

Hayato Motohashi, JGRG 22(2012)111417

“Cosmological constraints on sterile neutrino mass in $f(R)$
gravity”

**RESCEU SYMPOSIUM ON
GENERAL RELATIVITY AND GRAVITATION**

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Cosmological constraints on sterile neutrino mass in $f(R)$ gravity

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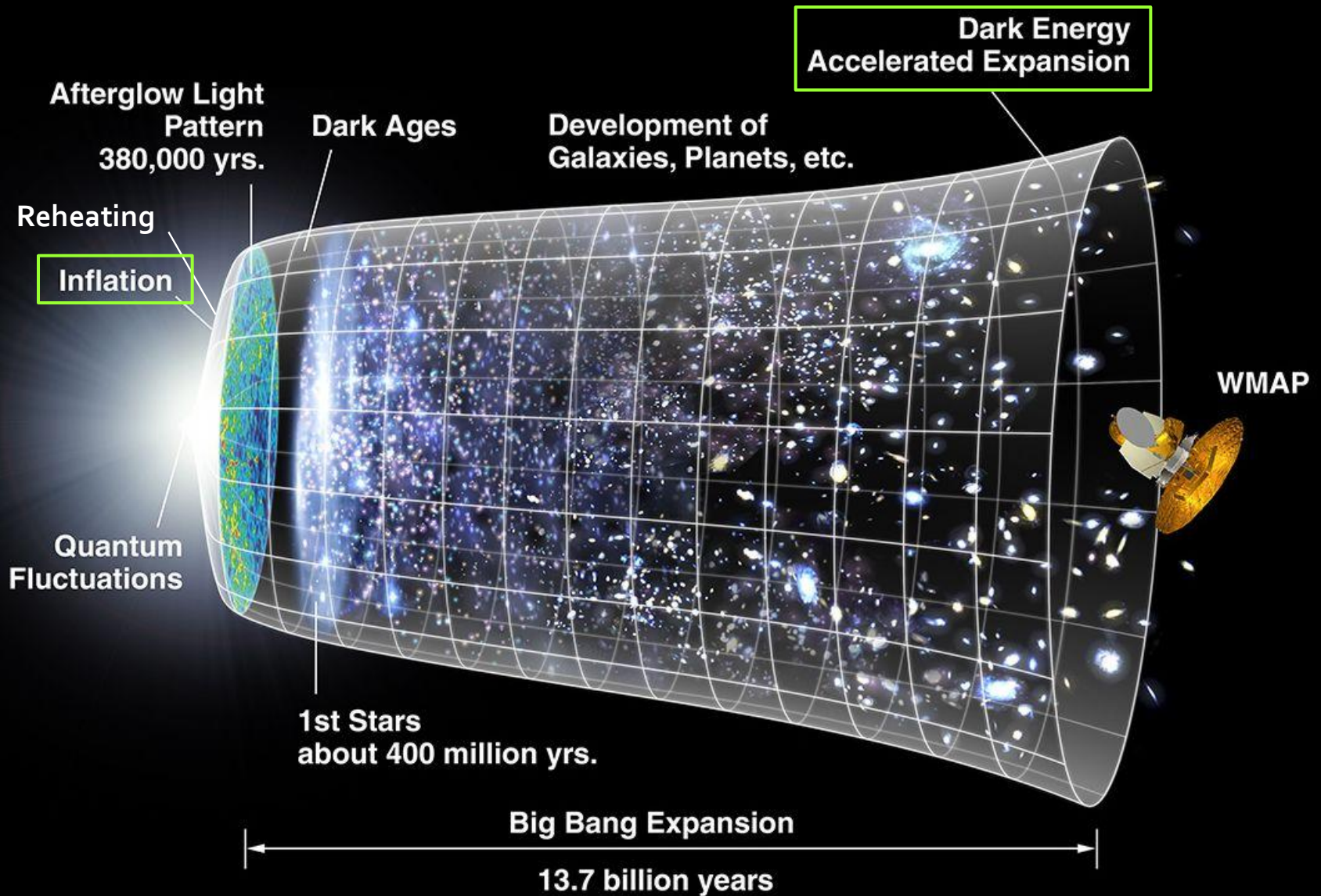
in collaboration with

Alexei A. Starobinsky (Landau Inst.)

Jun'ichi Yokoyama (RESCEU)



Two regimes of accelerated expansion



$f(R)$ gravity

can describe the accelerated expansion.

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} f(R) + S_m$$

Primordial inflation

Starobinsky, Phys.Lett. B91 (1980) 99

$$f(R) = R + \frac{R^2}{6M^2}$$

Late-time acceleration

Starobinsky, JETP Lett. 86, 157 (2007)
[arXiv:0706.2041]

