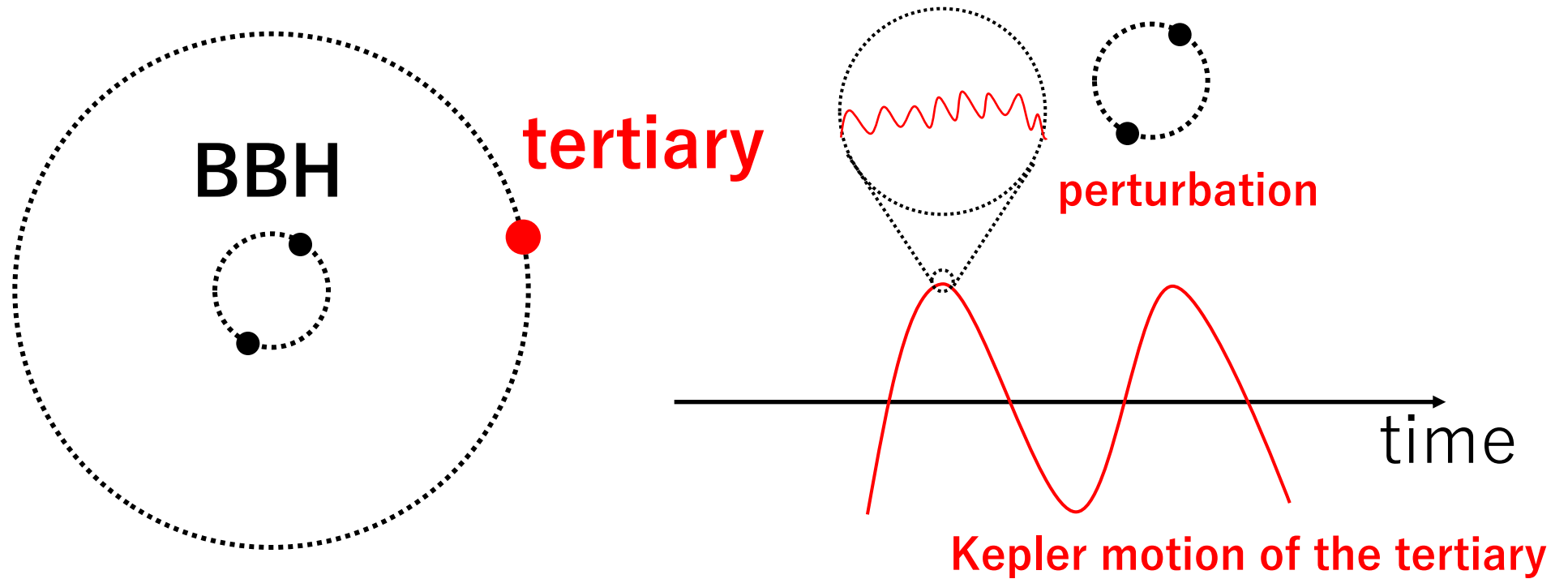


A strategy to search for an inner binary black hole from the motion of the tertiary companion:
radial-velocity modulation of a star and time-delay effect of a pulsar



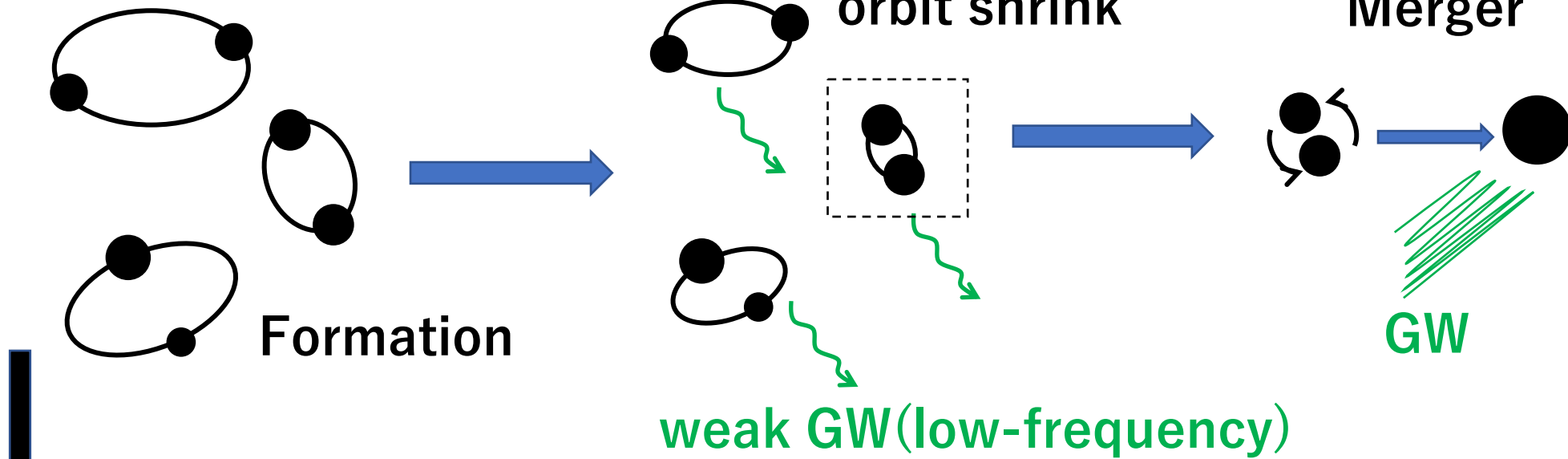
Toshinori Hayashi
University of Tokyo

11:10-11:25 18 Aug. 2020 @ Zoom meeting

Binary black holes (BBHs)

The discovery of BBH merger with GW
(2015, LIGO)

Binary black holes



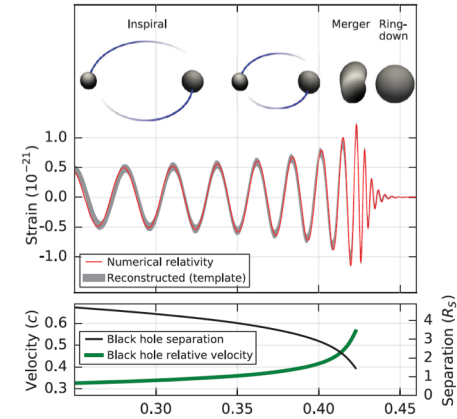
~Gyr scale orbital evolution (GW emission)

Long orbital-period BBHs
(e.g. ~10day orbital period \rightarrow $\sim 10^{-6}$ Hz)

Abundant progenitors ??

Except for GW, how to search for ?

