

A Minimal Supersymmetric Cosmological Model

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COSMO/CosPA 2010

University of Tokyo

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EDS, M Kawasaki, T Yanagida [hep-ph/9603324](https://arxiv.org/abs/hep-ph/9603324)

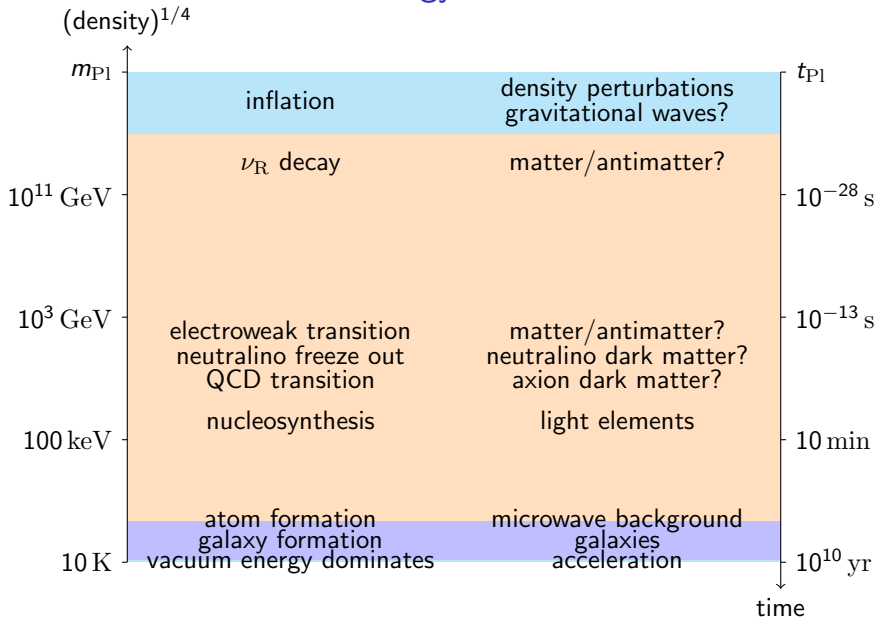
D Jeong, K Kadota, W-I Park, EDS [hep-ph/0406136](https://arxiv.org/abs/hep-ph/0406136)

G N Felder, H Kim, W-I Park, EDS [hep-ph/0703275](https://arxiv.org/abs/hep-ph/0703275)

R Easther, J T Giblin, E A Lim, W-I Park, EDS [arXiv:0801.4197](https://arxiv.org/abs/0801.4197)

S Kim, W-I Park, EDS [arXiv:0807.3607](https://arxiv.org/abs/0807.3607)

Standard model of cosmology



Moduli and gravitinos

Moduli are cosmologically dangerous. Nucleosynthesis constrains

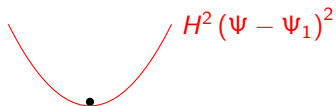
$$\frac{n}{s} \lesssim 10^{-12} \text{ to } 10^{-15}$$

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In the early universe

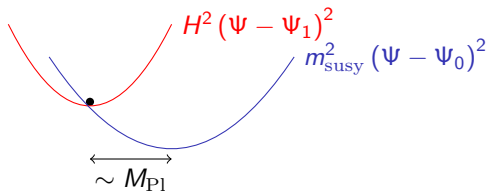

$$H^2 (\Psi - \Psi_1)^2$$

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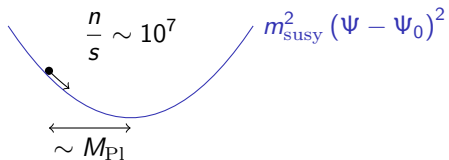


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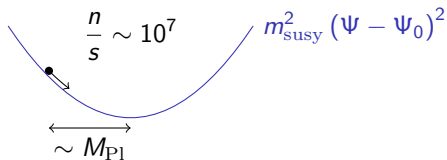


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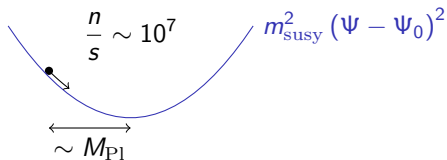
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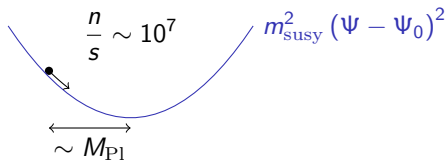
slow-roll inflation: $H \gtrsim m_{\text{inflaton}} \gtrsim m_{\text{susy}}$

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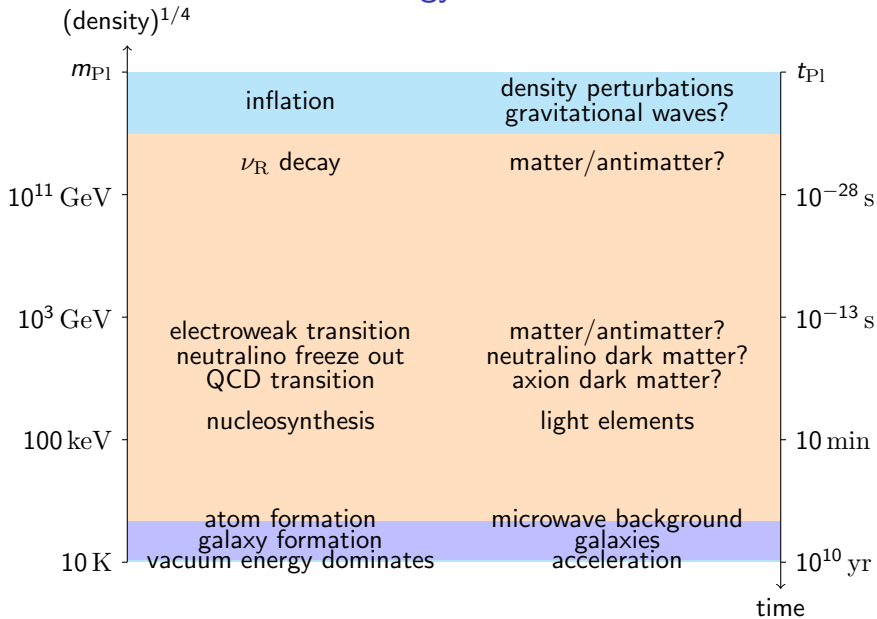


