

# Dark Matter Annihilation with Electroweak Bremsstrahlung

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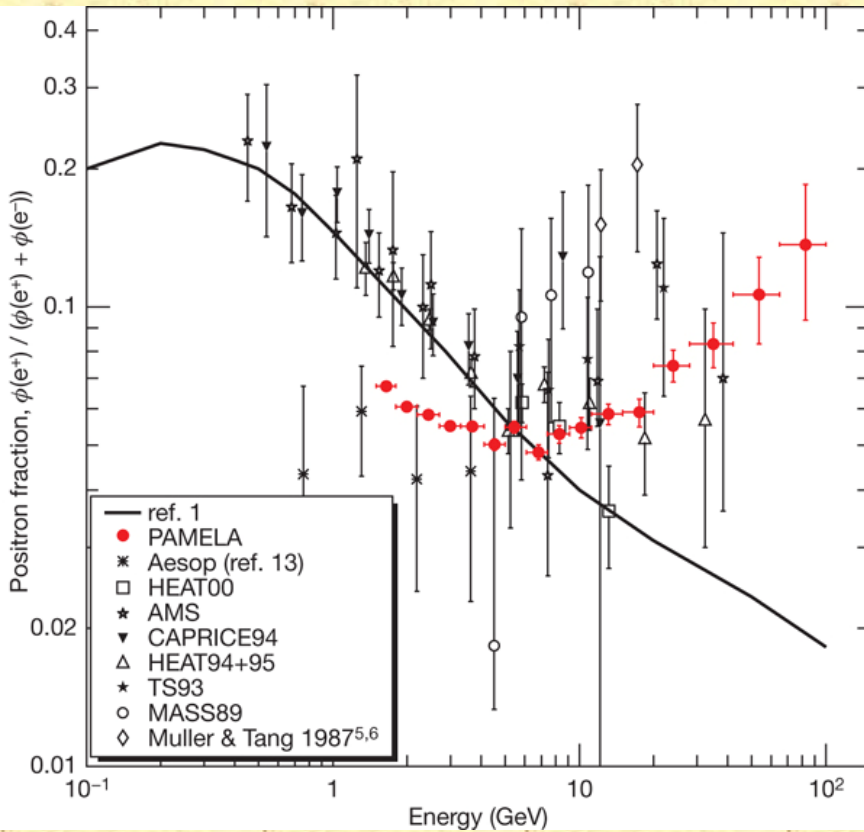
# Leptophilic Dark Matter

- ❖ Consider “**Leptophilic**” models:
  - dark matter couples only to leptons

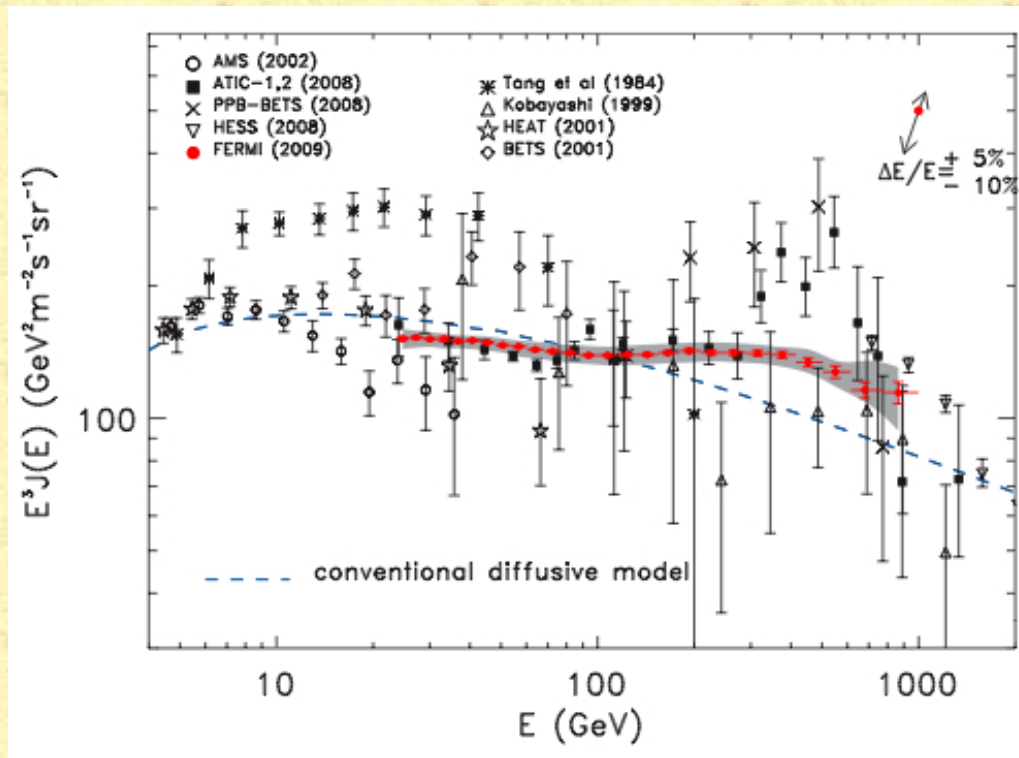
(Note that this can only be true at tree-level. Higher order corrections will inevitably lead to couplings to quarks).

- ❖ Leptophilic dark matter has been subject of much recent attention due to various observed anomalies in the cosmic ray positrons: **PAMELA**, **ATIC**, **Fermi**...
- ❖ These observations all suggest more **positrons** and **electrons** than can be readily accounted for.

