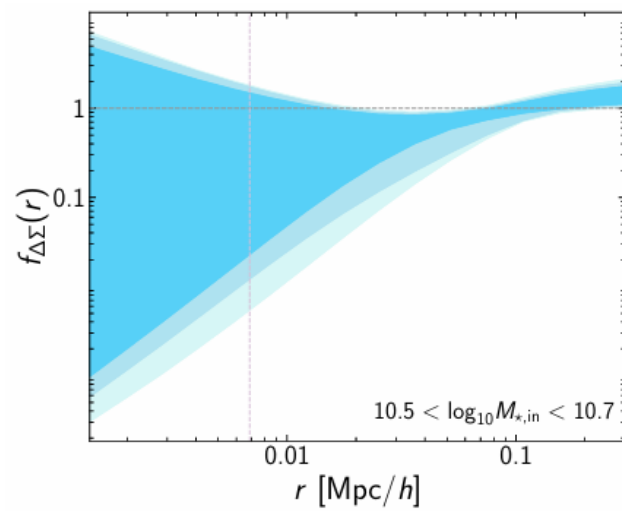
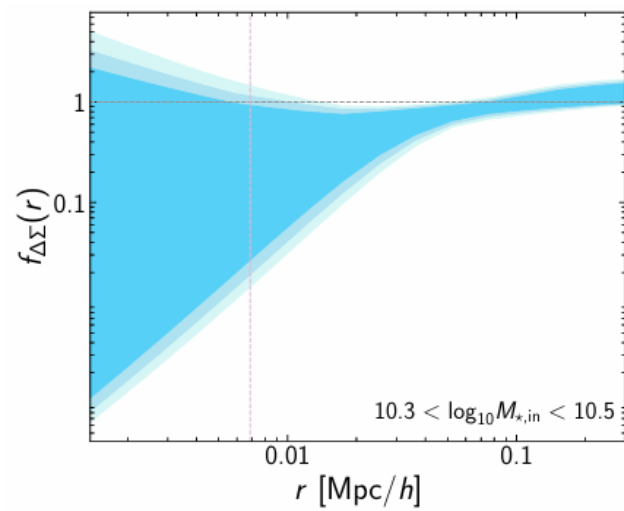