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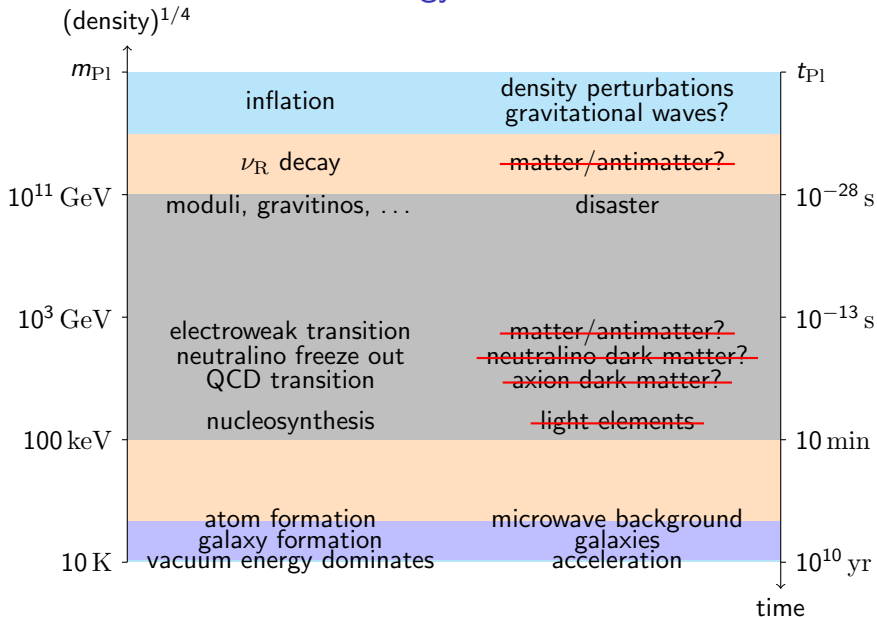
after

slow-roll inflation: $H \gtrsim m_{\text{inflaton}} \gtrsim m_{\text{susy}}$

Standard model of cosmology



Standard model of cosmology



Minimal Supersymmetric Standard Model

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \mu H_u H_d$$

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But

- ▶ μ ?
- ▶ neutrino masses?
- ▶ strong CP ?

Minimal Supersymmetric Cosmological Model

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

Minimal Supersymmetric Cosmological Model

MSSM

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

Minimal Supersymmetric Cosmological Model

MSSM

neutrino masses

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Minimal Supersymmetric Cosmological Model

MSSM

neutrino masses

MSSM μ -term

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

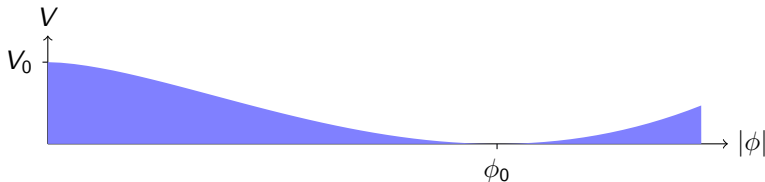
$$\mu = \lambda_\mu \phi_0^2$$

Minimal Supersymmetric Cosmological Model

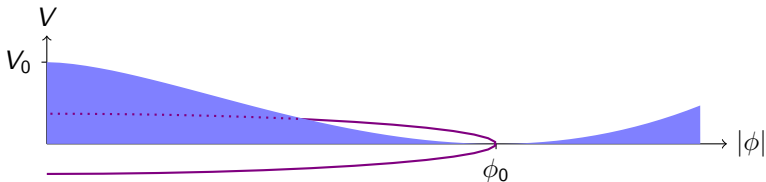
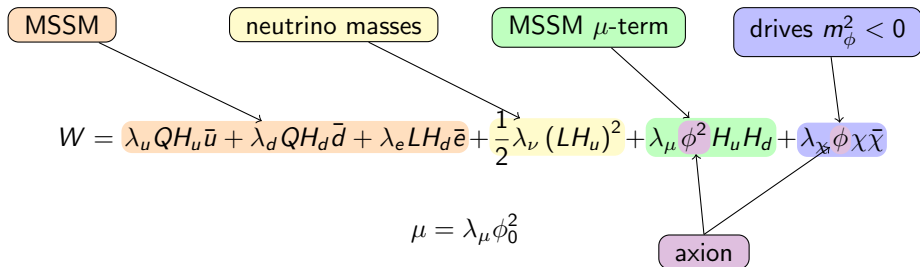


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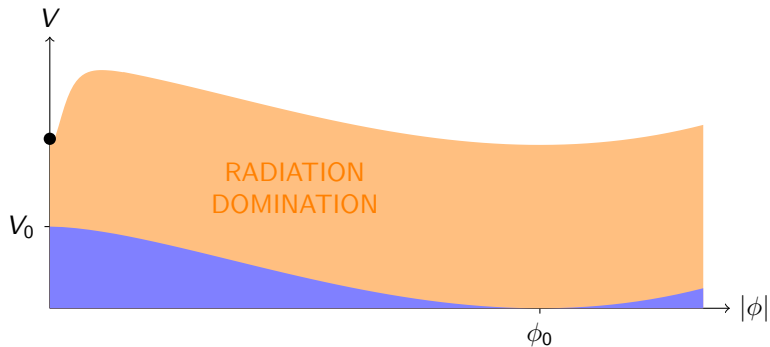
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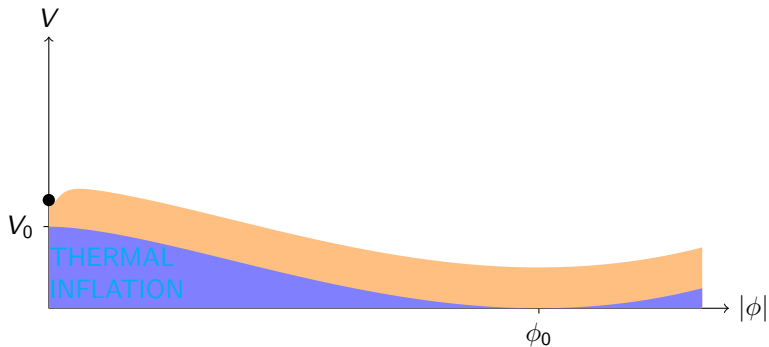
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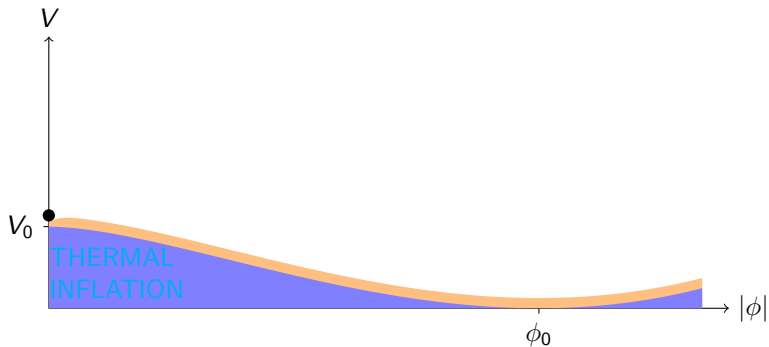
Thermal inflation