# Positrons

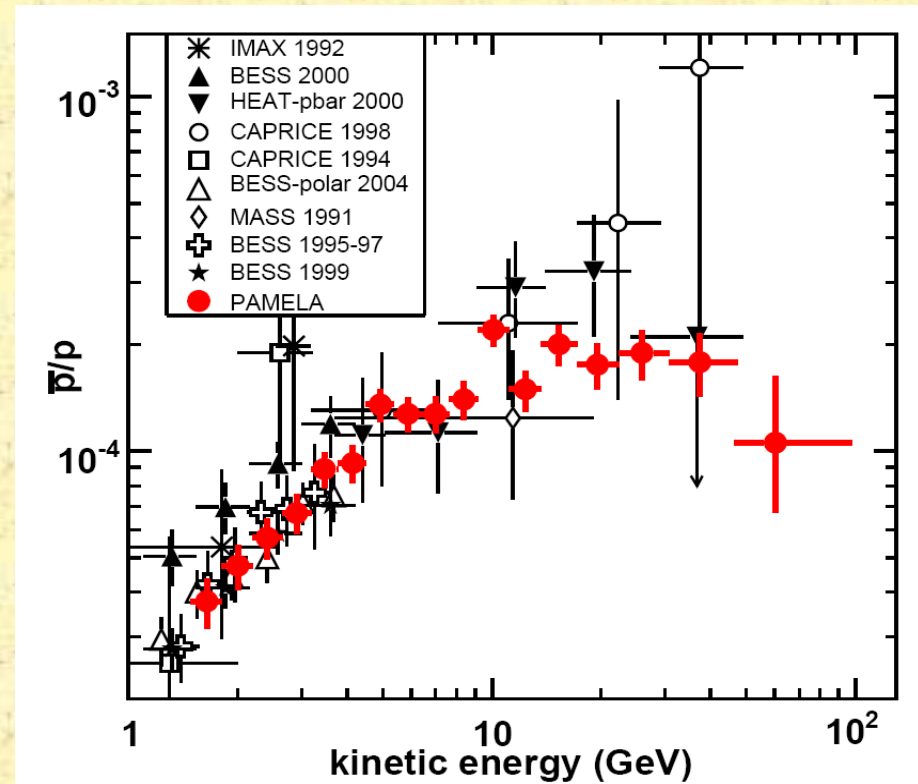
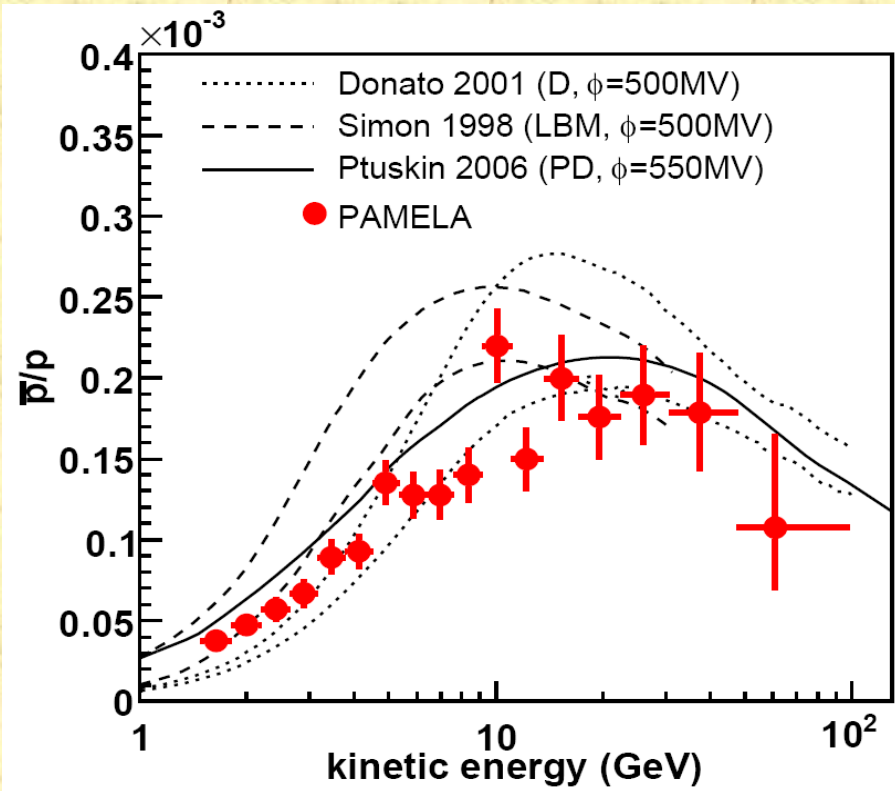


**PAMELA  $e^+$  excess**  
Nature 458, 607-609



**Fermi  $e^+e^-$  excess**  
Phys. Rev. Lett. 102, 181101 (2009)

# Antiprotons



Antiproton data consistent with theory expectation (for secondary production of antiprotons via cosmic ray propagation in the Galaxy).

# Solution of positron anomalies

## ❖ Positrons from astrophysics?

Re-examine the expected positron flux from:

- pulsars
- supernova remnants
- acceleration of secondary  $e^+$
- cosmic ray propagation

## ❖ Positrons from Dark Matter?

- Must produce enough  $e^+e^-$  without overproducing  $p\bar{p}$ .
- Need big cross sections!  
(Boost via DM clumping/substructure or enhanced cross sections → "Sommerfeld", non-thermal DM, ...)
- But annihilation to leptons is often suppressed.....

# Annihilation cross section

Parameterize the annihilation cross section as:

$$\langle \sigma v \rangle = a + bv^2 + \dots$$

**a** -- from s-wave ( $L=0$ ) annihilation

**b** -- both s-wave and p-wave ( $L=1$ ) contributions

The  $L^{\text{th}}$  partial wave contribution is suppressed as  $v^{2L}$

In galactic halos,  $v \sim 10^{-3}c$ , so only the s-wave contribution will be significant.

However, in many models, s-wave annihilation to a fermion pair is helicity suppressed by a factor of  $\left(m_f / m_{DM}\right)^2$

# Example: SUSY

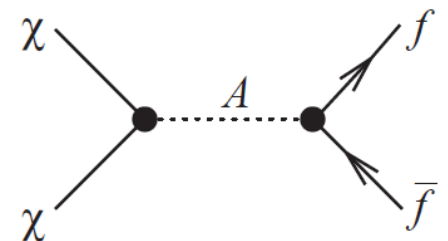
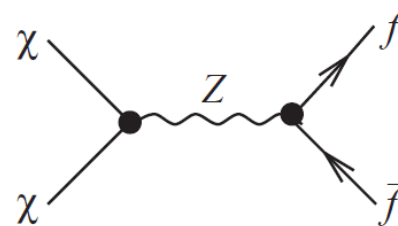
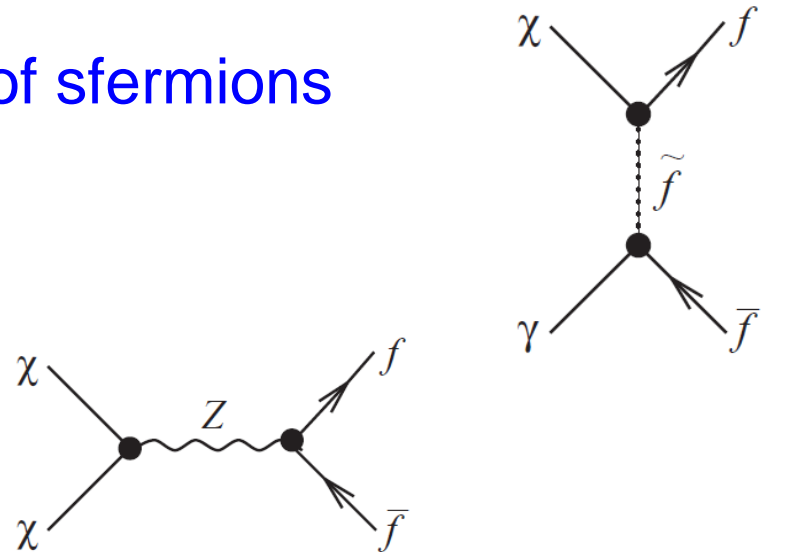
Majorana neutralinos annihilate to a fermion pair via:

- t- and u-channel exchange of sfermions  
→ helicity suppressed

- s-channel exchange of Z  
→ helicity suppressed

- s-channel exchange of higgs  
→ suppressed by yukawa couplings

$$\left(m_f / v_{\text{ev}}\right)^2$$



# When is annihilation suppressed?

❖ For s-channel annihilation:

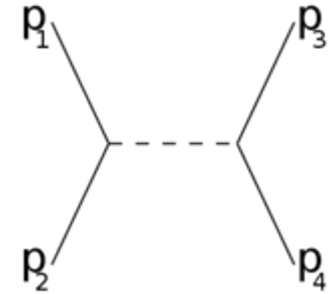
*Suppressed:* scalar  
axial-vector

*Non-suppressed:* pseudo-scalar

vector (not allowed for Majorana DM)

tensor (not allowed for Majorana DM)

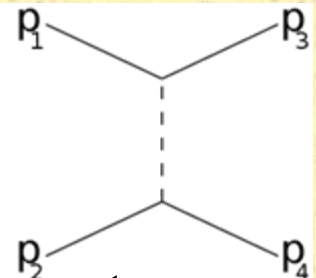
→ s-channel exchange of a pseudo-scalar is the sole non-suppressed mode for Majorana DM.



❖ What about t- and u-channel annihilation?

→ Fierz transform to s-channel form.