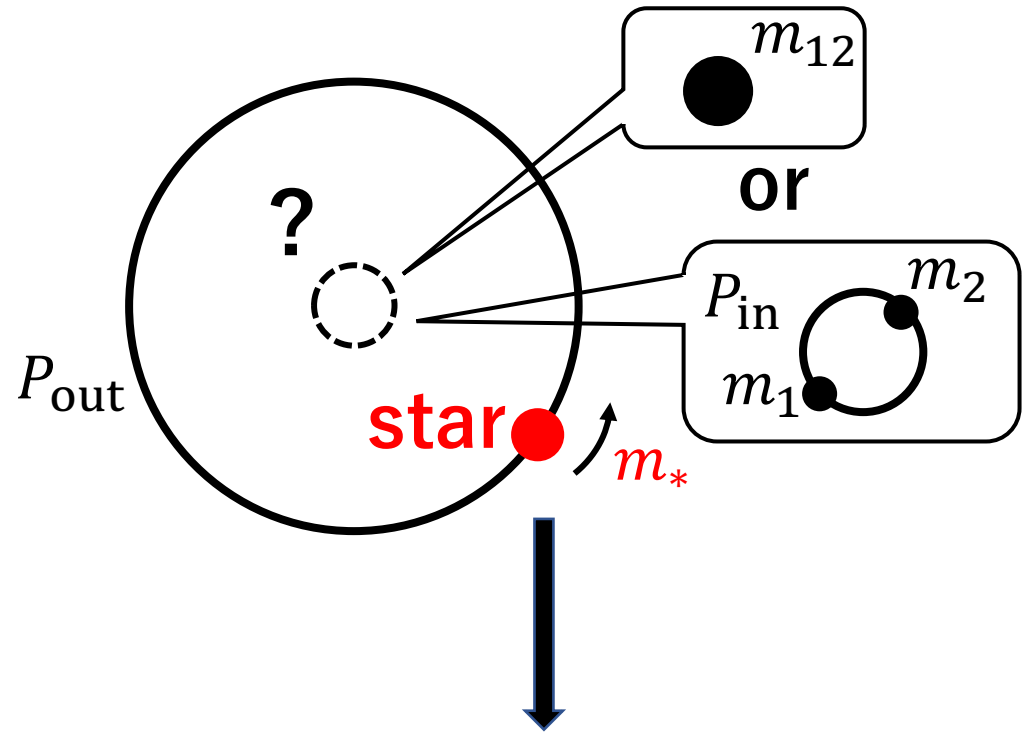
LIGO team 2016



GW detector

RV variations induced by the inner-binary perturbation

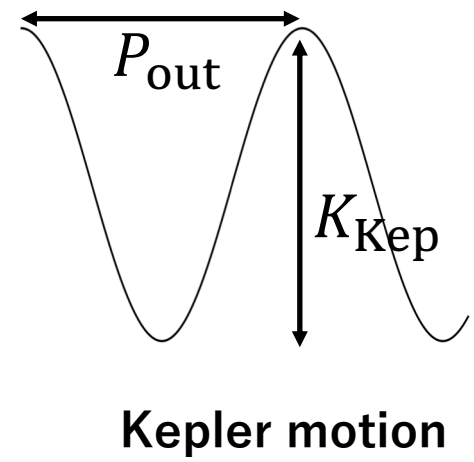
unseen object = **single** or **inner binary**



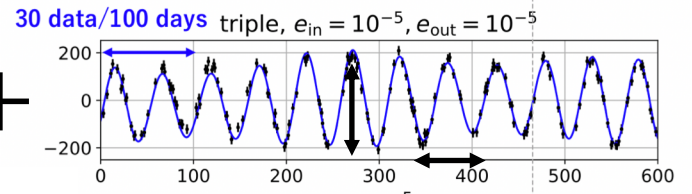
high-precision RV follow-up

Keplerian motion RV
+ **RV variations by inner binary**

(i) Coplanar triple



$$\text{Amp} \sim K_{\text{Kep}} \left(\frac{P_{\text{in}}}{P_{\text{out}}} \right)^{7/3}$$



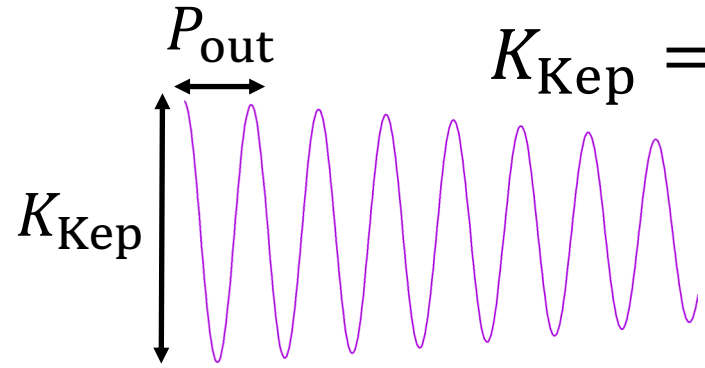
$$\text{Per} \sim P_{\text{in}}/2$$

Hayashi, Wang, Suto 2020

Short-term RV variations
(inner-binary perturbation)