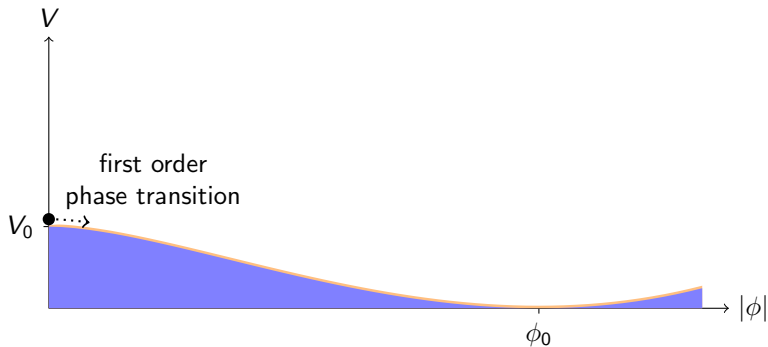
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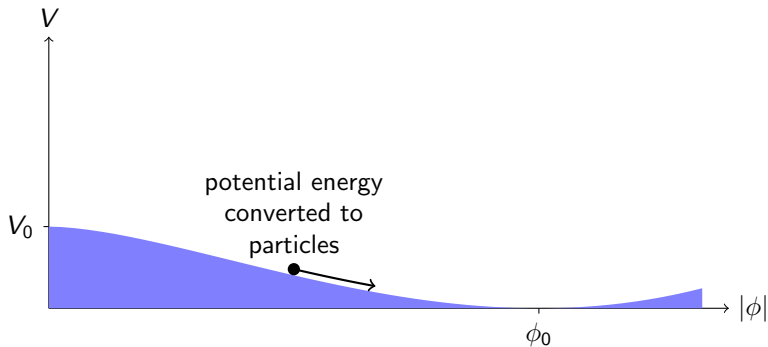
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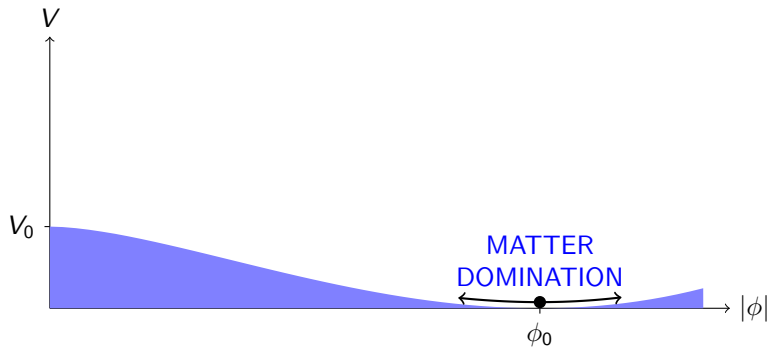
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Key properties of thermal inflation

For

$$\phi_0 \sim 10^{10} \text{ to } 10^{12} \text{ GeV}$$

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$$N \sim 10 \implies \begin{array}{l} \text{primordial perturbations} \\ \text{from slow-roll inflation} \\ \text{preserved on large scales} \end{array}$$

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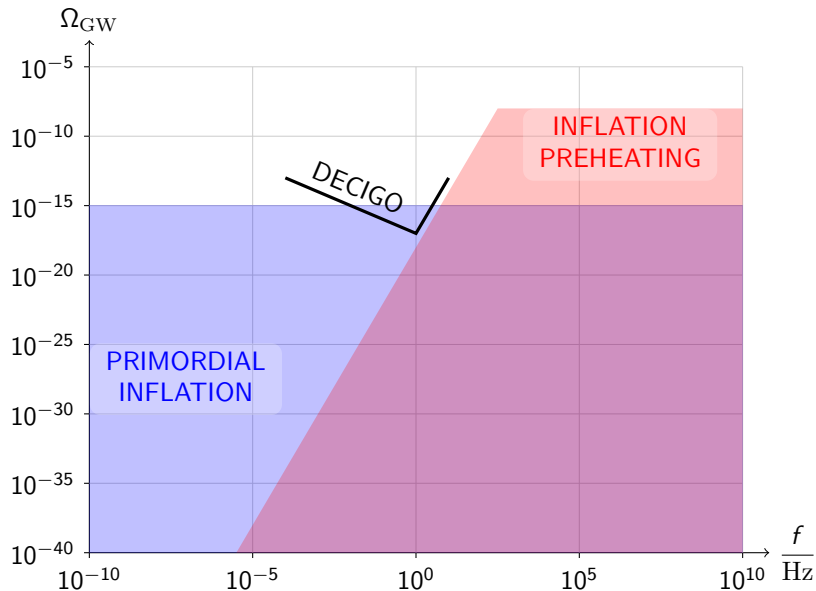
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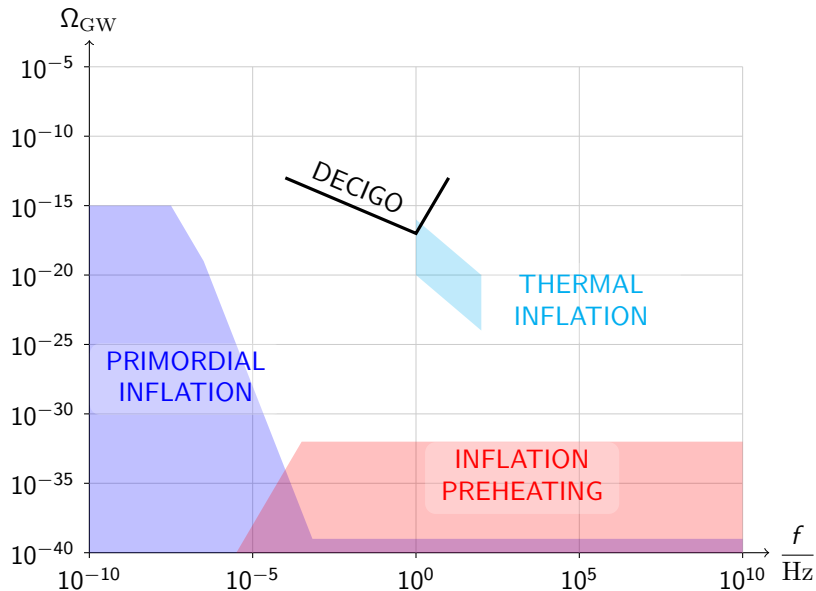
Low energy scale

$$V_0^{1/4} \sim 10^6 \text{ to } 10^7 \text{ GeV} \implies \begin{array}{l} \text{moduli regenerated with} \\ \text{sufficiently small abundance} \end{array}$$