→ Non-suppressed only if a pseudo-scalar term present



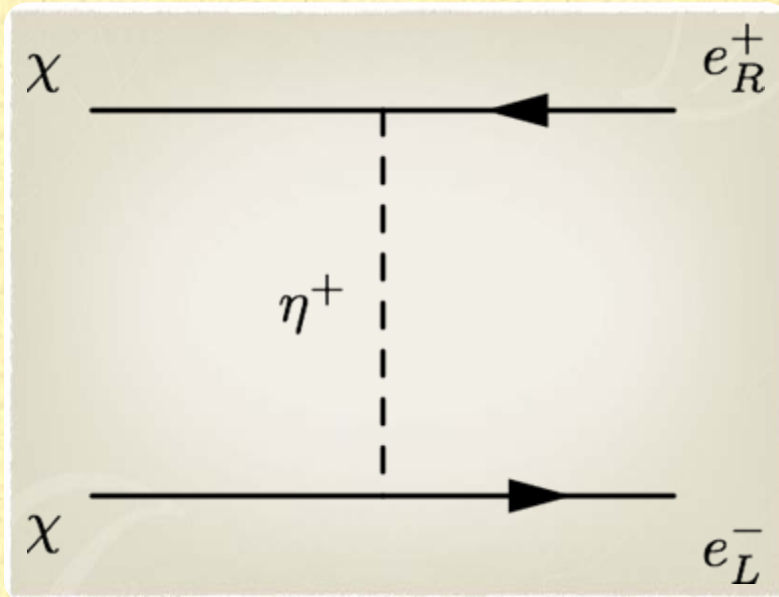


# Example: leptophilic model

❖ Cao, Ma, Shaughnessy, PLB 2009.

Dark matter = gauge-singlet Majorana fermion =  $\chi$

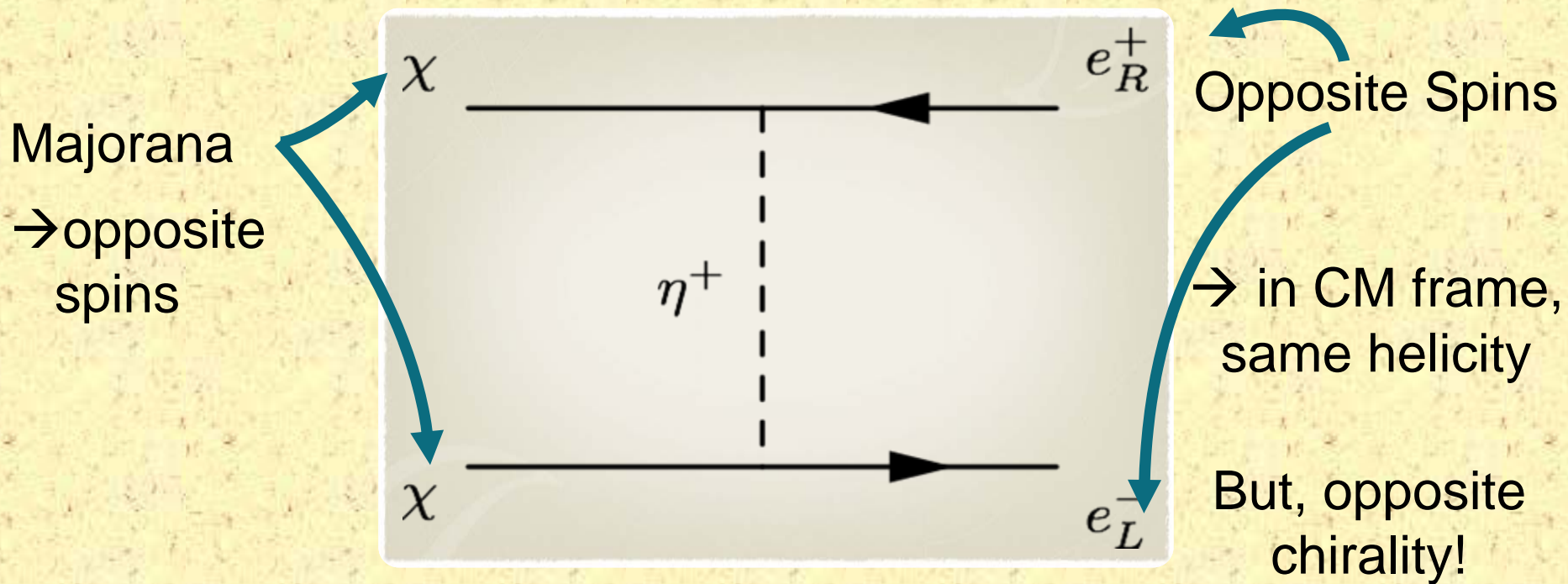
$$\mathcal{L} = f(\nu_L \eta^0 - \ell_L \eta^+) \chi + h.c.$$



Annihilation to leptons via t- and u-channel exchange of an SU(2) doublet scalar,  $\eta$ .

$$v \sigma = \frac{f^4 M_\chi^2}{16\pi M_\eta^4} \left[ \frac{m_l^2}{s} + \frac{2}{3} v^2 + \mathcal{O}(v^4) \right]$$

# Helicity suppression of s-wave



In massless limit, helicity = chirality, so

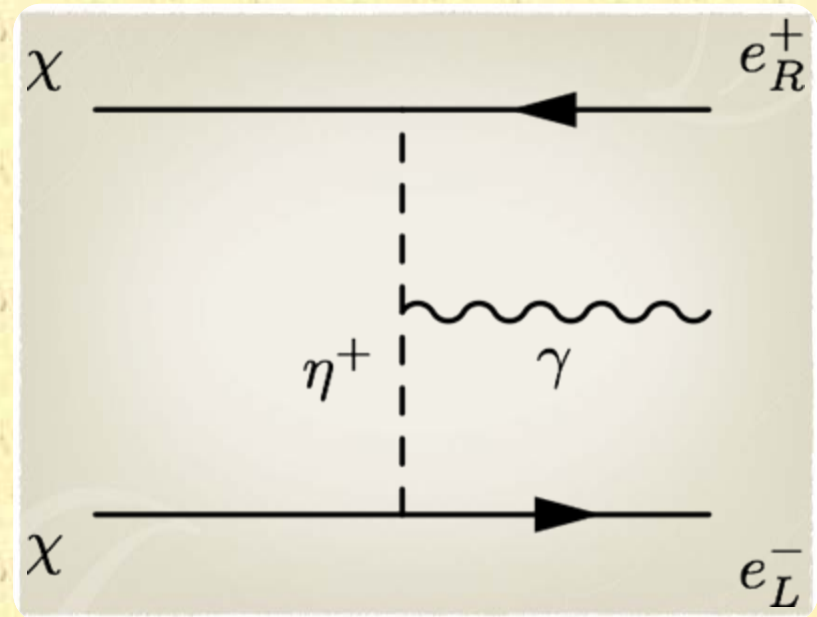
$$\langle \sigma v \rangle = \left( \frac{m_\ell}{E_\ell} \right)^2 a + bv^2$$

Heavily Suppressed!

# Lifting the suppression (photons)

Emission of a high energy photon from the propagator can lift this suppression:

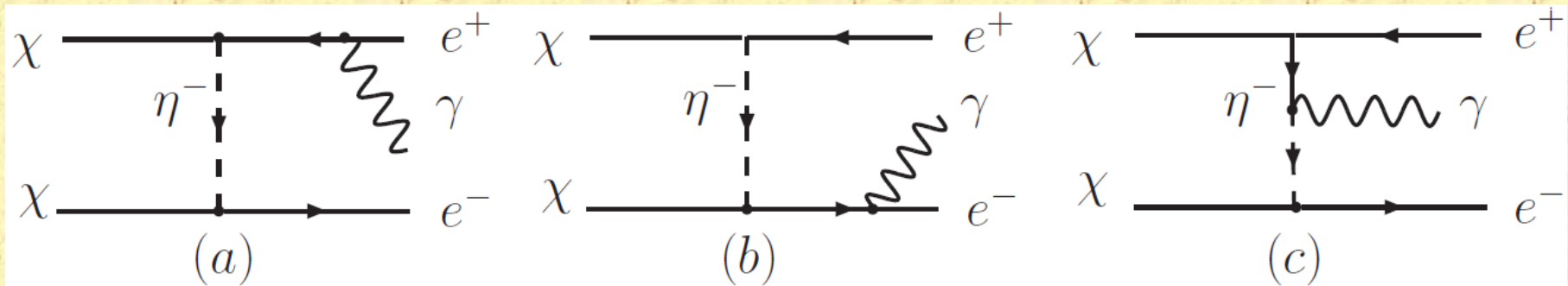
Bergstrom, PLB 225, 372 (1989);  
 Flores, Olive, Rudaz, PLB 232, 377 (1989);  
 Bringmann, Bergstrom, Edsjo, 2008);  
 Barger, Gao, Keung, Marfatia, 2009.