(ii) Inclined triple

Inclination $I_{\text{out}}(t)$ evolves with Kozai-Lidov timescale

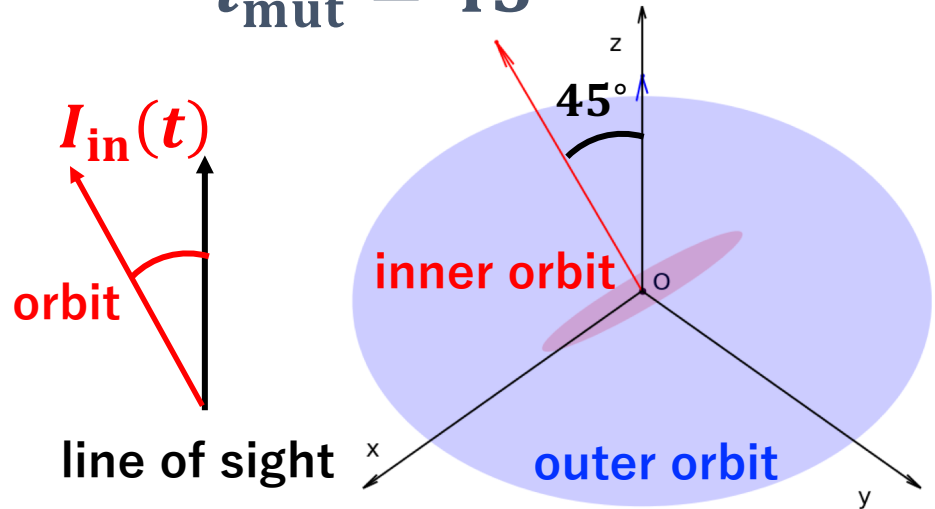


$$K_{\text{Kep}} = K_0 \sin I_{\text{out}}(t)$$

Amplitude of Kepler RV
varies with long-time scale

Time evolution of inclination for inclined triples

$i_{\text{mut}} = 45^\circ$ $t = 0P_{\text{out}}^{(0)}$



$P_{\text{out}} = 78.9$ days

$P_{\text{in}} = 10$ days

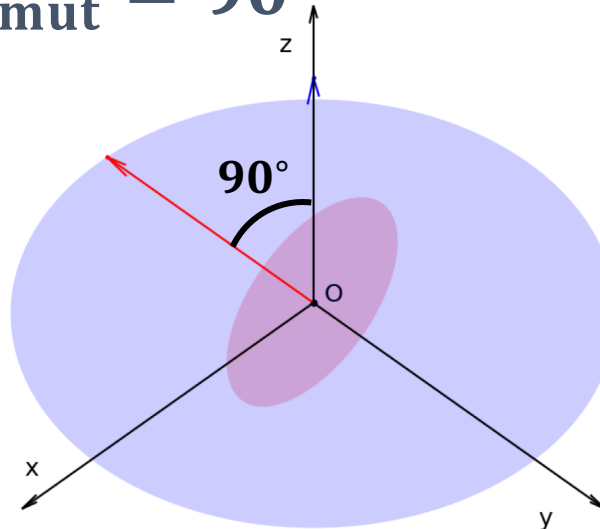
$m_1 = m_2 = 10M_\odot$

$m_* = 3M_\odot$

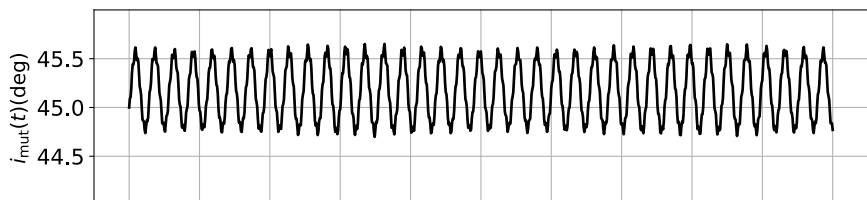
$e_{\text{out}} = 0.03$

$e_{\text{in}} = 10^{-5}$

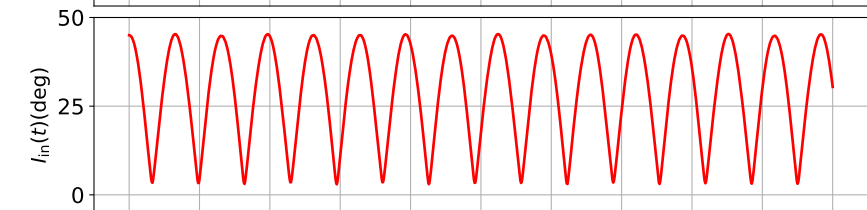
$i_{\text{mut}} = 90^\circ$ $t = 0P_{\text{out}}^{(0)}$