Gravitational waves



Gravitational waves



Baryogenesis

Key assumption

$$m_{LH_u}^2 = \frac{1}{2} (m_L^2 + m_{H_u}^2) < 0$$

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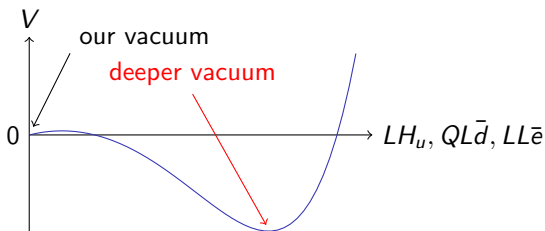
Implies a dangerous **non-MSSM vacuum** with

$$LH_u \sim (10^9 \text{ GeV})^2$$

and

$$\lambda_d QL\bar{d} + \lambda_e LL\bar{e} = \mu LH_u$$

eliminating the μ -term contribution to LH_u 's mass squared.



Reduction

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

Reduction

$$W = \lambda_u Q H_u \bar{u} + \lambda_d Q H_d \bar{d} + \lambda_e L H_d \bar{e} + \frac{1}{2} \lambda_\nu (L H_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

$$L = \begin{pmatrix} I \\ e/\sqrt{2} \end{pmatrix}, \quad H_u = \begin{pmatrix} 0 \\ h_u \end{pmatrix}, \quad H_d = \begin{pmatrix} h_d \\ 0 \end{pmatrix}, \quad \bar{e} = (e/\sqrt{2})$$

$$\bar{u} = (0 \ 0 \ 0) , \quad Q = \begin{pmatrix} 0 & 0 & 0 \\ d/\sqrt{2} & 0 & 0 \end{pmatrix}, \quad \bar{d} = (d/\sqrt{2} \ 0 \ 0)$$

$$\phi = \phi, \quad \chi = 0, \quad \bar{\chi} = 0$$

Potential

$$\begin{aligned} & V_0 + m_L^2 |l|^2 - m_{H_u}^2 |h_u|^2 + m_{H_d}^2 |h_d|^2 + m_d^2 |d|^2 + m_e^2 |e|^2 - m_\phi^2 |\phi|^2 \\ & + \left[\frac{1}{2} A_\nu \lambda_\nu l^2 h_u^2 - \frac{1}{2} A_d \lambda_d h_d d^2 - \frac{1}{2} A_e \lambda_e h_d e^2 - A_\mu \lambda_\mu \phi^2 h_u h_d + \text{c.c.} \right] \\ & + |\lambda_\nu l h_u^2|^2 + |\lambda_\nu l^2 h_u - \lambda_\mu \phi^2 h_d|^2 + \left| \lambda_\mu \phi^2 h_u + \frac{1}{2} \lambda_d d^2 + \frac{1}{2} \lambda_e e^2 \right|^2 \\ & \quad + |\lambda_d h_d d|^2 + |\lambda_e h_d e|^2 + |2\lambda_\mu \phi h_u h_d|^2 \\ & \quad + \frac{1}{2} g^2 \left(|h_u|^2 - |h_d|^2 - |l|^2 + \frac{1}{2} |d|^2 + \frac{1}{2} |e|^2 \right)^2 \end{aligned}$$

Potential

drives thermal inflation

$$\begin{aligned} V_0 &+ m_L^2 |l|^2 - m_{H_u}^2 |h_u|^2 + m_{H_d}^2 |h_d|^2 + m_d^2 |d|^2 + m_e^2 |e|^2 - m_\phi^2 |\phi|^2 \\ &+ \left[\frac{1}{2} A_\nu \lambda_\nu l^2 h_u^2 - \frac{1}{2} A_d \lambda_d h_d d^2 - \frac{1}{2} A_e \lambda_e h_d e^2 - A_\mu \lambda_\mu \phi^2 h_u h_d + \text{c.c.} \right] \\ &+ |\lambda_\nu l h_u^2|^2 + |\lambda_\nu l^2 h_u - \lambda_\mu \phi^2 h_d|^2 + \left| \lambda_\mu \phi^2 h_u + \frac{1}{2} \lambda_d d^2 + \frac{1}{2} \lambda_e e^2 \right|^2 \\ &\quad + |\lambda_d h_d d|^2 + |\lambda_e h_d e|^2 + |2\lambda_\mu \phi h_u h_d|^2 \\ &\quad + \frac{1}{2} g^2 \left(|h_u|^2 - |h_d|^2 - |l|^2 + \frac{1}{2} |d|^2 + \frac{1}{2} |e|^2 \right)^2 \end{aligned}$$

Potential

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h_u rolls away

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lh_u stabilized
with
fixed phase

Potential

drives thermal inflation

h_u rolls away

ϕ rolls away

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 & \quad + |\lambda_d h_d d|^2 + |\lambda_e h_d e|^2 + |2\lambda_\mu \phi h_u h_d|^2 \\
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h_u stabilized
with
fixed phase

h_d forced out

Potential

drives thermal inflation

h_u rolls away

ϕ rolls away

$$\begin{aligned}
 & V_0 + m_L^2 |l|^2 - m_{H_u}^2 |h_u|^2 + m_{H_d}^2 |h_d|^2 + \cancel{m_d^2 |d|^2} + \cancel{m_e^2 |e|^2} - m_\phi^2 |\phi|^2 \\
 & + \left[\frac{1}{2} A_\nu \lambda_\nu l^2 h_u^2 - \frac{1}{2} A_d \lambda_d h_d d^2 - \frac{1}{2} A_e \lambda_e h_d e^2 - A_\mu \lambda_\mu \phi^2 h_u h_d + \text{c.c.} \right] \\
 & + |\lambda_\nu |h_u|^2|^2 + |\lambda_\nu l^2 h_u - \lambda_\mu \phi^2 h_d|^2 + \left| \lambda_\mu \phi^2 h_u + \frac{1}{2} \lambda_d d^2 + \frac{1}{2} \lambda_e e^2 \right|^2 \\
 & + |\lambda_d h_d d|^2 + |\lambda_e h_d e|^2 + |2\lambda_\mu \phi h_u h_d|^2 \\
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 \end{aligned}$$