The photon carries away a unit of angular momentum  
 → no longer helicity suppressed.

$$\chi\chi \rightarrow f\bar{f}\gamma \gg \chi\chi \rightarrow f\bar{f}$$

# Lifting the suppression (photons)

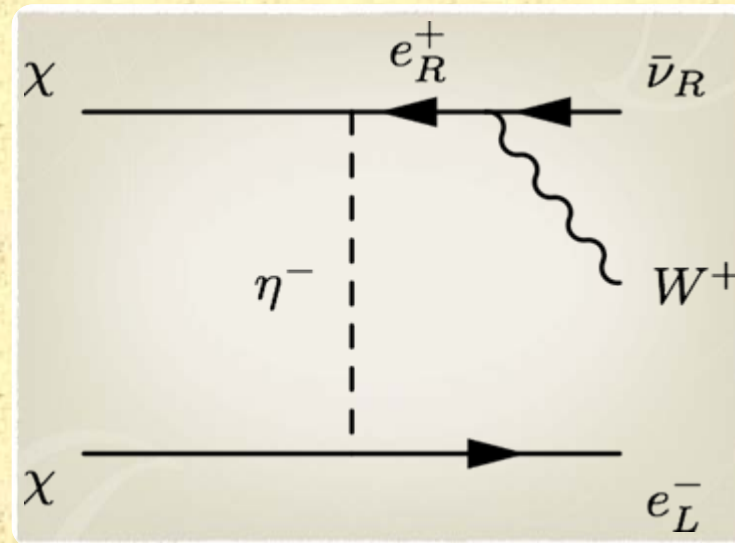


Final state radiation (FSR)

“Virtual internal  
bremsstrahlung”  
(VIB)

- ❖ FSR not effective in lifting suppression (soft/collinear)
  - ❖ VIB is effective in lifting suppression, but is suppressed by additional  $\eta$  propagator
- Large effect only for near-degenerate  $\chi$  and  $\eta$  masses.

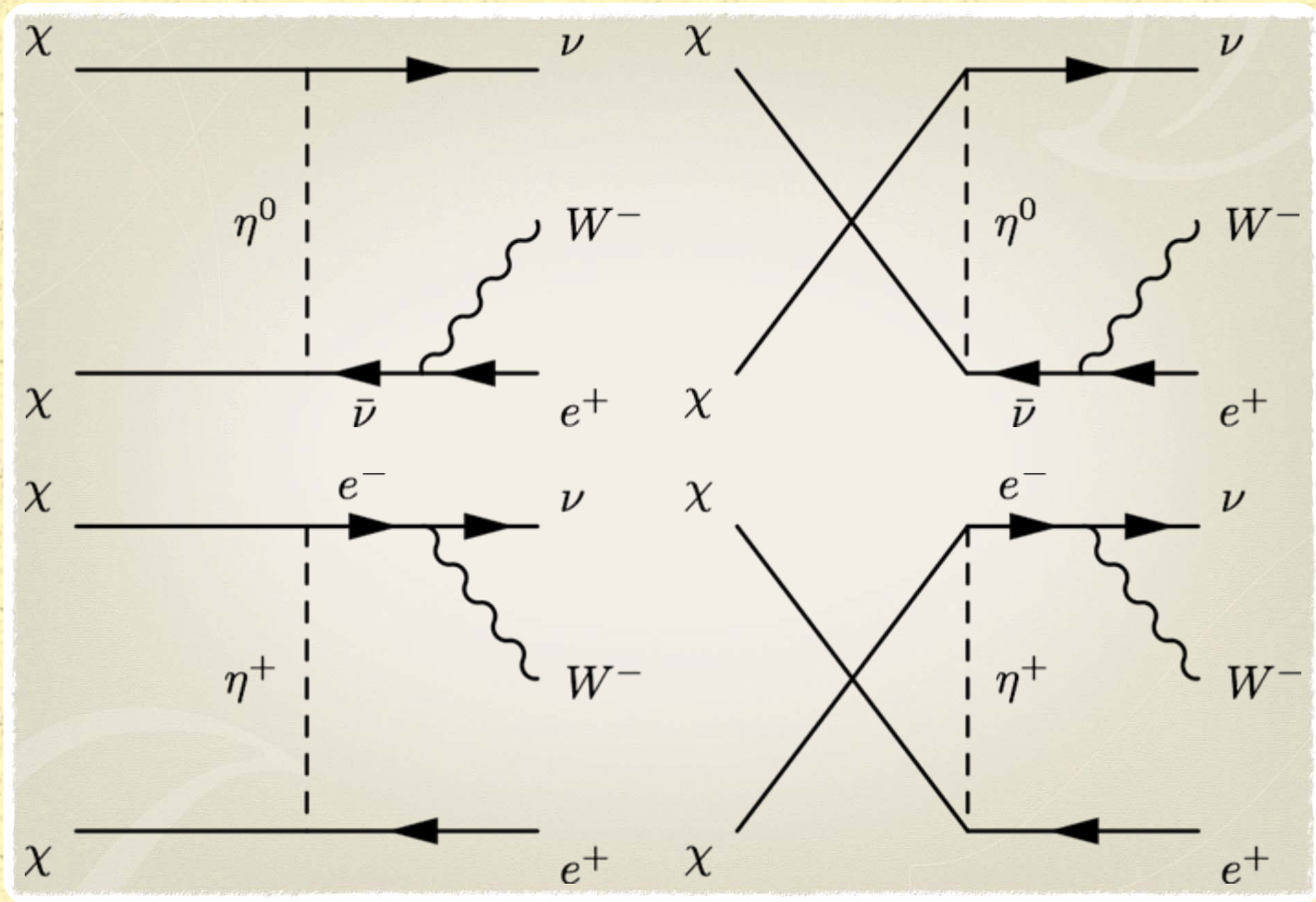
# Lifting suppression (electroweak brem.)<sup>13</sup>