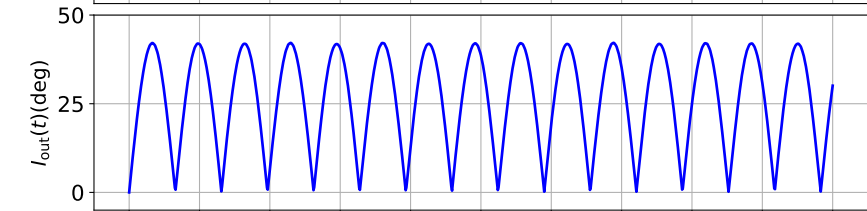
$i_{\text{mut}}(t)$



$I_{\text{in}}(t)$

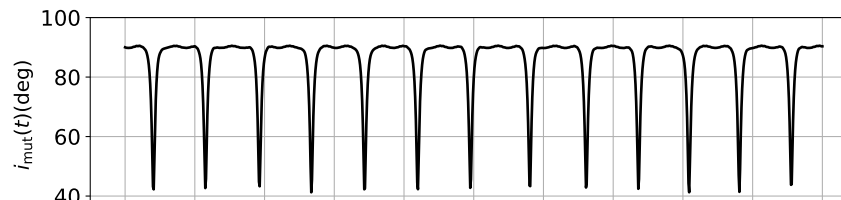


$I_{\text{out}}(t)$

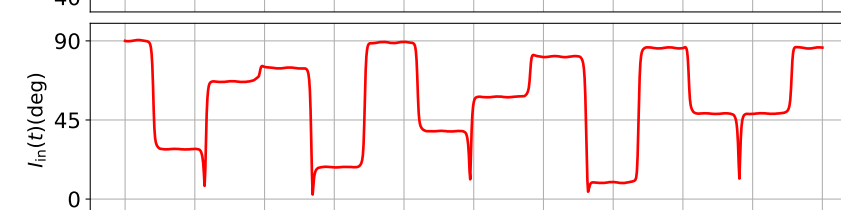


$t/P_{\text{out}}^{(0)}$

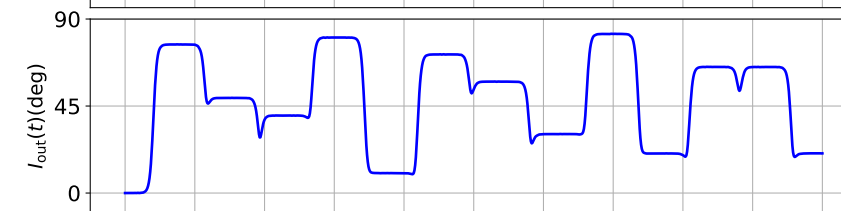
$i_{\text{mut}}(t)$



$I_{\text{in}}(t)$



$I_{\text{out}}(t)$

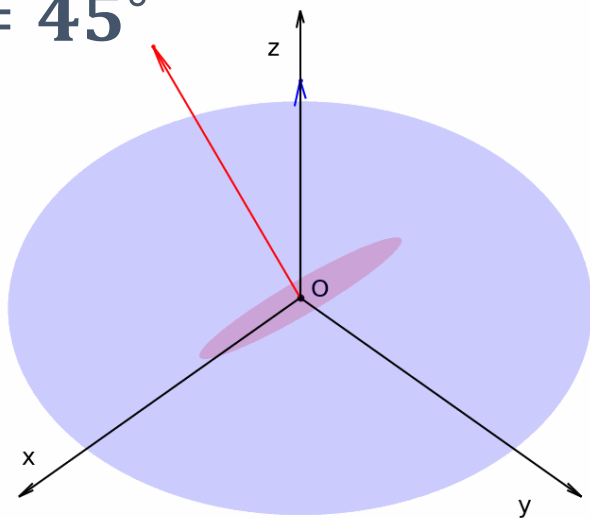


$t/P_{\text{out}}^{(0)}$

Time evolution of inclination for inclined triples

$t = 0P_{\text{out}}^{(0)}$

$i_{\text{mut}} = 45^\circ$

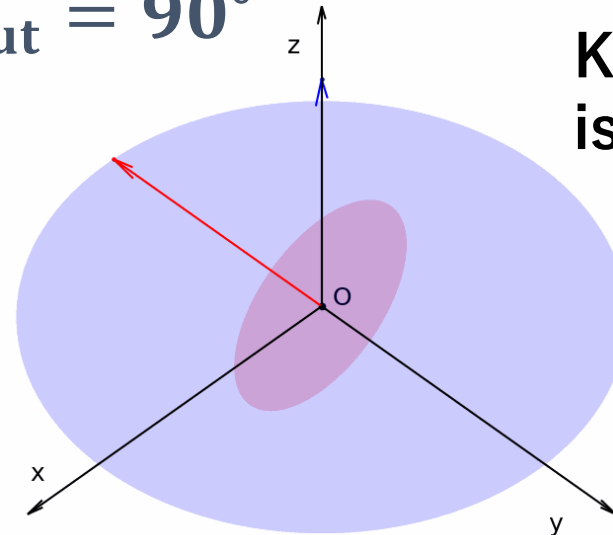


KL oscillation
is not effective
Regular
precession

$$K_{\text{Kep}} = K_0 \sin I_{\text{out}}(t)$$

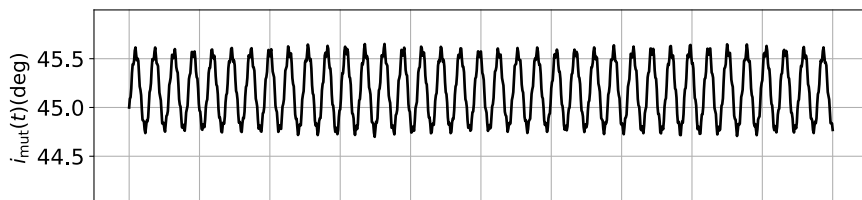
$t = 0P_{\text{out}}^{(0)}$

$i_{\text{mut}} = 90^\circ$

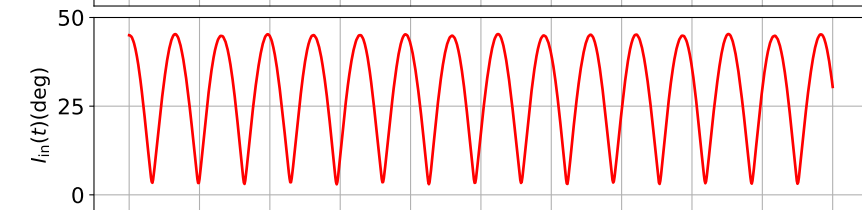


KL oscillation
is effective
Drastic
change

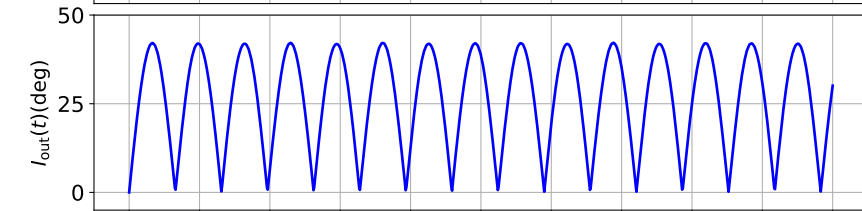
$i_{\text{mut}}(t)$



$I_{\text{in}}(t)$

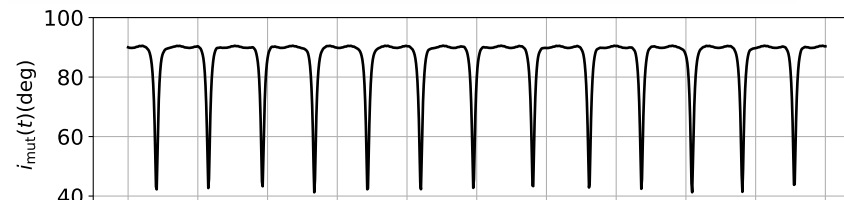


$I_{\text{out}}(t)$

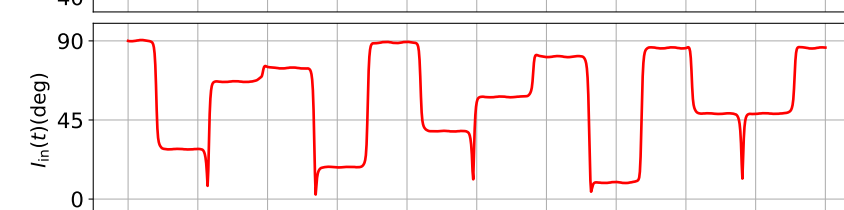


$t/P_{\text{out}}^{(0)}$

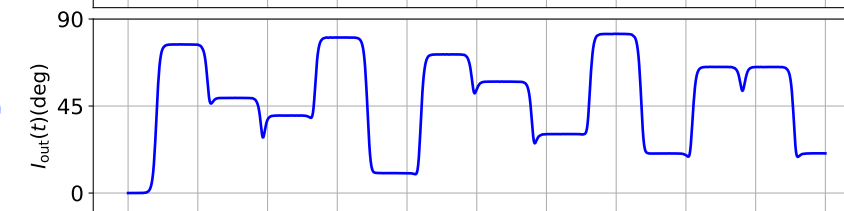
$i_{\text{mut}}(t)$



$I_{\text{in}}(t)$



$I_{\text{out}}(t)$

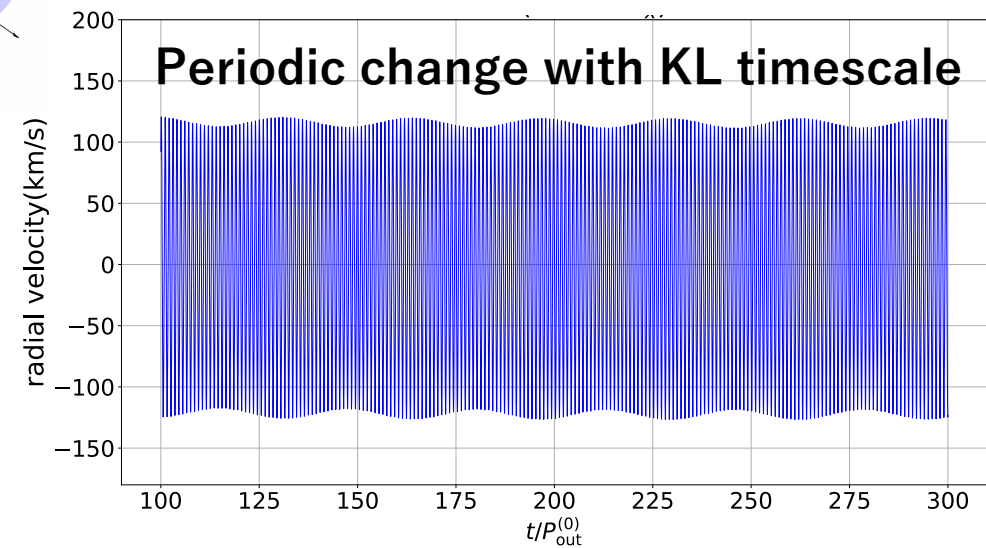
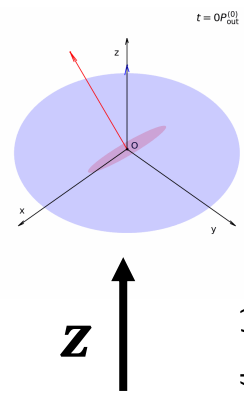