h_u stabilized with fixed phase

d and e held at origin

h_d forced out

Potential

drives thermal inflation

lh_u rolls away

ϕ rolls away

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 & V_0 + m_L^2 |l|^2 - m_{H_u}^2 |h_u|^2 + m_{H_d}^2 |h_d|^2 + \cancel{m_d^2 |d|^2} + \cancel{m_e^2 |e|^2} - m_\phi^2 |\phi|^2 \\
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 & + |\lambda_\nu l h_u^2|^2 + |\lambda_\nu l^2 h_u - \lambda_\mu \phi^2 h_d|^2 + |\lambda_\mu \phi^2 h_u + \frac{1}{2} \lambda_d d^2 - \frac{1}{2} \lambda_e e^2|^2 \\
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 \end{aligned}$$

lh_u stabilized with fixed phase

d and e held at origin

lh_u returns with rotation

h_d forced out

Potential

drives thermal inflation

lh_u rolls away

ϕ rolls away
 ϕ stabilized
 $m_\phi^2(\phi_0) = -\alpha_\phi m_\phi^2(0)$

$$V_0 + m_L^2 |l|^2 - m_{H_u}^2 |h_u|^2 + m_{H_d}^2 |h_d|^2 + \cancel{m_d^2 |d|^2} + \cancel{m_e^2 |e|^2} + m_\phi^2(\phi) |\phi|^2$$

$$+ \left[\frac{1}{2} A_\nu \lambda_\nu l^2 h_u^2 - \frac{1}{2} A_d \lambda_d h_d d^2 - \frac{1}{2} A_e \lambda_e h_d e^2 - A_\mu \lambda_\mu \phi^2 h_u h_d + \text{c.c.} \right]$$

$$+ |\lambda_\nu l h_u^2|^2 + |\lambda_\nu l^2 h_u - \lambda_\mu \phi^2 h_d|^2 + |\lambda_\mu \phi^2 h_u + \frac{1}{2} \lambda_d d^2 - \frac{1}{2} \lambda_e e^2|^2$$

$$+ |\lambda_d h_d d|^2 + |\lambda_e h_d e|^2 + |2\lambda_\mu \phi h_u h_d|^2$$

$$+ \frac{1}{2} g^2 \left(|h_u|^2 - |h_d|^2 - |l|^2 + \frac{1}{2} |d|^2 - \frac{1}{2} |e|^2 \right)^2$$

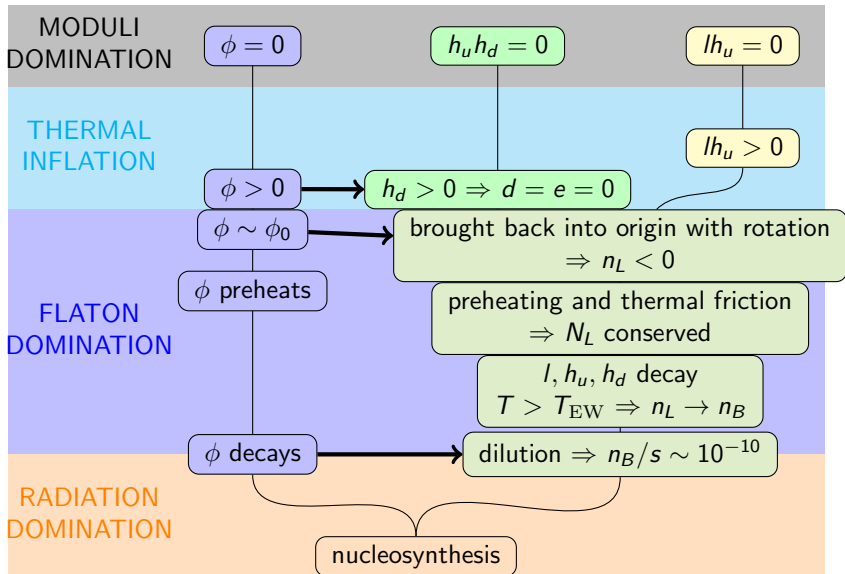
lh_u stabilized with fixed phase

d and e held at origin

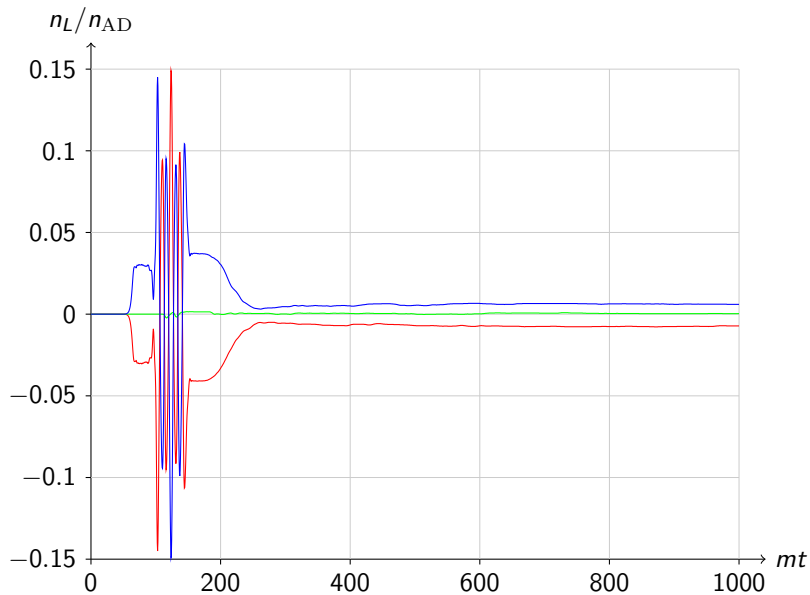
lh_u returns with rotation

h_d forced out

Baryogenesis



Numerical simulation



Baryon asymmetry

$$\frac{n_B}{s} \sim \frac{n_L}{n_{\text{AD}}} \frac{n_{\text{AD}}}{n_\phi} \frac{T_d}{m_\phi(\phi_0)}$$

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Using

$$n_\phi \sim m_\phi(\phi_0) \phi_0^2 \quad , \quad m_\phi^2(\phi_0) \sim \alpha_\phi m_\phi^2(0) \quad , \quad n_{AD} \sim m_{LH_u} l_0^2$$

$$l_0 \sim 10^9 \text{ GeV} \sqrt{\left(\frac{10^{-2} \text{ eV}}{m_\nu}\right) \left(\frac{m_{LH_u}}{\text{TeV}}\right)}$$

$$T_d \sim 1 \text{ GeV} \left(\frac{10^{12} \text{ GeV}}{\phi_0}\right) \left(\frac{|\mu|}{\text{TeV}}\right)^2$$

gives

$$\frac{n_B}{s} \sim 10^{-10} \left(\frac{n_L/n_{AD}}{10^{-2}}\right) \left(\frac{10^{12} \text{ GeV}}{\phi_0}\right)^3 \left(\frac{10^{-2} \text{ eV}}{m_\nu}\right) \left(\frac{|\mu|}{\text{TeV}}\right)^2 \left(\frac{10^{-1}}{\alpha_\phi}\right) \left(\frac{m_{LH_u}}{m_\phi(0)}\right)^2$$