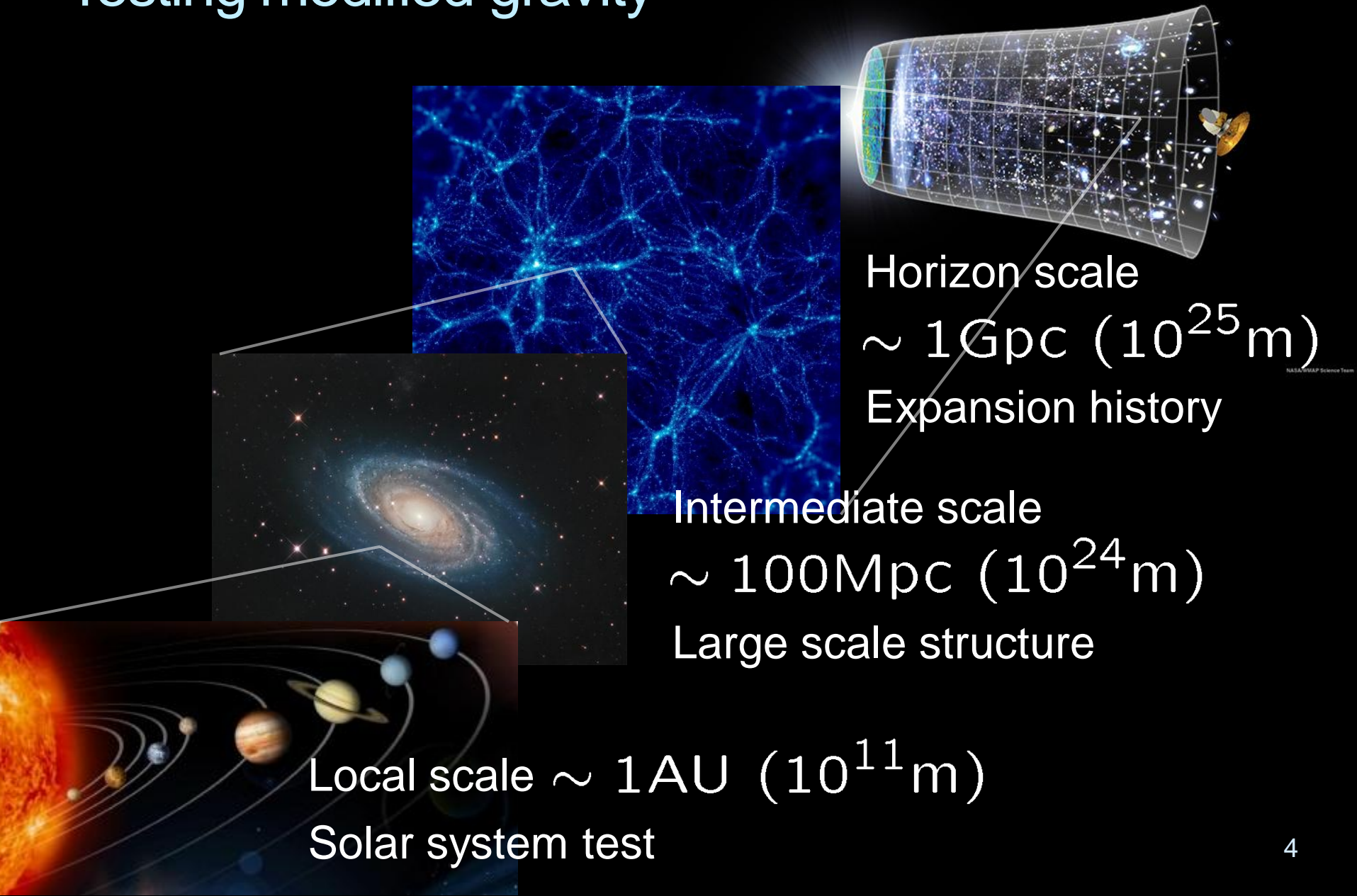
$$f(R) = R + \lambda R_s \left[\left(\frac{R^2}{R_s^2} + 1 \right)^{-n} - 1 \right]$$

cf. $f(R)$ model for both accelerated expansion

Appleby, Battye, Starobinsky, JCAP 1006, 005 (2010) [arXiv:0909.1737]

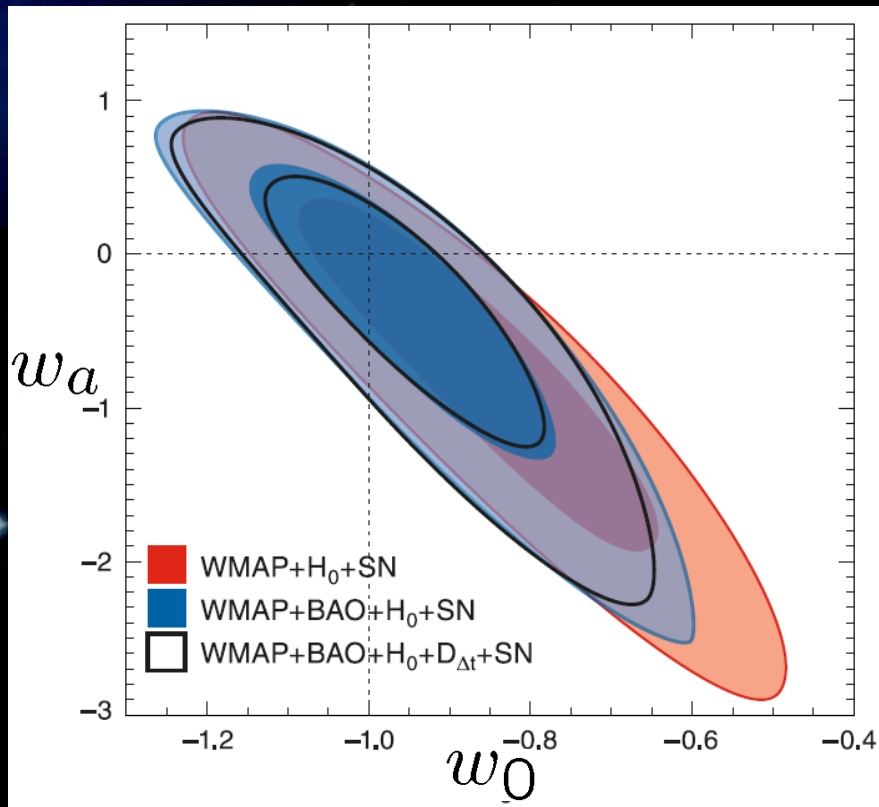
H.M., Nishizawa, PRD 86 (2012) 093514 [arXiv:1204.1472]