Bell, Dent, Jacques  
& Weiler

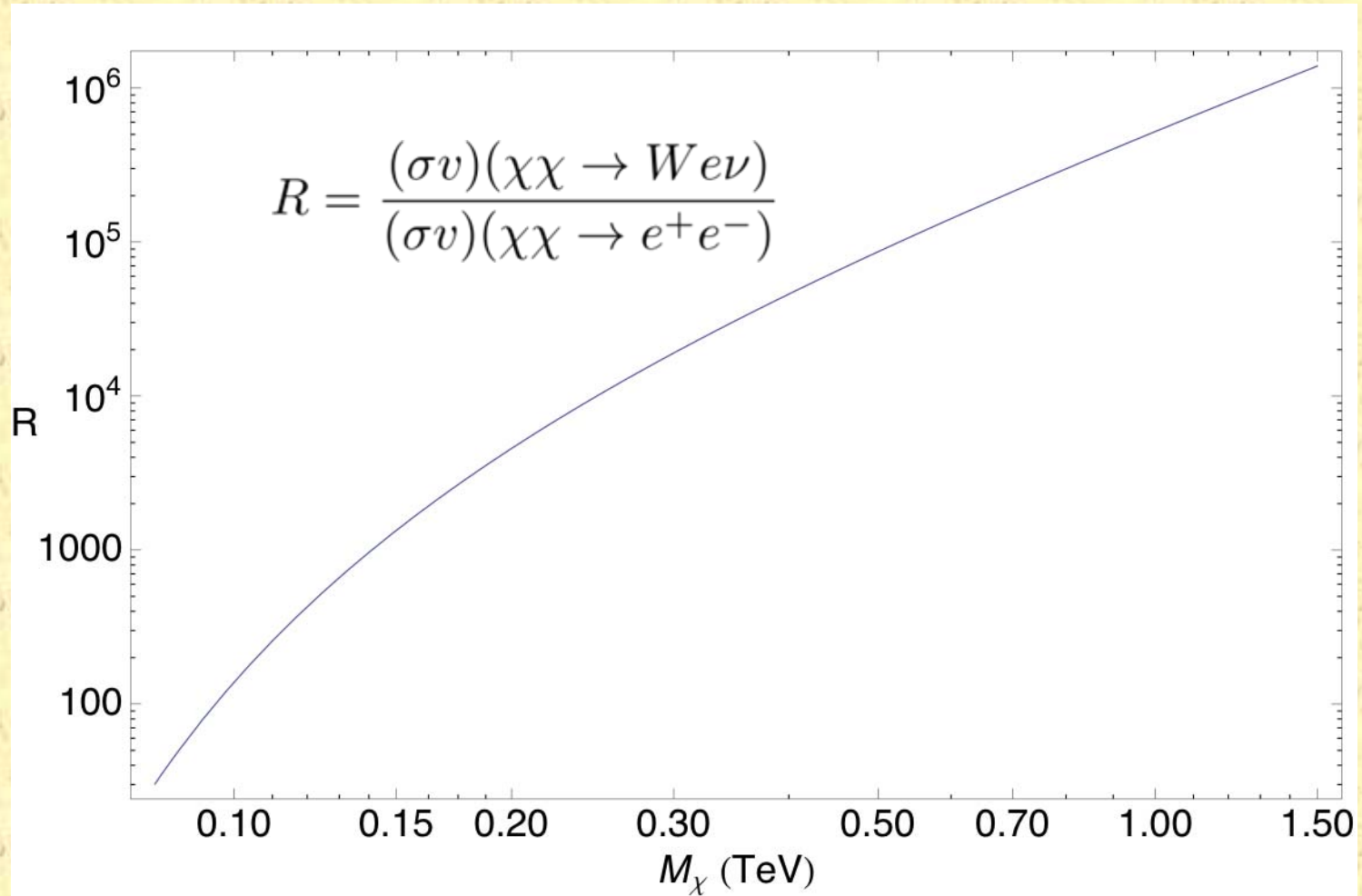
- ❖ Radiating a  $W$  or  $Z$  boson can also lift the suppression
- ❖ Radiation from a final state particle is sufficient  
(& radiation from propagator suppressed for heavy  $\eta$ )
- ❖ Don't need near-degenerate  $\chi$  and  $\eta$  masses
- ❖  $W$  and  $Z$  bosons decay to leptons, gamma, and hadrons  
→ hadron production even for leptophilic models

# Electroweak brem. diagrams



$$\chi\chi \rightarrow e\nu W$$

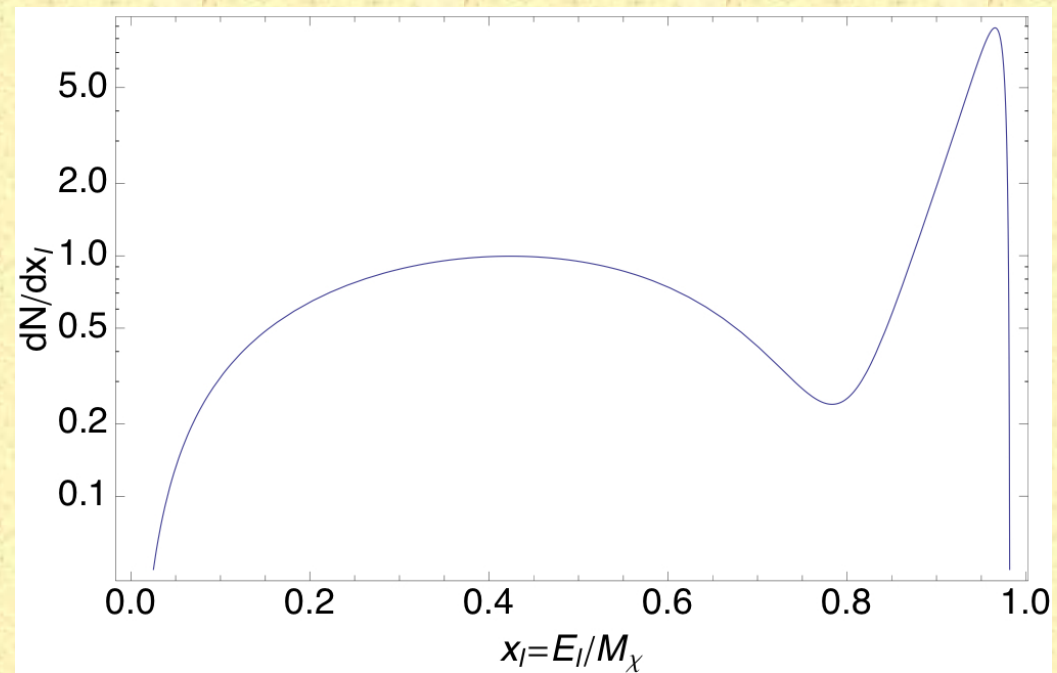
# Ratio of $e\nu W$ and $e^+e^-$ cross sections



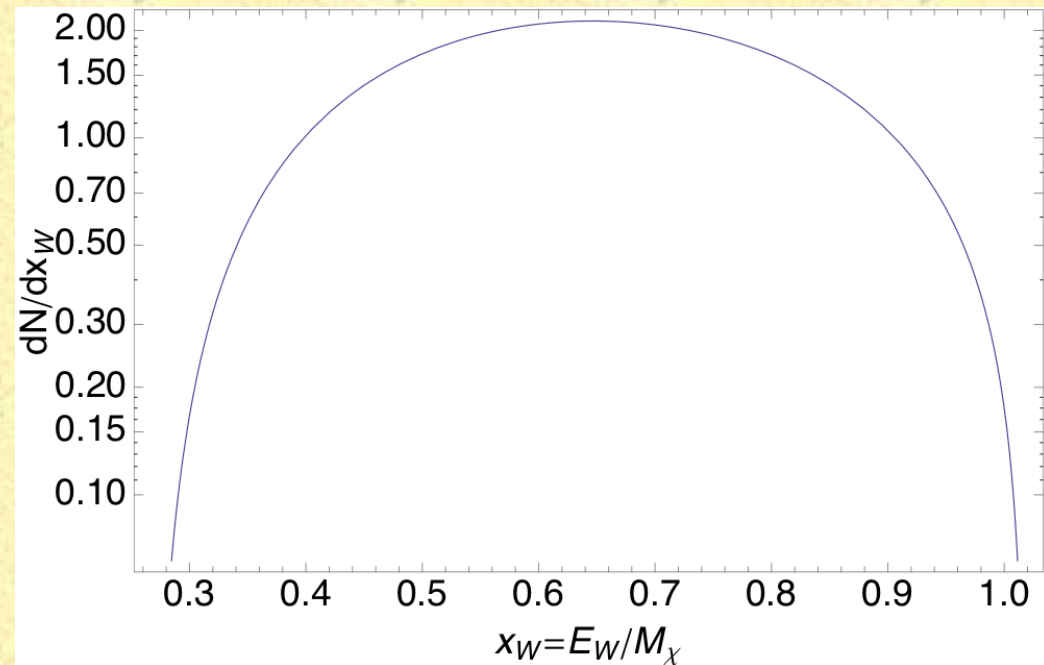
- Annihilation to  $e\nu W$  or  $e^+e^-Z$  dominates over  $e^+e^-$
- Enhancement by many orders of magnitude!