$t/P_{\text{out}}^{(0)}$

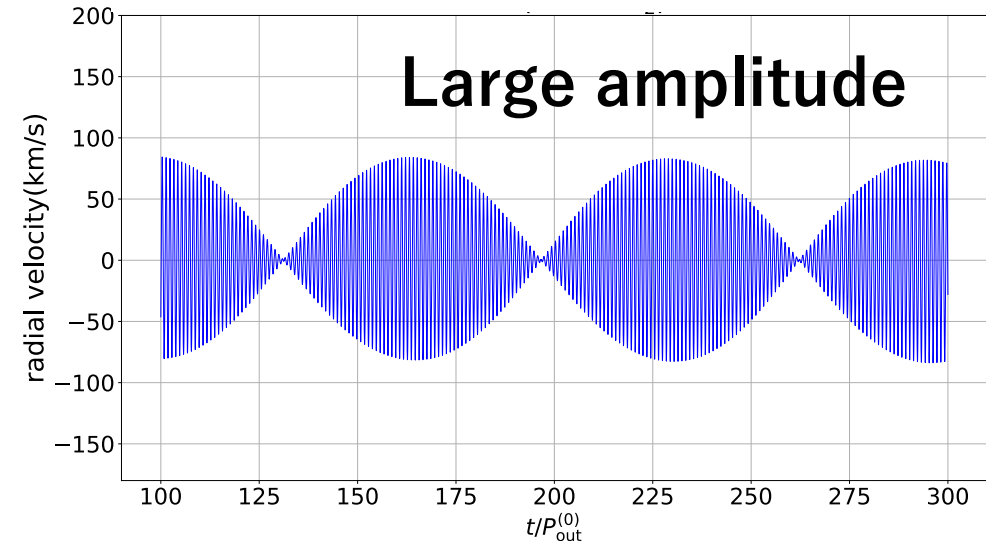
Long-term RV variations for inclined triples (ii)

$i_{\text{mut}} = 45^\circ$ $K_{\text{Kep}} = K_0 \sin I_{\text{out}}(t)$

x-direction (near edge-on) total RV

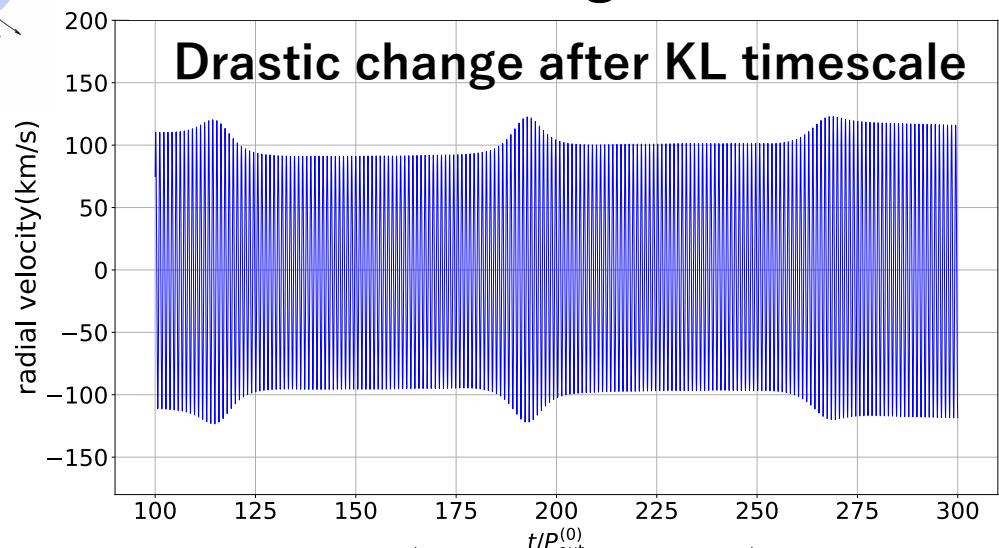
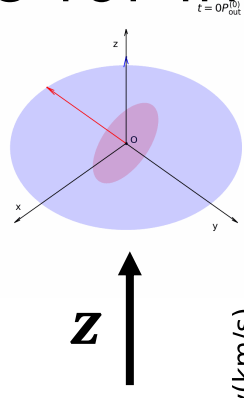


z-direction (near face-on) total RV

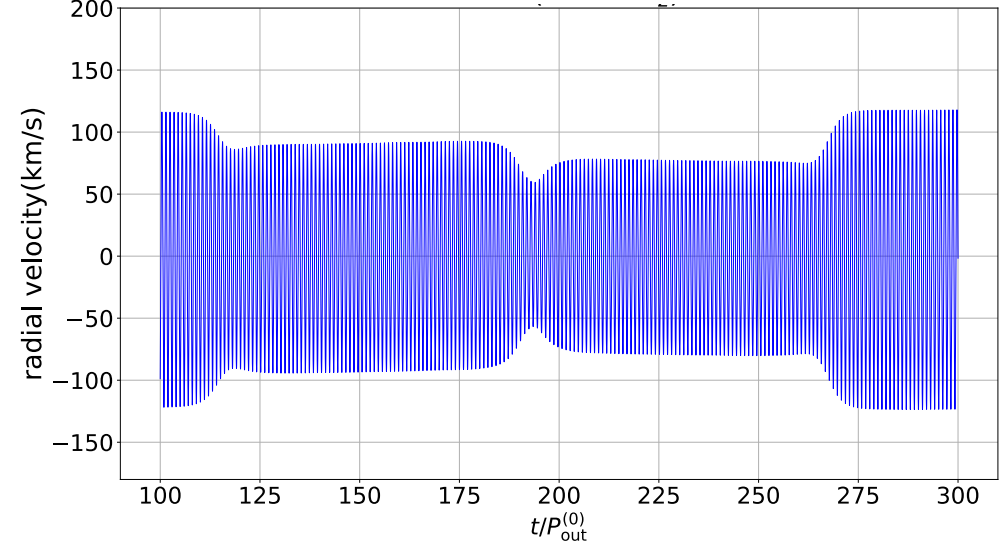


$i_{\text{mut}} = 90^\circ$

x-direction (near edge-on) total RV



z-direction (near face-on) total RV



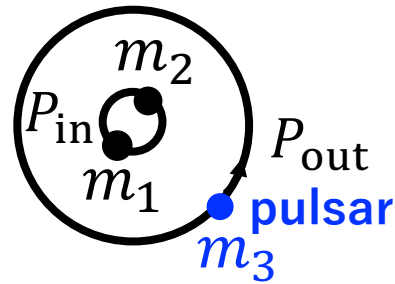
Pulsar time delay by the inner-binary perturbation

(Radial Velocity)

Plavchan+2015

- (1) Short distance ($< \text{kpc}$) for $O(10)$ m/s precision
- (2) Bright stars ($< 15 \text{mag}$) for $O(10)$ m/s precision
- (3) High-precision spectroscopy required