Testing modified gravity

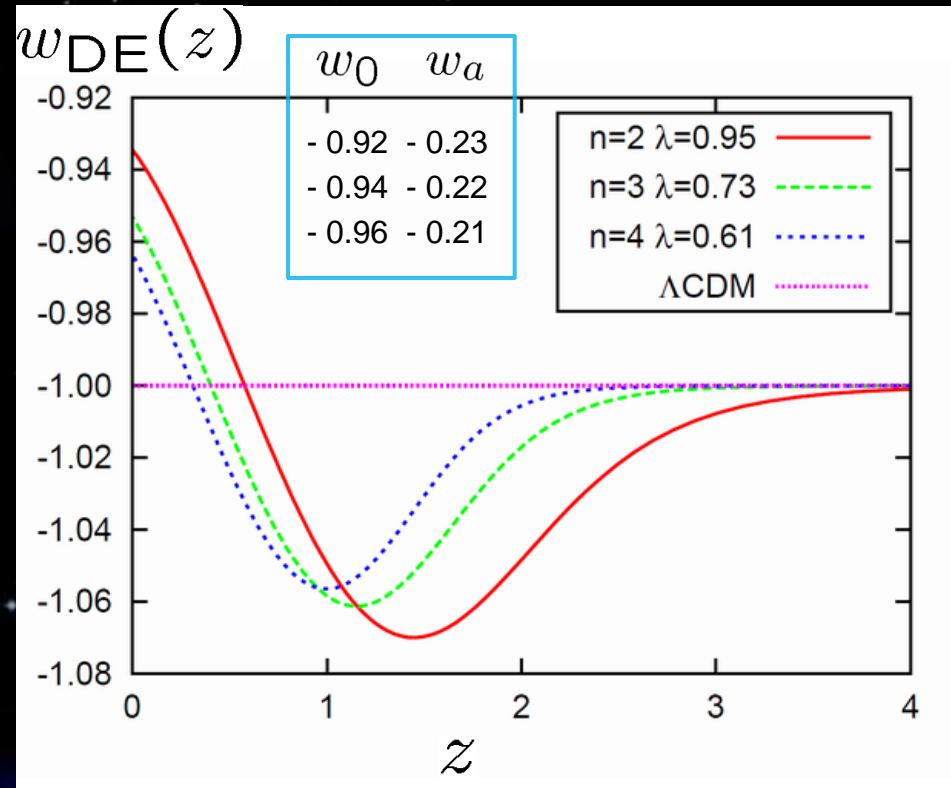


Time variation of EoS parameter $w \equiv P/\rho$

$$w_{\text{DE}} = w_0 + \frac{w_a z}{1+z}$$



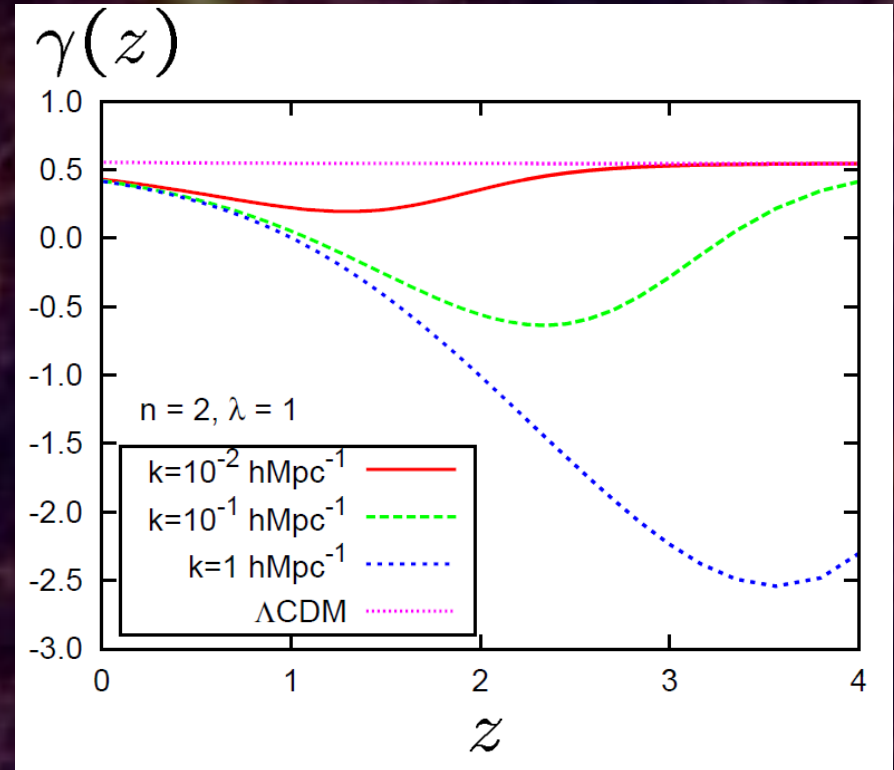
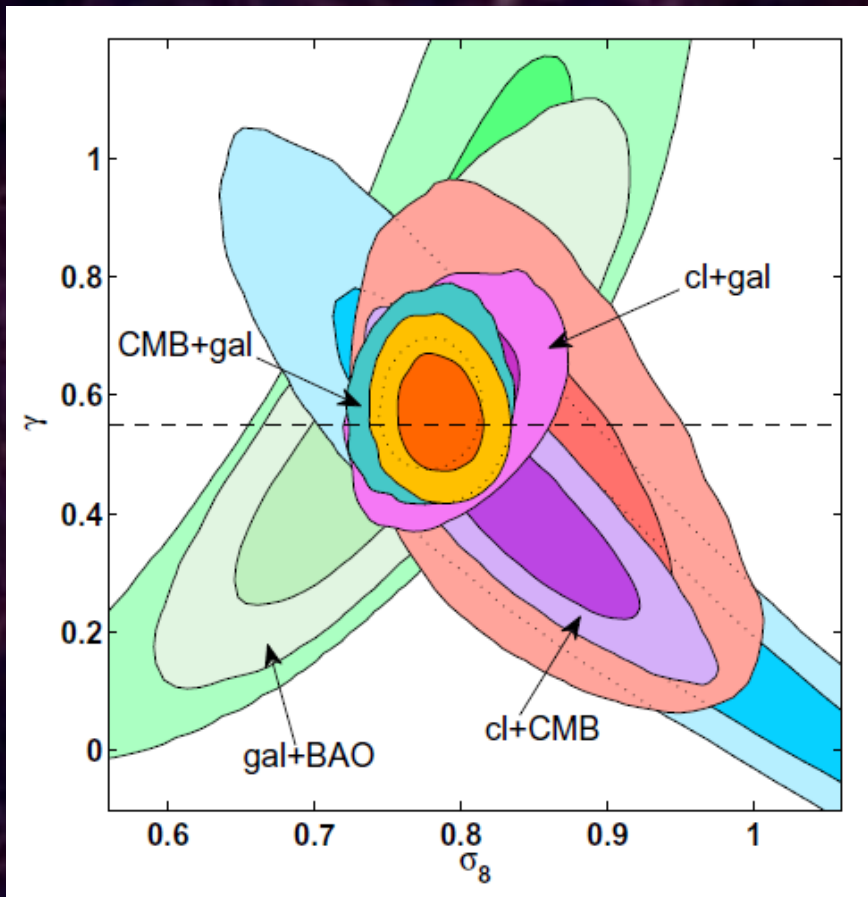
Komatsu et al.,
 APJ Suppl. 192, 18 (2011)
 [arXiv:1001.4538]