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which suggests

$$\phi_0 \sim 10^{12} \text{ GeV}$$

Dark matter candidates

Peccei-Quinn symmetry

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

Dark matter candidates

Peccei-Quinn symmetry

DFSZ axion

$$W = \lambda_u QH_u \bar{u} + \lambda_d QH_d \bar{d} + \lambda_e LH_d \bar{e} + \frac{1}{2} \lambda_\nu (LH_u)^2 + \lambda_\mu \phi^2 H_u H_d + \lambda_\chi \phi \chi \bar{\chi}$$

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DFSZ axion

KSVZ axion

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Axion

$$m_a \sim \frac{\Lambda_{\text{QCD}}^2}{f_a} \quad \text{where } f_a = \frac{\sqrt{2} \phi_0}{N}$$
$$\simeq 6.2 \times 10^{-6} \text{ eV} \left(\frac{10^{12} \text{ GeV}}{f_a} \right)$$

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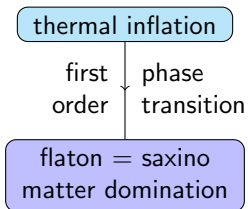
Axino

$$m_{\tilde{a}} = \frac{1}{16\pi^2} \sum_{\chi} \lambda_{\chi}^2 A_{\chi}$$
$$\sim 1 \text{ to } 10 \text{ GeV}$$

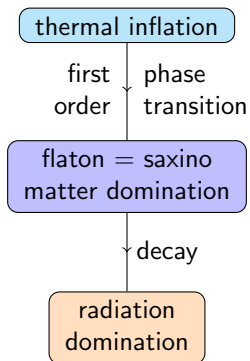
Dark matter genesis

thermal inflation

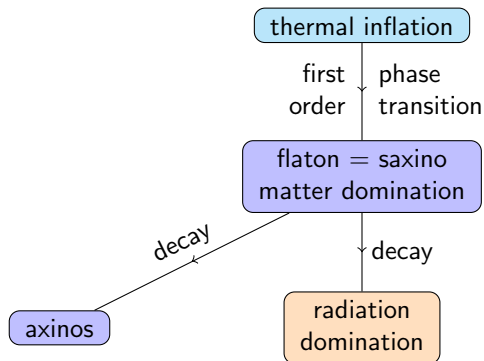
Dark matter genesis



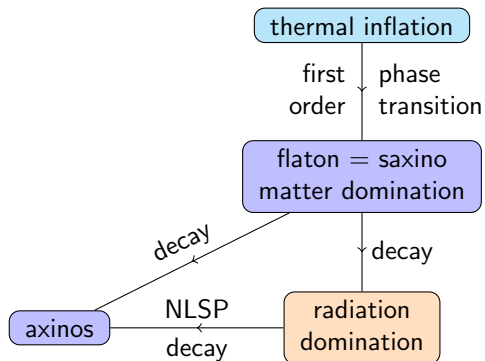
Dark matter genesis



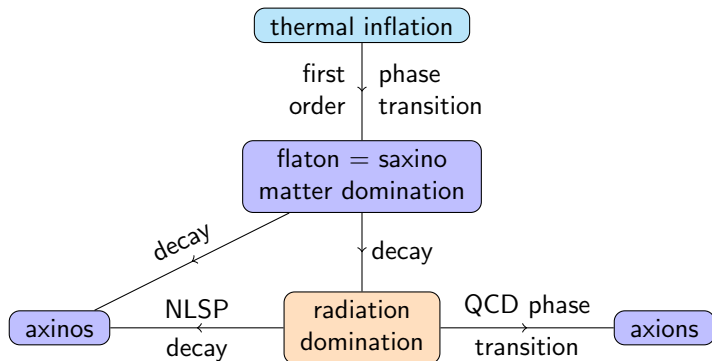
Dark matter genesis



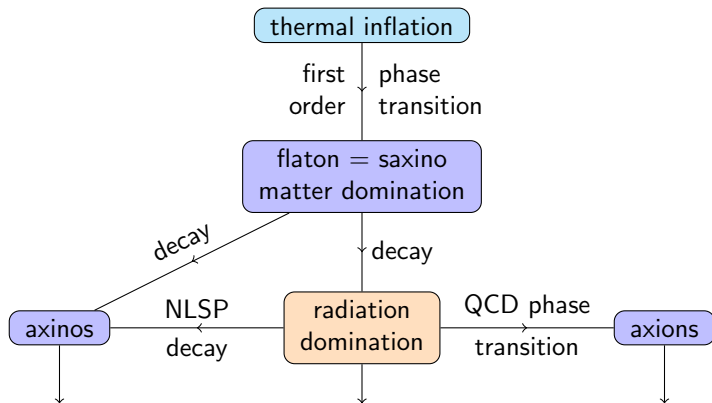
Dark matter genesis



Dark matter genesis



Dark matter genesis



Dark matter abundance

Axion

Axino

Dark matter abundance

Axion Misalignment

$$\Omega_a \sim 3 \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{1.2}$$

Axino

Dark matter abundance

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Axino Flaton decay

$$\Omega_{\tilde{a}} \simeq 0.04 \left(\frac{\alpha_{\tilde{a}}}{10^{-1}} \right)^2 \left(\frac{m_{\tilde{a}}}{1 \text{ GeV}} \right)^3 \left(\frac{10^{12} \text{ GeV}}{\phi_0} \right)^2 \left(\frac{1 \text{ GeV}}{T_d} \right)$$

Dark matter abundance

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Thermal NLSP decay

$$\Omega_{\tilde{a}} \sim 10 \left(\frac{m_{\tilde{a}}}{1 \text{ GeV}} \right) \left(\frac{10^{12} \text{ GeV}}{\phi_0} \right)^2$$

Dark matter abundance

Flaton decays late

$$\mathcal{T}_d \sim 1 \text{ GeV} \left(\frac{|\mu|}{\text{TeV}} \right)^2 \left(\frac{10^{12} \text{ GeV}}{\phi_0} \right)$$

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Dark matter abundance

Flaton decays late

$$\tau_d \sim 1 \text{ GeV} \left(\frac{|\mu|}{\text{TeV}} \right)^2 \left(\frac{10^{12} \text{ GeV}}{\phi_0} \right)$$

Axion Misalignment

$$\Omega_a \sim 3 \left(\frac{f_a}{10^{12} \text{ GeV}} \right)^{1.2} \times \begin{cases} 1 & \text{for } T_d \gg 1 \text{ GeV} \\ \left(\frac{T_d}{1 \text{ GeV}} \right)^2 & \text{for } T_d \ll 1 \text{ GeV} \end{cases}$$