→



(Pulsar timing)

- (1) High precision ($\sim O(10)$ μsec)
- (2) Long distance (~ 10 kpc or farther)
- (3) Continuous observations (Pulsar Timing Array)

Pulsar time delays

(1) Rømer delay (Keplerian motion)

Change of the radial distance of pulsar

(2) Rømer delay (perturbation)

Gravitational perturbation by inner binary

(3) Relativistic delays

Redshift (Einstein delay)

Spacetime curvature (Shapiro delay)

(1)+(2)+(3)

→ All orbital parameters estimated

Expected amplitude of each time delay

Equal-mass inner binary

$$P_{\text{in}} = P_{\text{out}}/10 \text{ (solid black)}$$

$$P_{\text{in}} = P_{\text{out}}/50 \text{ (dotted black)}$$

$m_{12} \gtrsim 10M_{\odot}$
 $P_{\text{out}} \lesssim 1000 \text{ days}$
 $P_{\text{in}} \gtrsim 1/50 P_{\text{out}}$

target

$$m_{12} \equiv m_1 + m_2$$

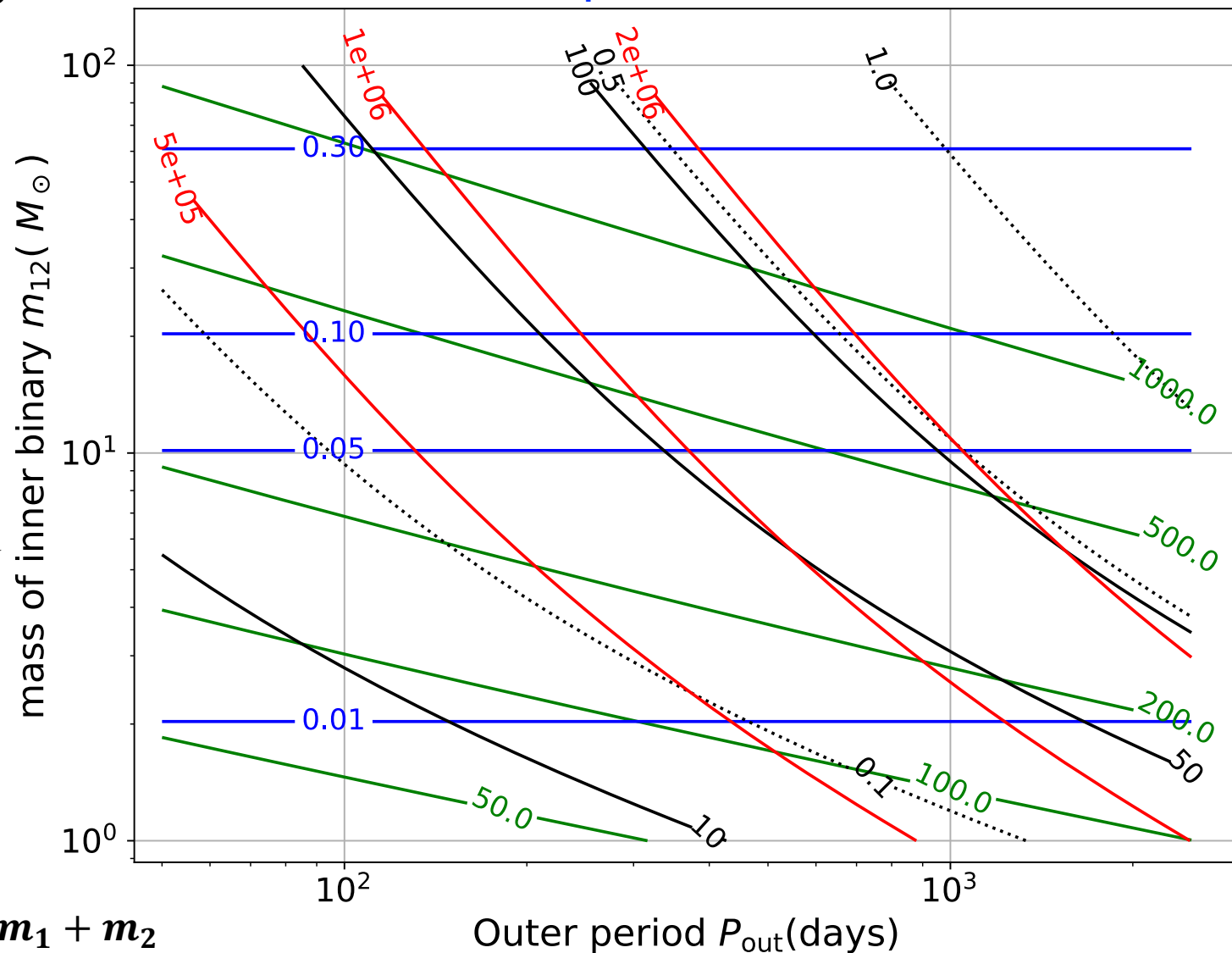
$m_1 = m_2$
 $m_3 = 1.4 M_{\odot}$

Einstein (msec)

Shapiro (msec)

Perturbation (msec)

Keplerian Rømer (msec)



Examples of time delay curves

Analytic expressions
(Backer&Hellings 1986,
Morais&Correia 2008,2011)

$$m_1 = m_2 = 10M_{\odot}$$

$$m_3 = 1.4M_{\odot}$$

$$P_{\text{out}} = 100 \text{ days}$$

$$P_{\text{in}} = 10 \text{ days}$$

Model CC (Coplanar Circular)