H.M., Starobinsky, Yokoyama
 PTP 123 (2010) 887 [arXiv:1002.1141] 5

Growth index $\gamma(z)$

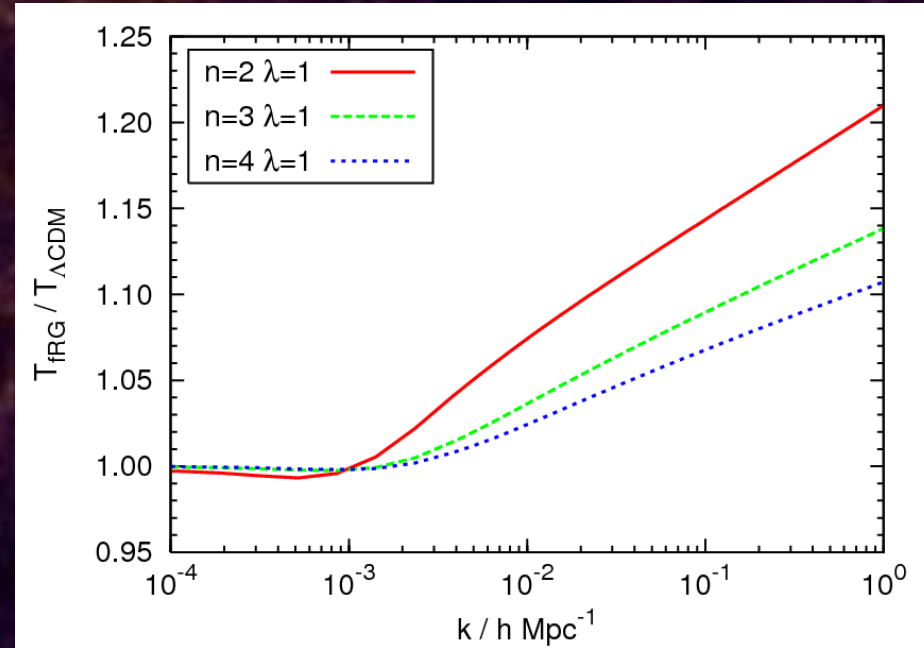
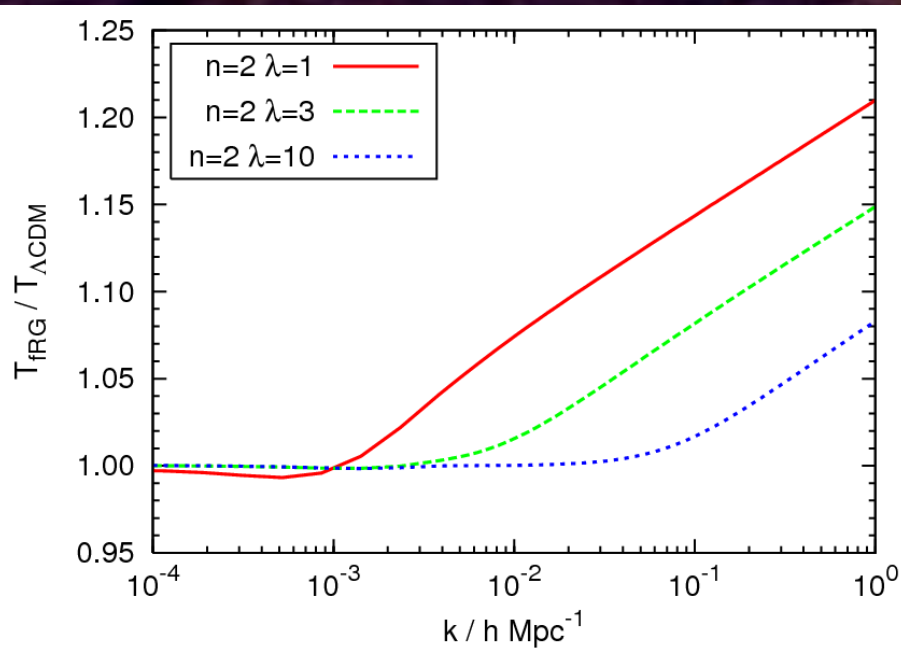
$$\frac{d \log \delta}{d \log a} = \Omega_m(z) \gamma(z)$$