$$\chi\chi \rightarrow e\nu W$$

❖ lepton energy spectrum



❖ W energy spectrum





# Including the Z brem

W-brem and Z-brem cross sections related in simple way

$$\chi\chi \rightarrow e^+\nu W^-$$

$$\chi\chi \rightarrow e^-\bar{\nu}W^+$$

$$\chi\chi \rightarrow e^+e^-Z$$

$$\chi\chi \rightarrow \nu\bar{\nu}Z$$

$$v\sigma_{e^+e^-Z} = \frac{2(\sin^2\theta_W - \frac{1}{2})^2}{\cos^2\theta_W} \times v\sigma_{e^+\nu W^-} \Big|_{M_W \rightarrow M_Z}$$

$$\simeq 0.19 \times v\sigma_{e^+\nu W^-} \Big|_{M_W \rightarrow M_Z} \quad ($$

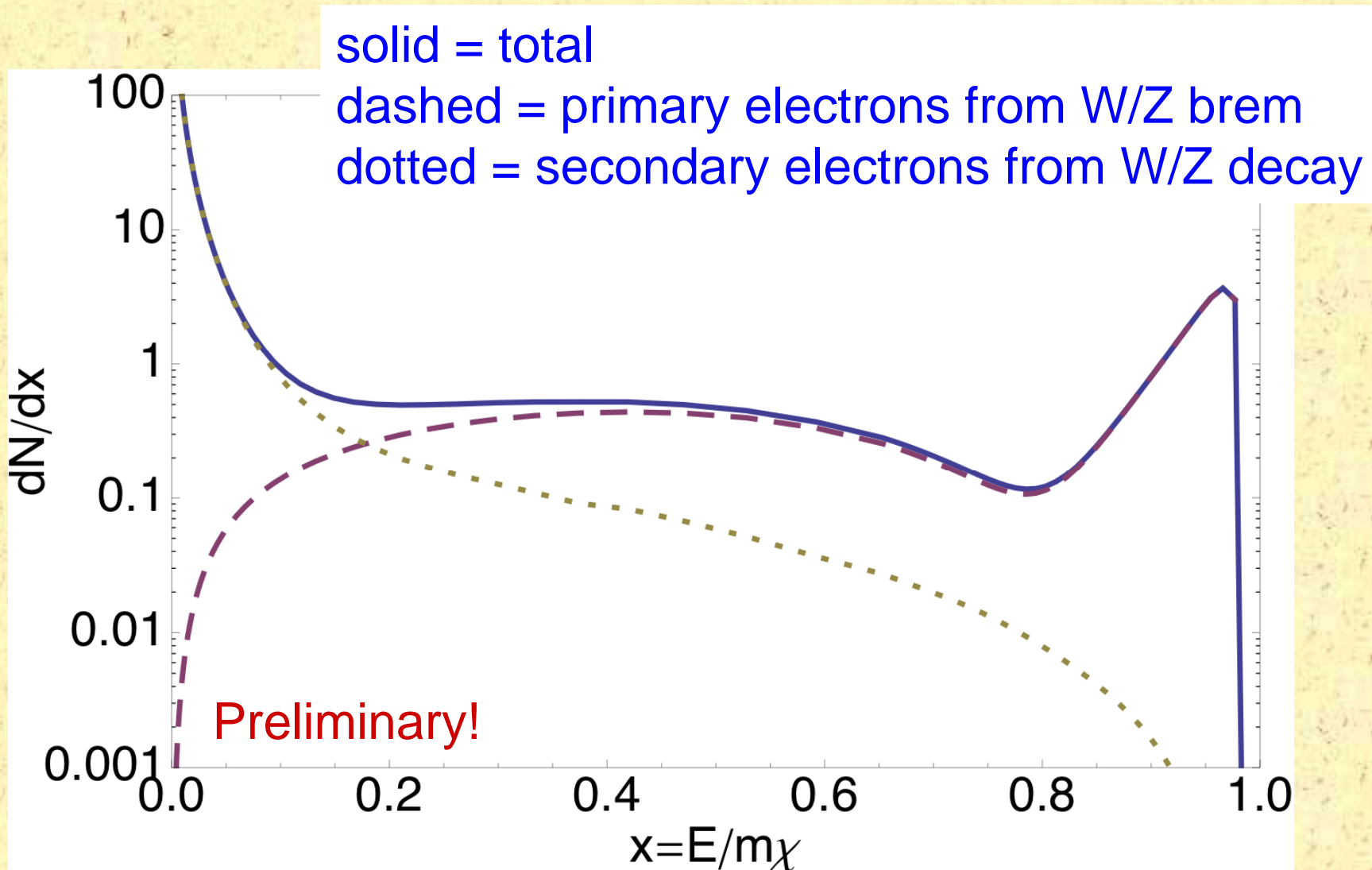
$$v\sigma_{\nu\bar{\nu}Z} = \frac{1}{(2\cos^2\theta_W)} \times v\sigma_{e^+\nu W^-} \Big|_{M_W \rightarrow M_Z}$$