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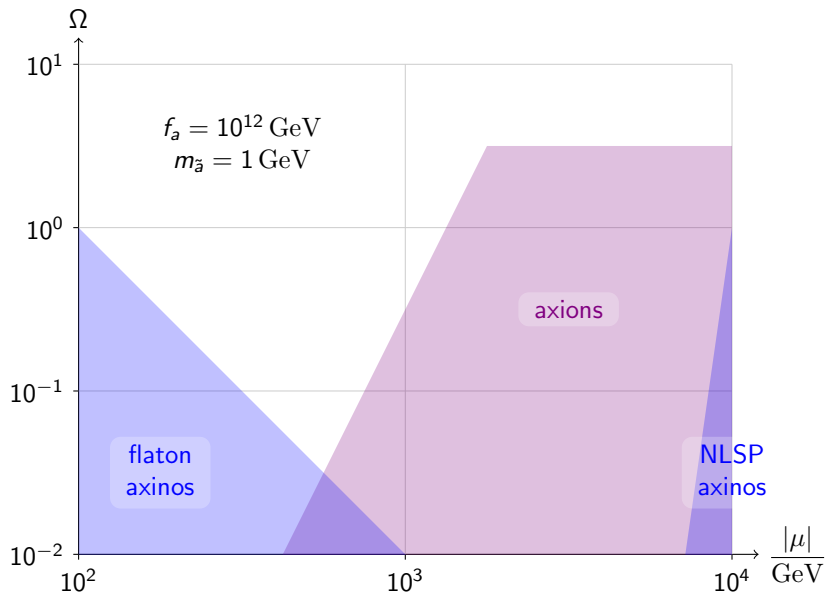
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Thermal NLSP decay

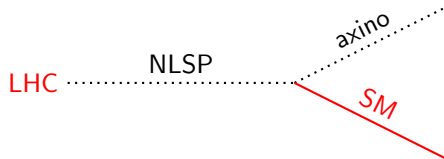
$$\Omega_{\tilde{a}} \sim 10 \left(\frac{m_{\tilde{a}}}{1 \text{ GeV}} \right) \left(\frac{10^{12} \text{ GeV}}{\phi_0} \right)^2 \times \begin{cases} 1 & \text{for } T_d \gg \frac{m_N}{7} \\ \left(\frac{7T_d}{m_N} \right)^7 & \text{for } T_d \ll \frac{m_N}{7} \end{cases}$$

Dark matter composition



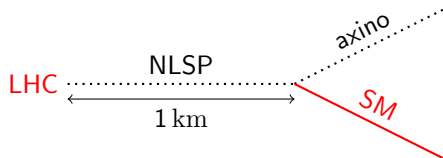
Axino LHC signal

NLSPs produced by the LHC decay to axinos plus Standard Model particles



Axino LHC signal

NLSPs produced by the LHC decay to axinos plus Standard Model particles



with a decay length

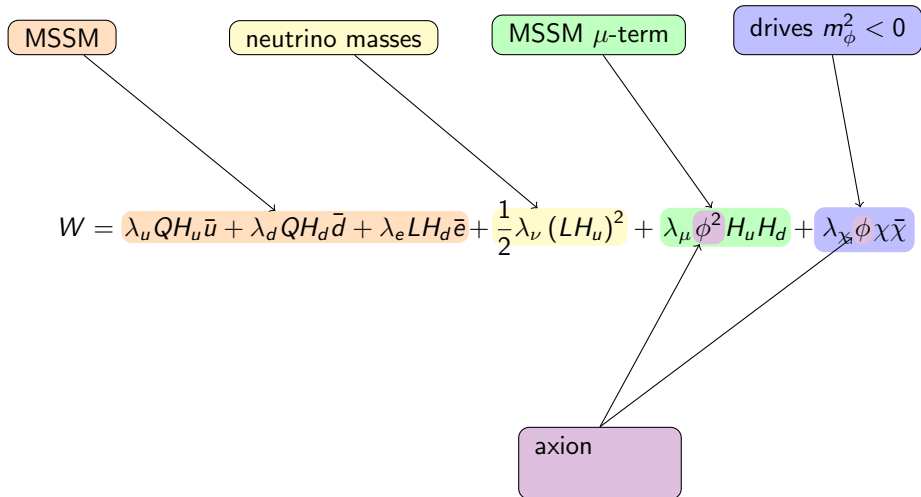
$$\frac{1}{\Gamma_{N \rightarrow \tilde{a}}} \sim \frac{16\pi\phi_0^2}{m_N^3} \sim 1 \text{ km} \left(\frac{200 \text{ GeV}}{m_N} \right)^3 \left(\frac{\phi_0}{10^{12} \text{ GeV}} \right)^2$$