H.M., Starobinsky, Yokoyama
PTP 123 (2010) 887 [arXiv:1002.1141]

Rapetti et al., arXiv: 1205.4679

Additional transfer function in $f(R)$ gravity



$f(R)$ gravity enhances matter power spectrum.

↕ cancel

Massive neutrino suppresses matter power spectrum.

Constraint on N_{eff} from BBN

Abazajian et al [arXiv:1204.5379]

Model	Data	N_{eff}	Ref.
$\eta+N_{eff}$	$\eta_{CMB}+Y_p+D/H$	$3.8^{(+0.8)}_{(-0.7)}$	[331]
	$\eta_{CMB}+Y_p+D/H$	$< (4.05)$	[332]
	Y_p+D/H	3.85 ± 0.26	[333]
		3.82 ± 0.35	[333]
3.13 ± 0.21		[333]	
$\eta+N_{eff}, (\Delta N_{eff} \equiv N_{eff} - 3.046 \geq 0)$	$\eta_{CMB}+D/H$	3.8 ± 0.6	[122]
	$\eta_{CMB}+Y_p$	$3.90^{+0.21}_{-0.58}$	[122]
	Y_p+D/H	$3.91^{+0.22}_{-0.55}$	[122]

[331] Izotov, Thuan, *Astrophys.J.* 710, L67 (2010) [arXiv:1001.4440]

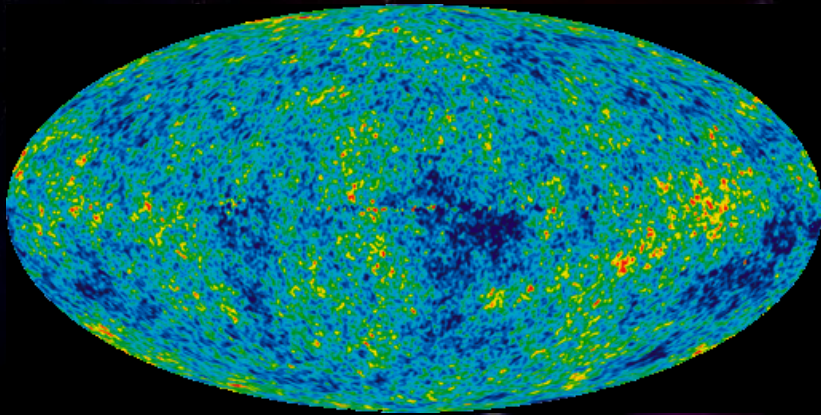
[332] Mangano, Serpico, *Phys.Lett. B* 701, 296 (2011) [arXiv:1103.1261]

[333] Nollett, Holder [arXiv:1112.2683]

[122] Hamann et al, *JCAP* 1109, 034 (2011) [arXiv:1108.4136]

Constraints on N_{eff} and $\sum m_\nu$ in ΛCDM

CMB



Komatsu et al.,
APJ Suppl. 192, 18 (2011)
[arXiv:1001.4538]