$$\simeq 0.65 \times v\sigma_{e^+\nu W^-} \Big|_{M_W \rightarrow M_Z} \cdot$$

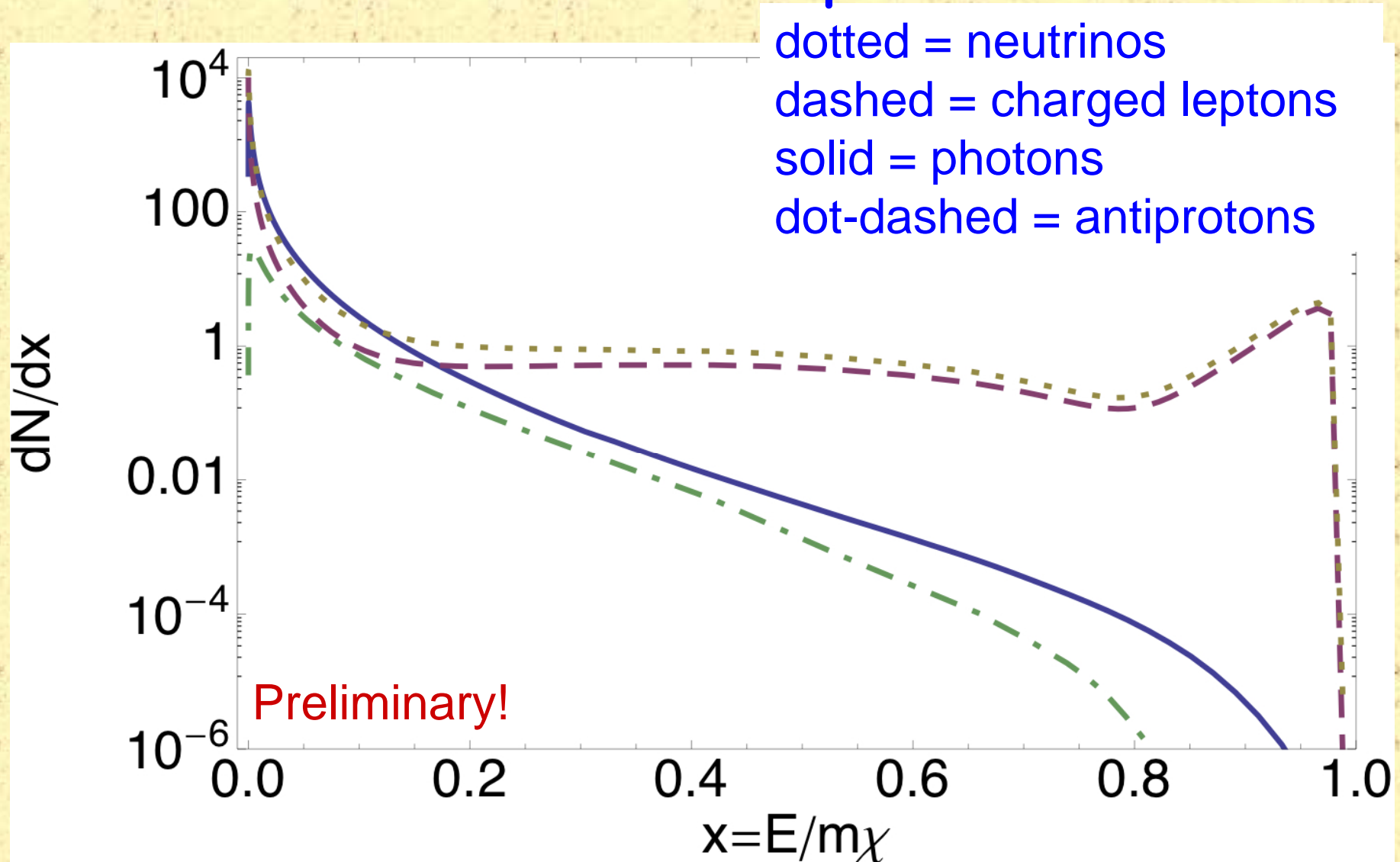
$$\langle\sigma v\rangle_{\text{Brem}} = \langle\sigma v\rangle_{e^+\nu W^-} + \langle\sigma v\rangle_{e^-\bar{\nu}W^+}$$