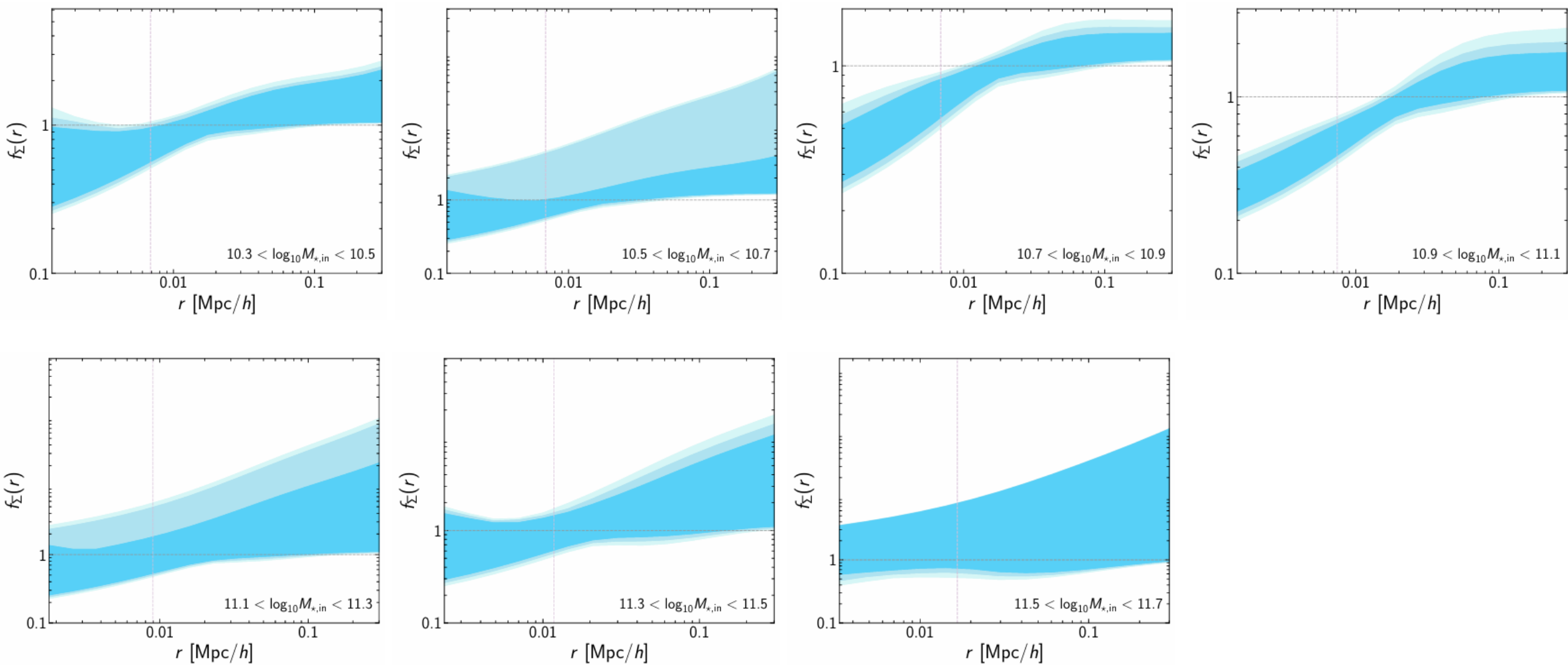
✓ evaluating with

$$f_{\Delta\Sigma}(r) = \frac{\Delta\Sigma_{\text{DM}}(r)}{\Delta\Sigma_{\text{NFW}}(r)}$$



$\log_{10}(M_{\star,\text{in}}[M_{\odot}])$	$M_{\text{NFW}} [M_{\odot}/h]$	$M_{\text{h}} [M_{\odot}/h]$	f_{sat}	$\chi^2_{\text{out}}/\text{dof}$
10.3–10.5	$1.2^{+0.1}_{-0.1} \times 10^{12}$	$5.1^{+0.1}_{-0.1} \times 10^{13}$	$0.40^{+0.00}_{-0.01}$	19.3/16
10.5–10.7	$1.3^{+0.1}_{-0.1} \times 10^{12}$	$5.4^{+0.5}_{-0.4} \times 10^{13}$	$0.32^{+0.02}_{-0.02}$	20.9/16
10.7–10.9	$1.4^{+0.1}_{-0.1} \times 10^{12}$	$5.5^{+0.6}_{-0.1} \times 10^{13}$	$0.27^{+0.02}_{-0.02}$	19.3/16
10.9–11.1	$1.8^{+0.1}_{-0.1} \times 10^{12}$	$6.8^{+0.9}_{-0.7} \times 10^{13}$	$0.21^{+0.02}_{-0.02}$	31.4/16
11.1–11.3	$2.6^{+0.2}_{-0.1} \times 10^{12}$	$6.7^{+1.1}_{-0.6} \times 10^{13}$	$0.21^{+0.02}_{-0.03}$	13.31/16
11.3–11.5	$4.7^{+0.4}_{-0.3} \times 10^{12}$	$1.1^{+0.4}_{-0.3} \times 10^{14}$	$0.14^{+0.03}_{-0.03}$	19.2/16
11.5–11.7	$7.6^{+1.3}_{-1.2} \times 10^{12}$	$4.9^{+4.1}_{-1.6} \times 10^{13}$	$0.30^{+0.10}_{-0.10}$	16.0/16





$\log_{10}(M_{\star,\text{in}}[M_{\odot}])$	$f_{\text{DM}}(< 5r_{\text{e}})$
10.3–10.5	$0.19^{+0.70}_{-0.12}$
10.5–10.7	$0.51^{+0.45}_{-0.47}$
10.7–10.9	$0.087^{+0.125}_{-0.050}$
10.9–11.1	$0.035^{+0.050}_{-0.017}$
11.1–11.3	$0.056^{+0.431}_{-0.025}$
11.3–11.5	$0.14^{+0.53}_{-0.08}$
11.5–11.7	$0.50^{+0.42}_{-0.49}$