and well constrained parameters

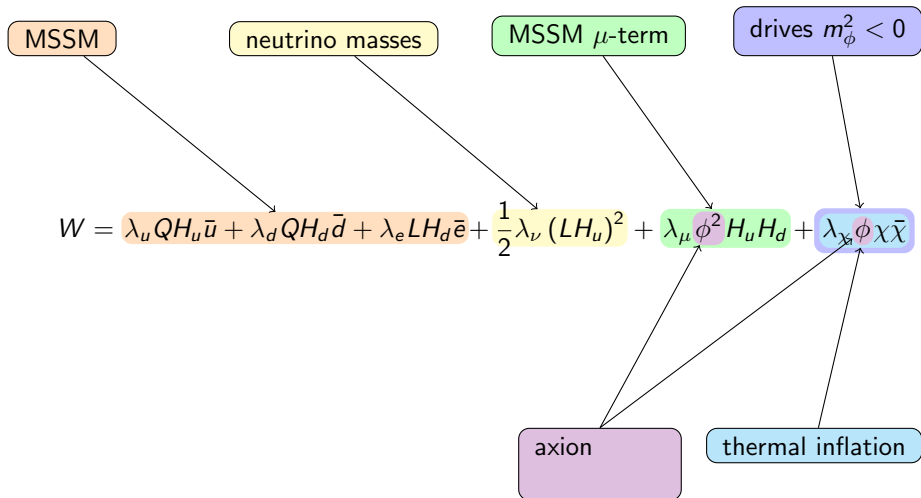
$$\phi_0 \sim 10^{12} \text{ GeV}$$

$$m_{\tilde{a}} \simeq 1 \text{ GeV}$$

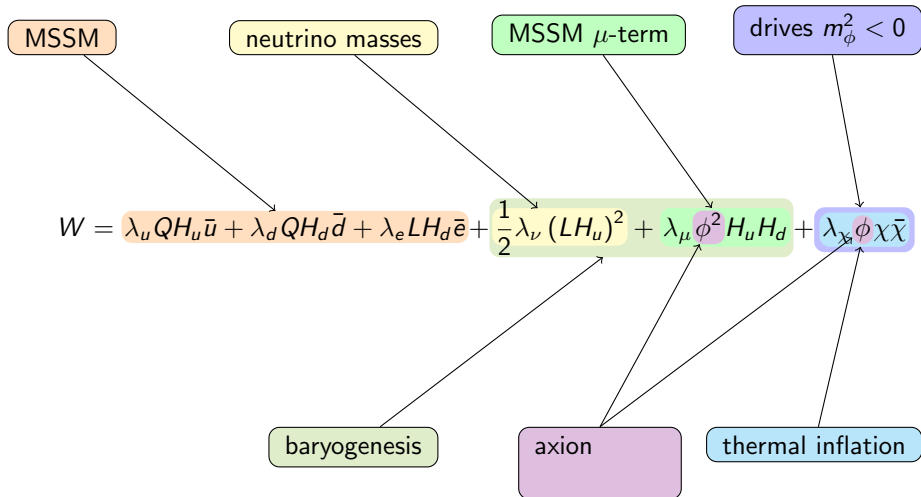
Simple model



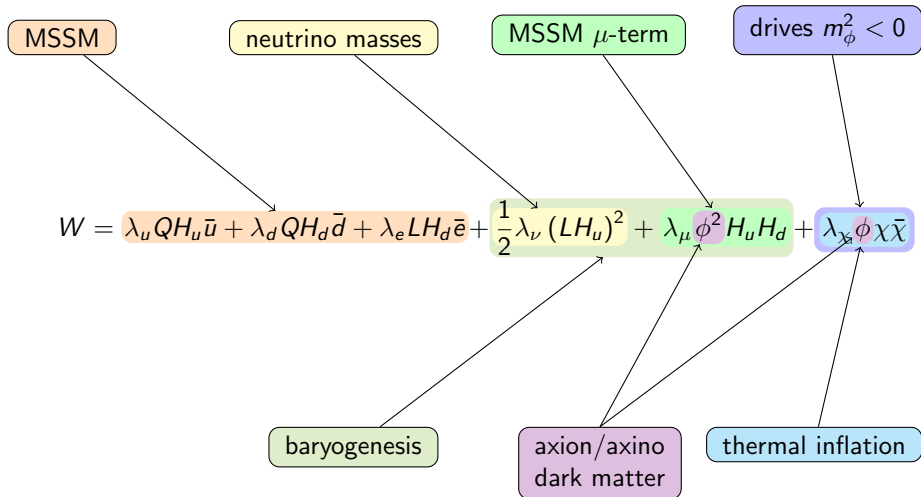
Simple model



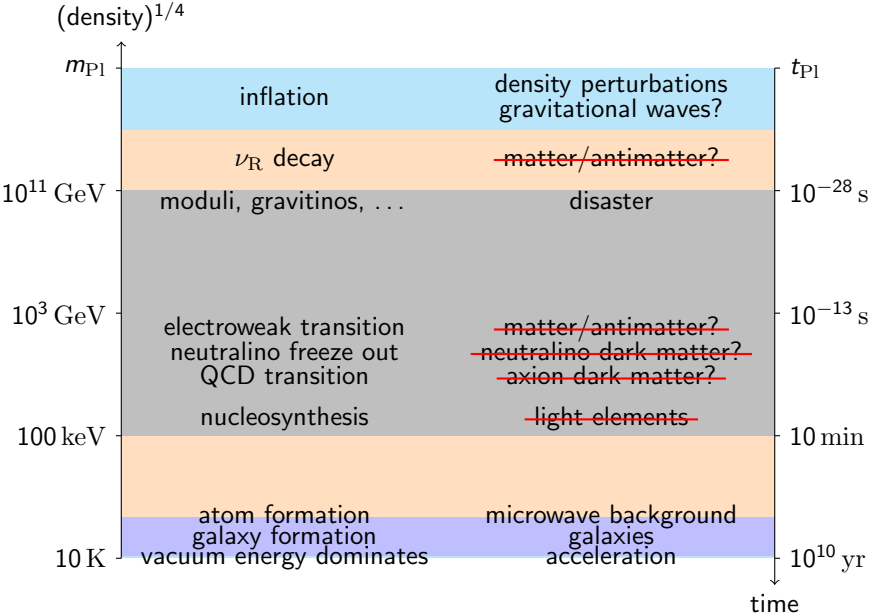
Simple model



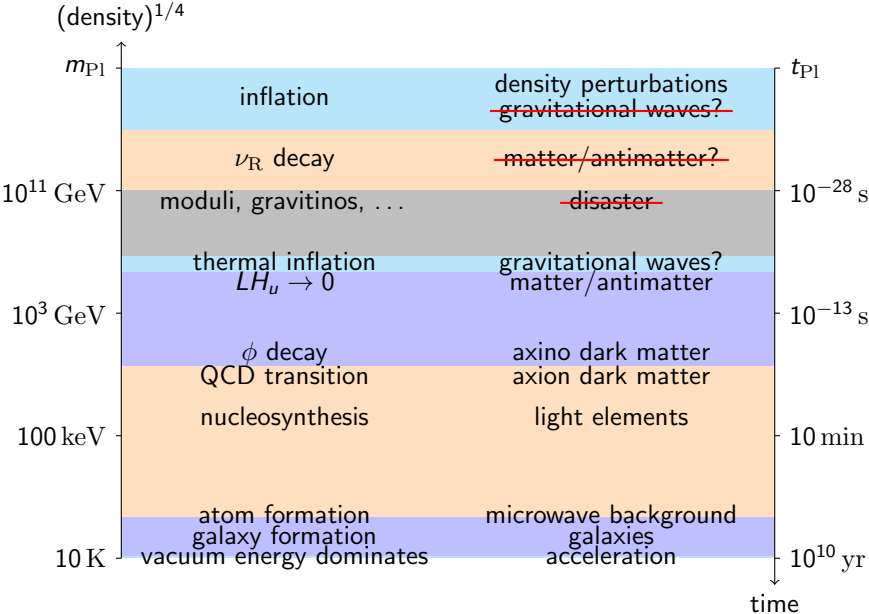
Simple model



Rich cosmology



Rich cosmology



A Minimal Supersymmetric Cosmological Model

Introduction

Standard model of cosmology

Moduli and gravitinos

A Minimal Supersymmetric Cosmological Model

MSSM

MSCM

Thermal inflation

Baryogenesis

Dark matter

Summary

Simple model

Rich cosmology