$$+ \langle\sigma v\rangle_{e^+e^-Z} + \langle\sigma v\rangle_{\nu\bar{\nu}Z}$$

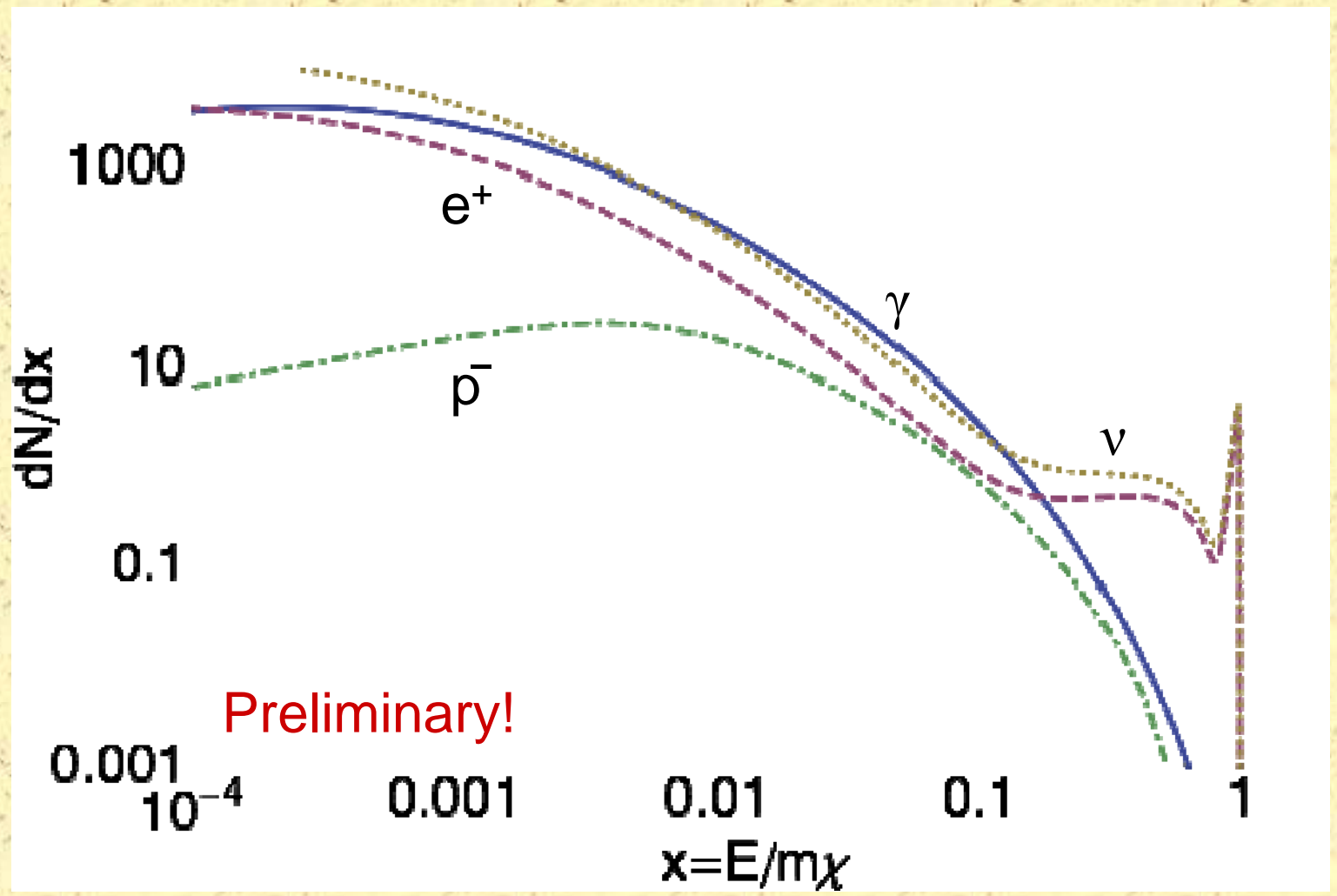
# Total electron energy spectrum



# Annihilation spectra

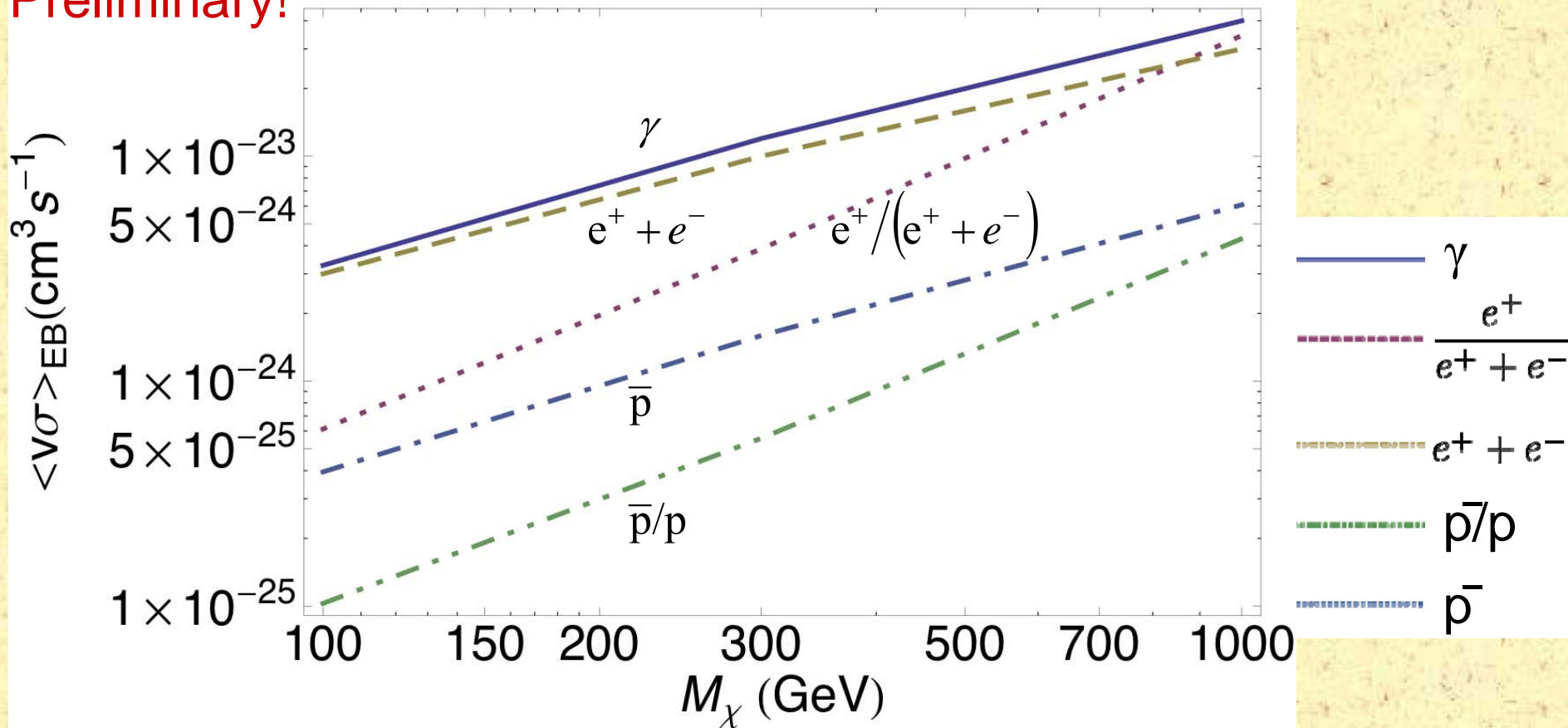


# Annihilation spectra



# Maximum allowed cross sections

Preliminary!



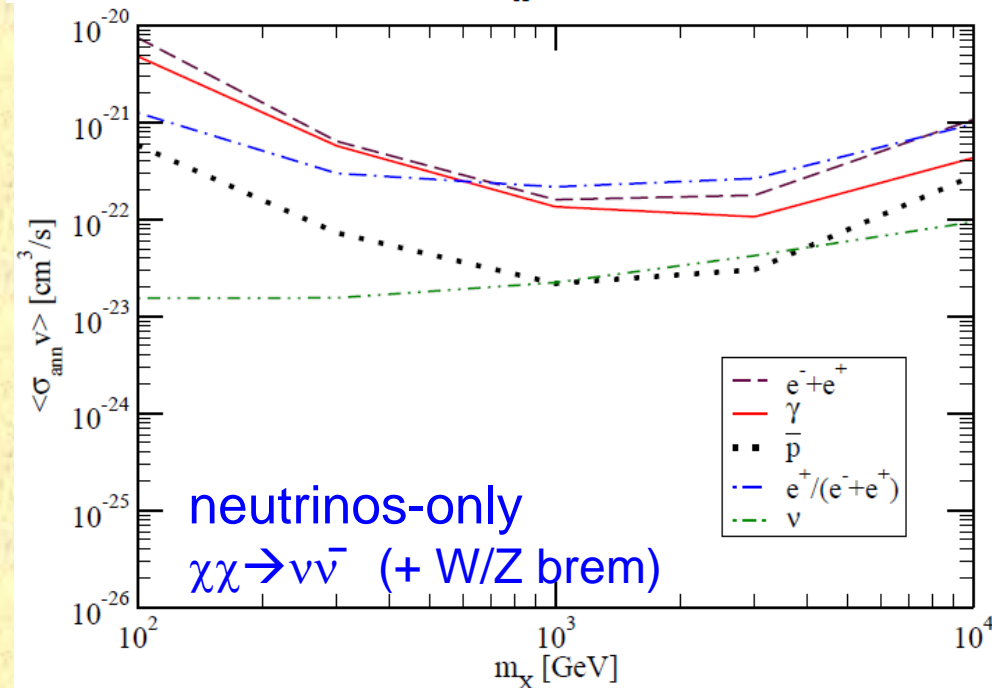
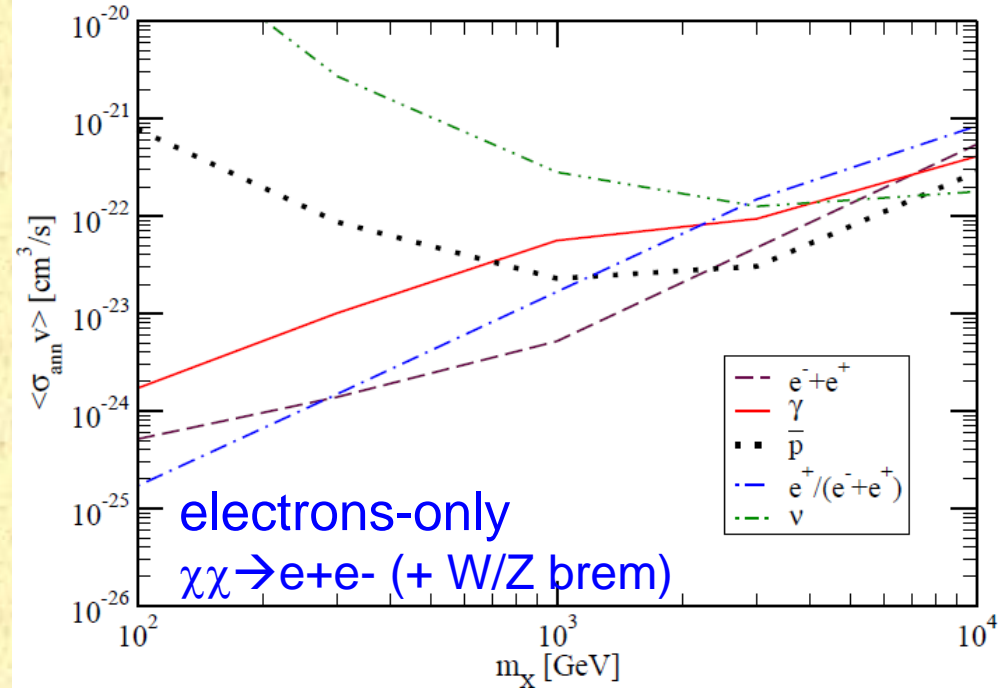
**→ Can't make significant contribution to  $e^+$  flux, without overproducing  $\bar{p}$ !**

## Models with no helicity suppression

→EW-brem still occurs, but is subdominant

→W/Z decays ensures there is at least a minimal yield of hadrons, photons, charged leptons and neutrinos.

Kachelriess, Serpico and Solberg  
arXiv:0911.0001



# Conclusions

## **Electroweak bremsstrahlung lifts helicity suppression → dominant annihilation channel**

- ❖  $e^+e^-Z$  and  $e\nu W$  rates dominate over  $e^+e^-$  by several orders of magnitude
- ❖ Allows indirect detection of processes that would otherwise be too suppressed to give observable signals
- ❖ Unavoidable hadronic component from  $W/Z$  decay
- ❖ Can't produce significant amount of  $e^+$  without overproducing antiprotons.

## **Even models where there is no suppression, purely leptonic annihilation products impossible**

NFB, J. B. Dent, T. D. Jacques and T. J. Weiler, arXiv:1009.2584

NFB, J. B. Dent, T. D. Jacques and T. J. Weiler, in preparation