+

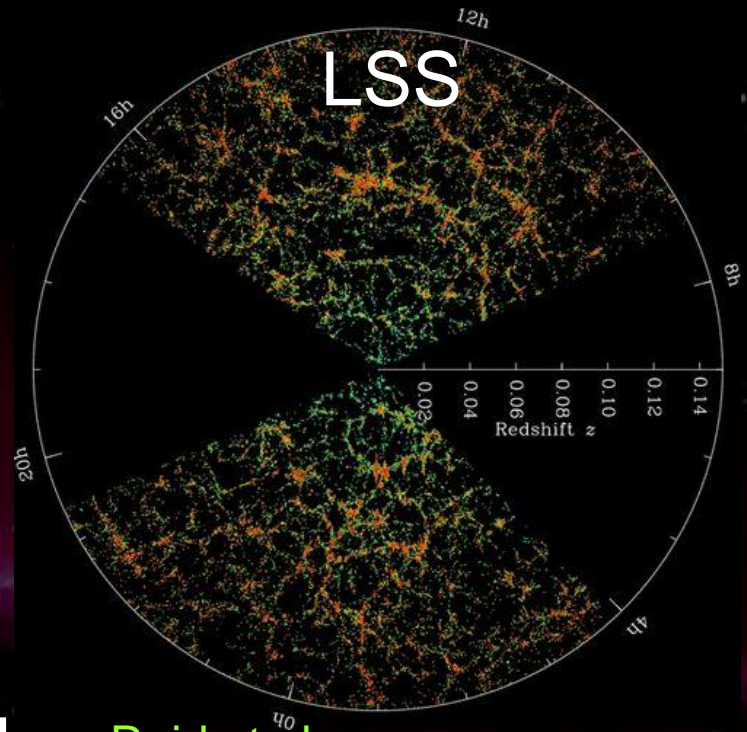
ΛCDM



$$\sum m_\nu < 0.44\text{eV} \quad (95\% \text{ CL})$$

$$N_{\text{eff}} = 4.34^{+0.86}_{-0.88} \quad (68\% \text{ CL})$$

LSS

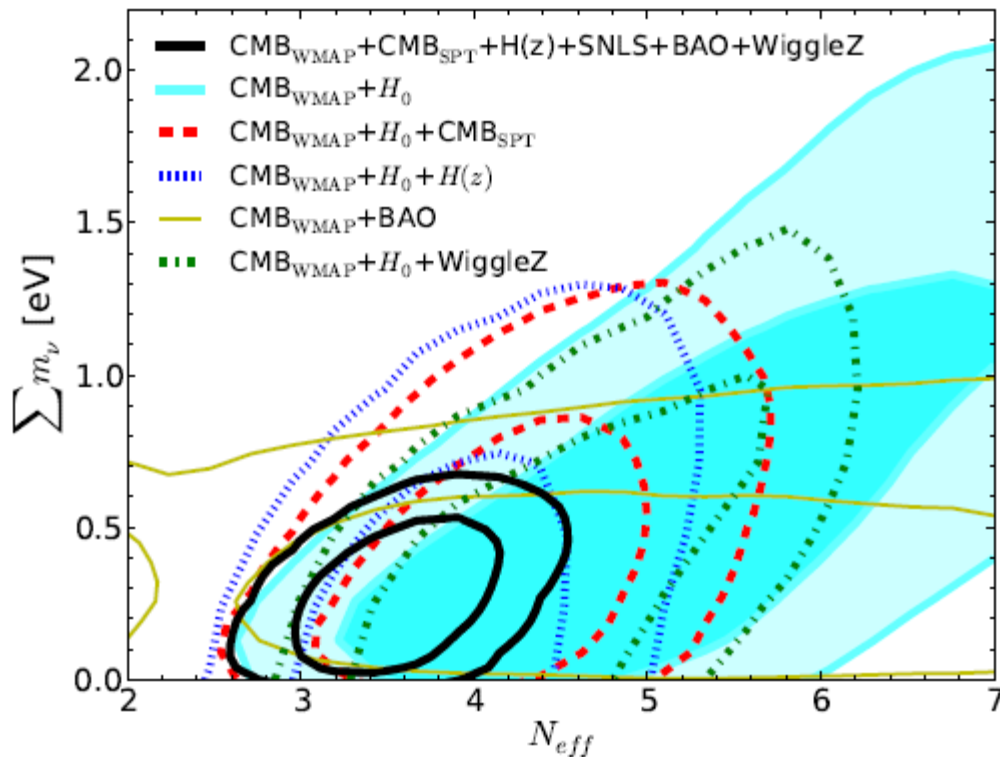


Reid et al,
Mon.Not.Roy.Astron.Soc. 404
(2010) 60 [arXiv:0907.1659]

Constraints on N_{eff} and $\sum m_\nu$ in Λ CDM

ABSTRACT

Recent indications from both particle physics and cosmology suggest the existence of more than three neutrino species. In cosmological analyses the effects of neutrino mass and number of species can in principle be disentangled for fixed cosmological parameters. However, since we do not have perfect measurements of the standard Λ Cold Dark Matter model parameters some correlation remains between the neutrino mass and number of species, and both parameters should be included in the analysis. Combining the newest observations of several cosmological probes (cosmic microwave background, large scale structure, expansion rate) we obtain $N_{\text{eff}} = 3.58^{+0.15}_{-0.16}$ (68% CL) $^{+0.55}_{-0.53}$ (95% CL) and $\sum m_\nu < 0.60$ eV (95% CL), which are currently the strongest constraints on N_{eff} and $\sum m_\nu$ from an analysis including both parameters. The preference for $N_{\text{eff}} > 3$ is now at a 2σ level.



Riemer-Sorensen et al
[arXiv:1210.2131]