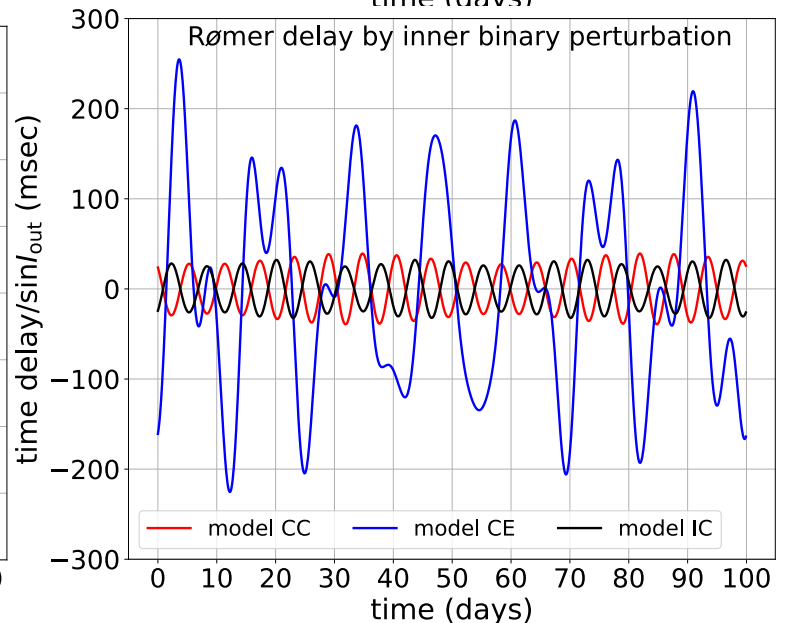
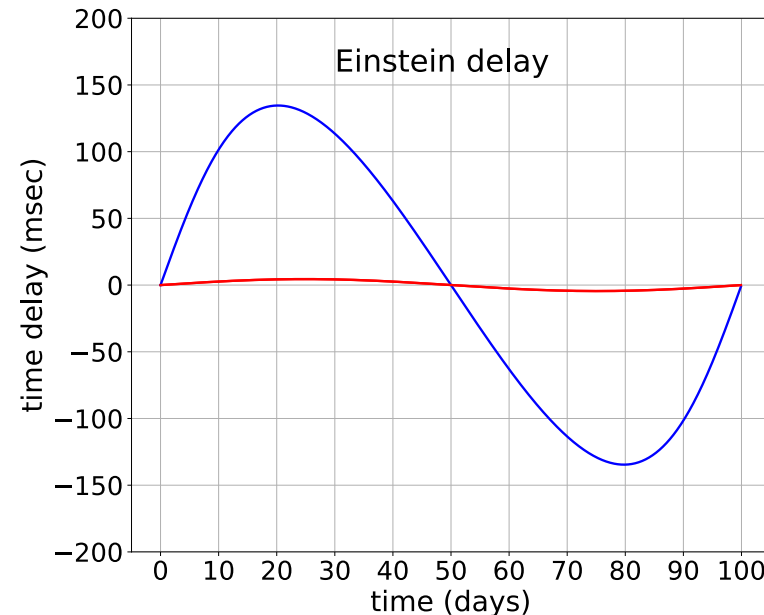
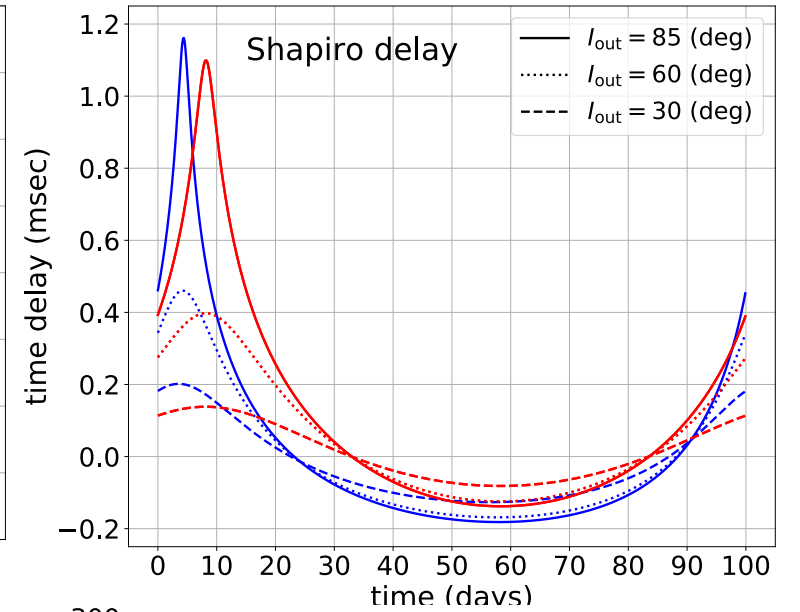
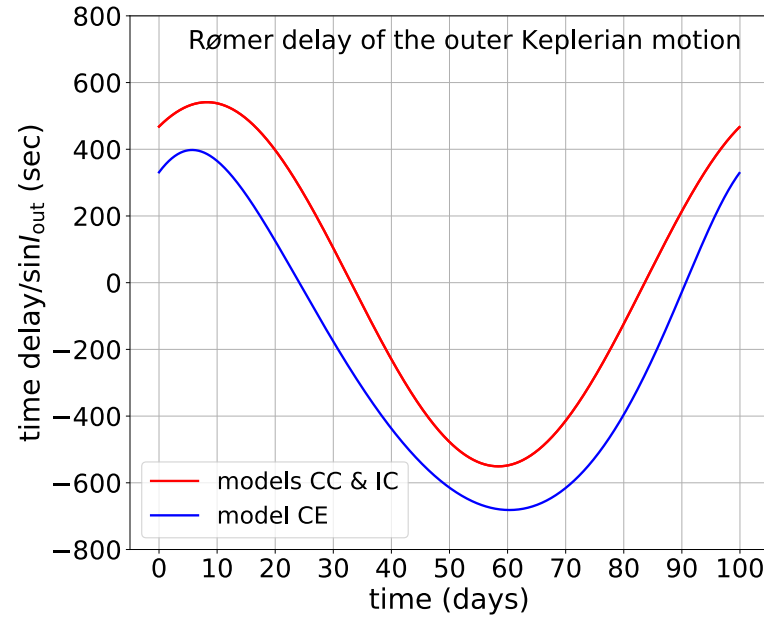
$$e_{\text{out}} = 0.01 \quad e_{\text{in}} = 0.0 \quad i_{\text{mut}} = 0^{\circ}$$

Model CE (Coplanar Eccentric)

