NEW HIGGS INFLATION

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Solution: Increase the friction!

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Quantum Gravity regime is avoided during Inflation!

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This defines the "New Higgs Inflation" Lagrangian:

$$S = \int d^4x\sqrt{-g}\left[\frac{R}{2\kappa^2} - \frac{1}{2}\left(g^{\alpha\beta} - \omega^2 G^{\alpha\beta}\right)\partial_\alpha\Phi\partial_\beta\Phi - \frac{\lambda}{4}\Phi^4\right]$$

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The unique action is the New Higgs Inflation action!!!

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Unitarity *is not* violated up to the Quantum Gravity scales!!!!

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- so $n_s \leq 1 \longrightarrow f > M_p \Rightarrow$ the model cannot be trusted!

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Once again we can increase the friction so that

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- *Is invariant* under the global unbroken symmetry $\Phi \to \Phi + c$

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- WMAP 7-years results reproduced
- New proposal: small field inflation with Nambu-Goldston Boson $\longrightarrow$ New Natural Inflation