Λ CDM cosmology



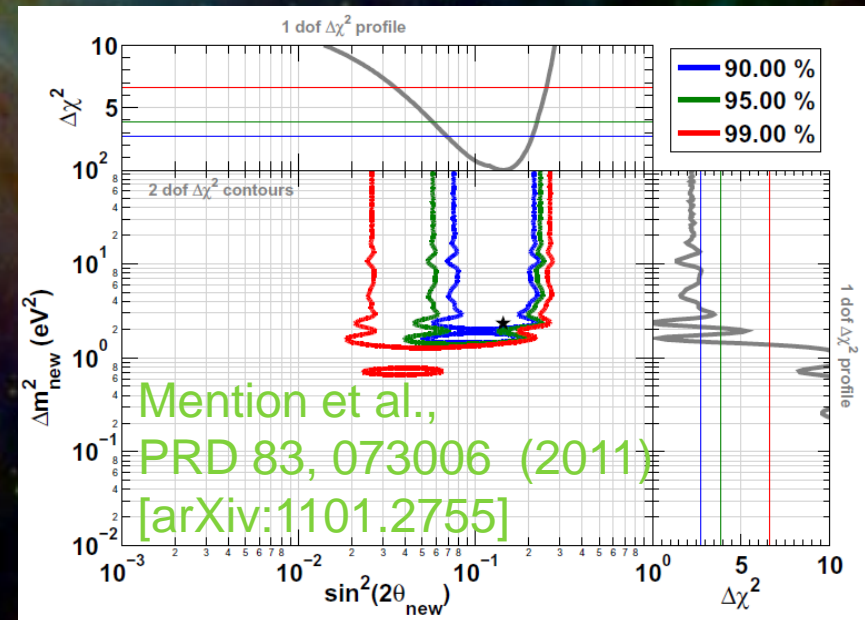
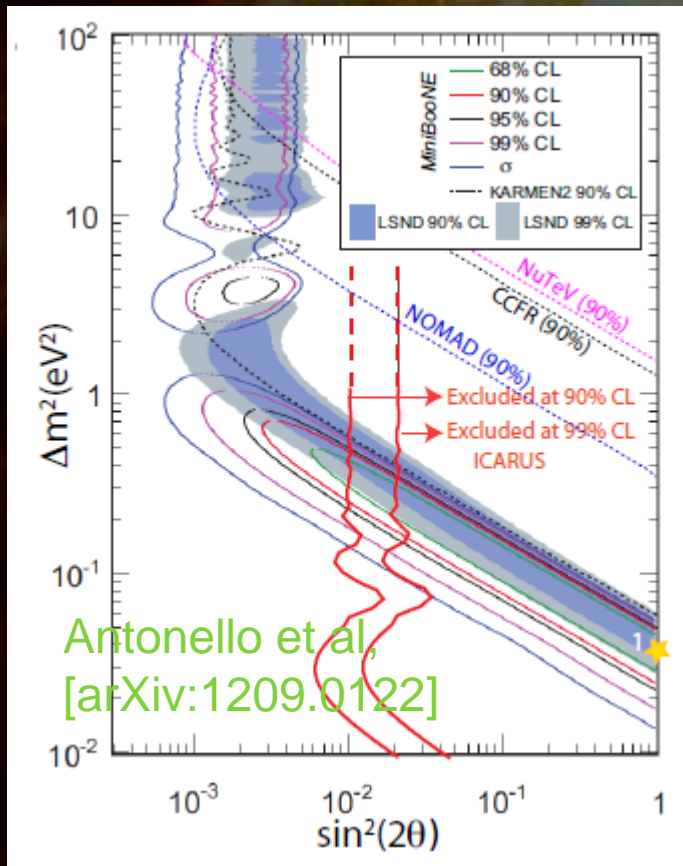
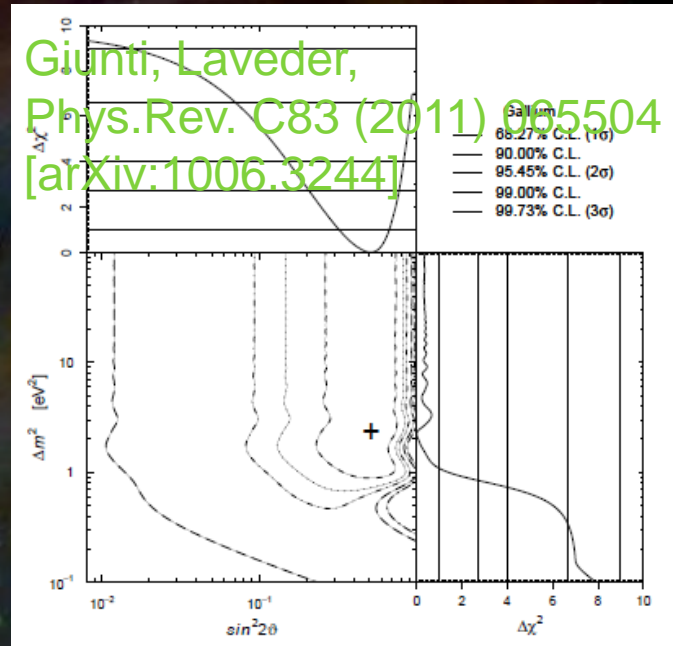
sub-eV