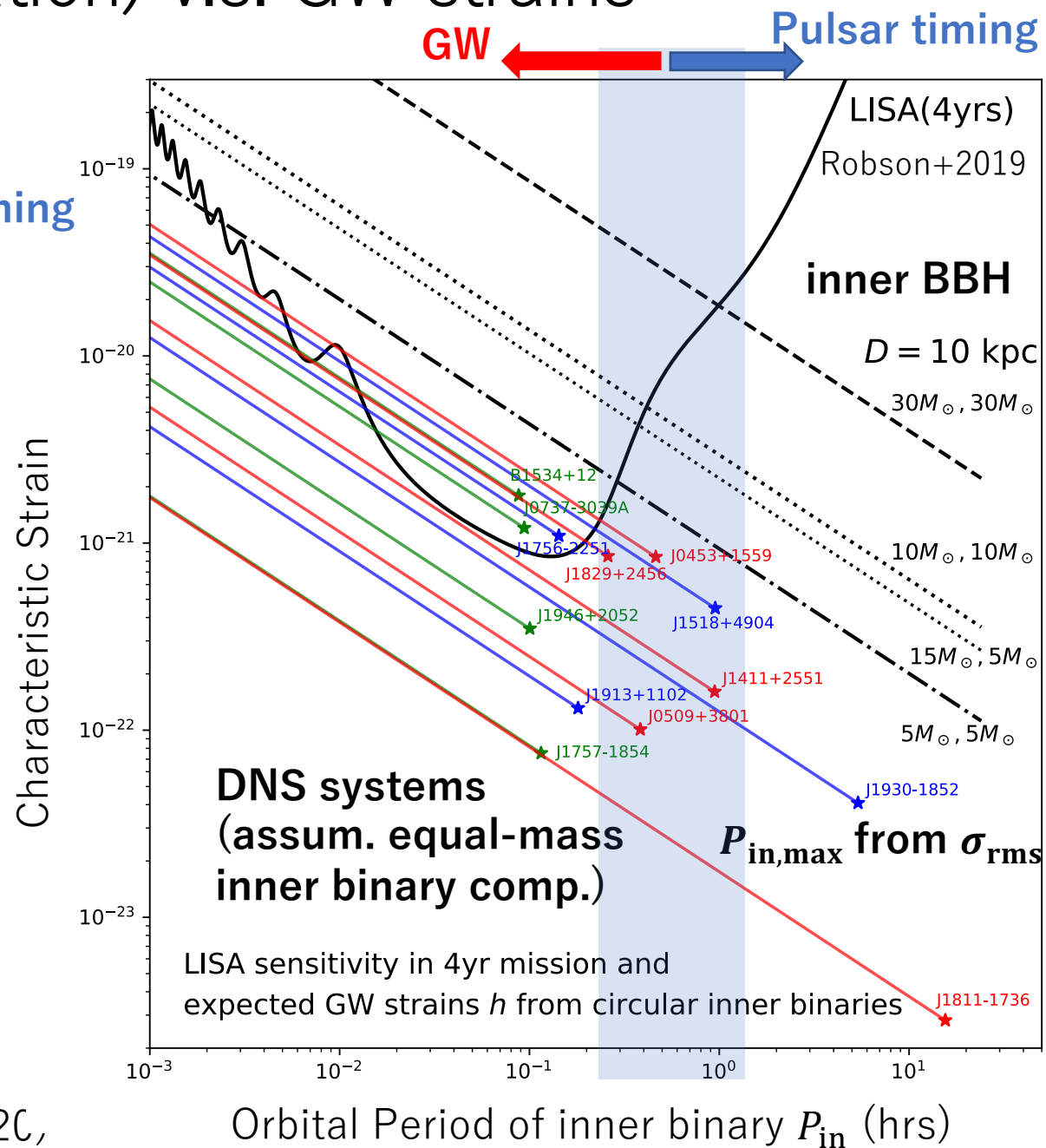
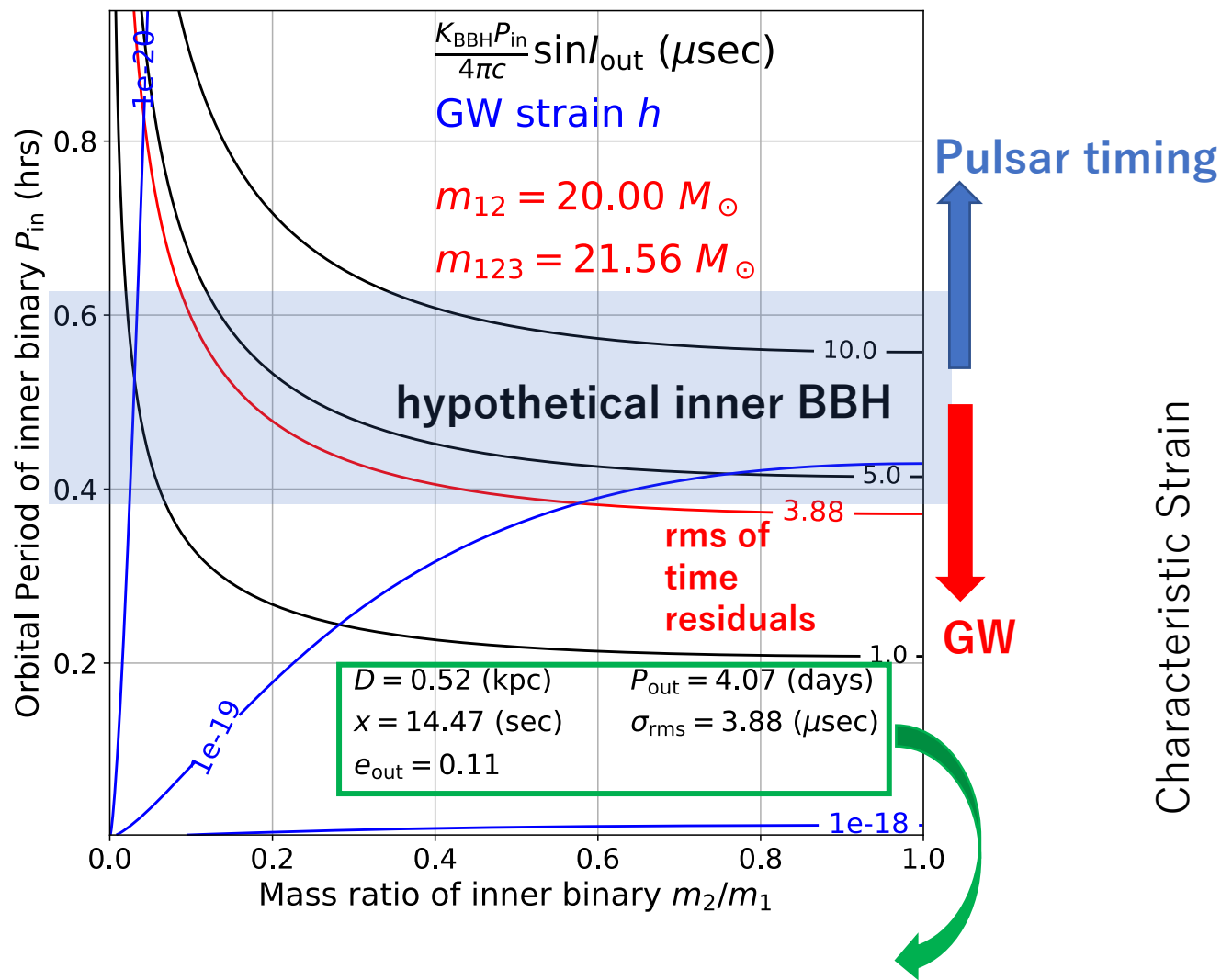
$$e_{\text{out}} = 0.3 \quad e_{\text{in}} = 0.2 \quad i_{\text{mut}} = 0^{\circ}$$

Model IC (Inclined Circular)

$$e_{\text{out}} = 0.01 \quad e_{\text{in}} = 0.0 \quad i_{\text{mut}} = 45^{\circ}$$



Rømer delay (perturbation) v.s. GW strains



Inner BBH could be constrained effectively by pulsar timing and GW

From double NS binary (DNS) J0453+1559 (Martinez+2015, Haniewicz+2020,

Summary and Future prospects

(Radial velocity)

Short-term RV variations due to an inner binary

Long-term RV amplitude variation **with KL timescale** for an inclined triple

Future surveys (Gaia; Yamaguchi+2018, TESS; Masuda&Hotokezaka 2019)

(Pulsar timing)

Rømer delays (**Kepler, perturbation**)+relativistic delays (**Einstein, Shapiro**)

→ Precise orbital parameter determination

A complementary method to future low-frequency GW surveys (e.g. LISA)