sterile neutrino

Neutrino oscillation

Sterile neutrino mass $\gtrsim 1$ eV

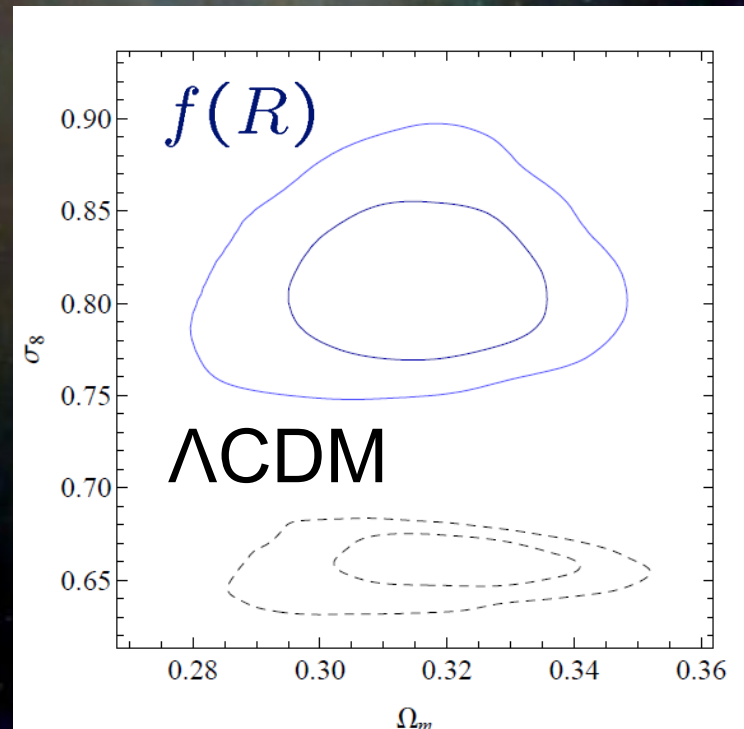
$\Leftrightarrow \Lambda$ CDM model



MCMC analysis: Λ CDM vs $f(R)$ gravity

H.M., Starobinsky and Yokoyama, arXiv:1203.6828

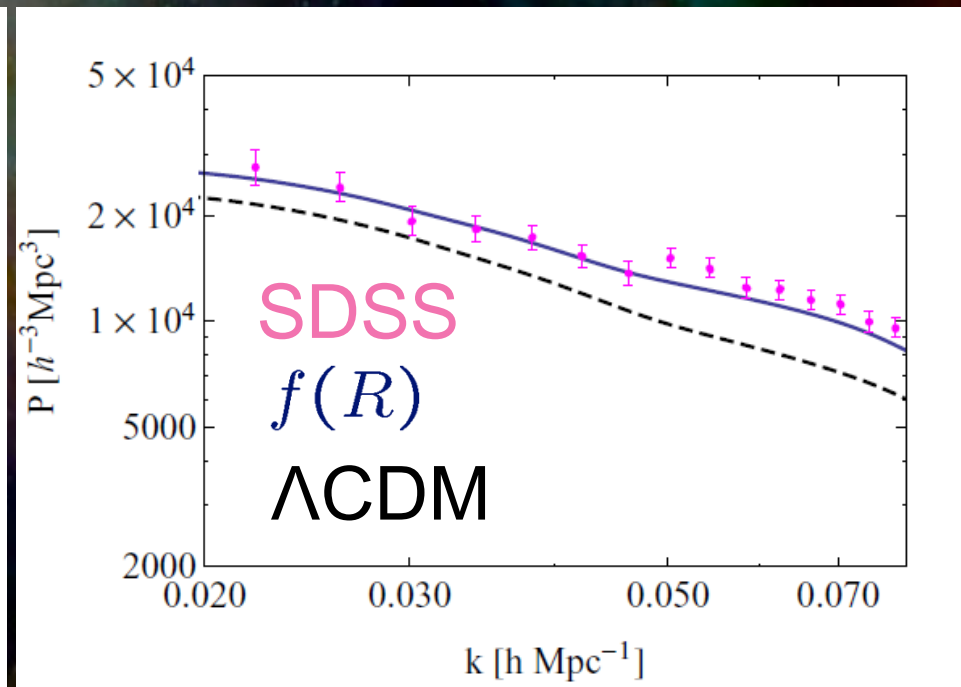
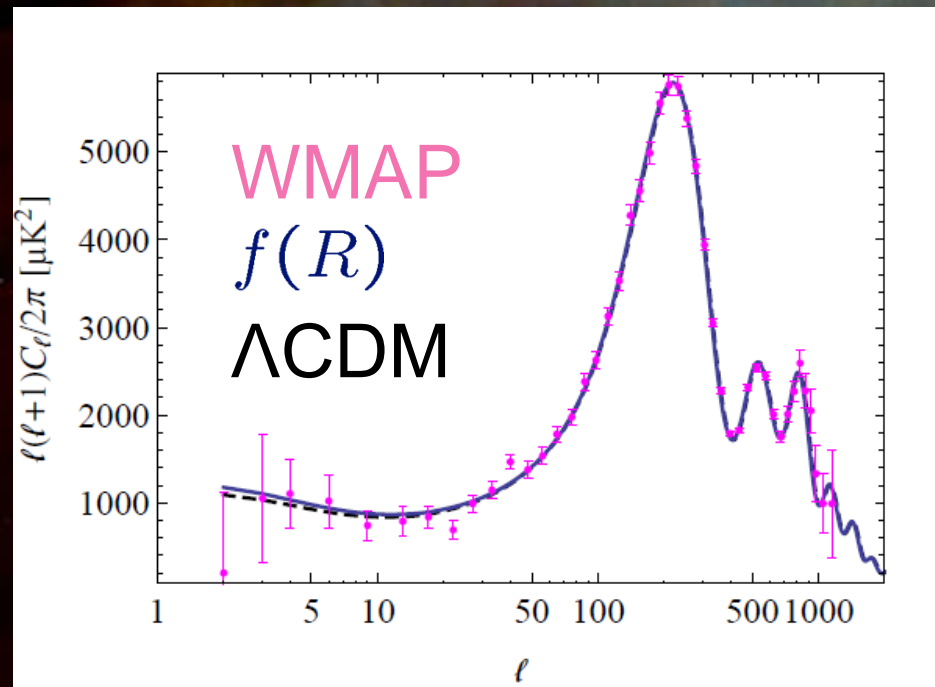
- 3 massless and 1 massive neutrino with mass = 1 eV
- WMAP7, SDSS DR 7 ($0.02h\text{Mpc}^{-1} \leq k \leq 0.08h\text{Mpc}^{-1}$)
- Better fit : $\Delta\chi^2 = 10.7$ ($\Delta\text{AIC} = 8.7$)
- GR : $\sigma_8 = 0.661_{-0.027}^{+0.023}$, $f(R)$: $\sigma_8 = 0.815_{-0.066}^{+0.105}$



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Summary

- Cosmology based on Λ CDM model
Sterile neutrino mass < 1 eV
- Neutrino oscillation experiments
Sterile neutrino mass $\gtrsim 1$ eV
- $f(R)$ gravity can resolve the tension.