

# Satellitesimal Formation with Collisional Growth and Radial Drift of Dust Particles in Steady Circumplanetary Disks

Yuhito Shibaïke<sup>1</sup>

Satoshi Okuzumi<sup>1</sup>, Takanori Sasaki<sup>2</sup>, Shigeru Ida<sup>1</sup>

1. Tokyo Institute of Technology, 2. Kyoto University

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# Satellites in the solar system



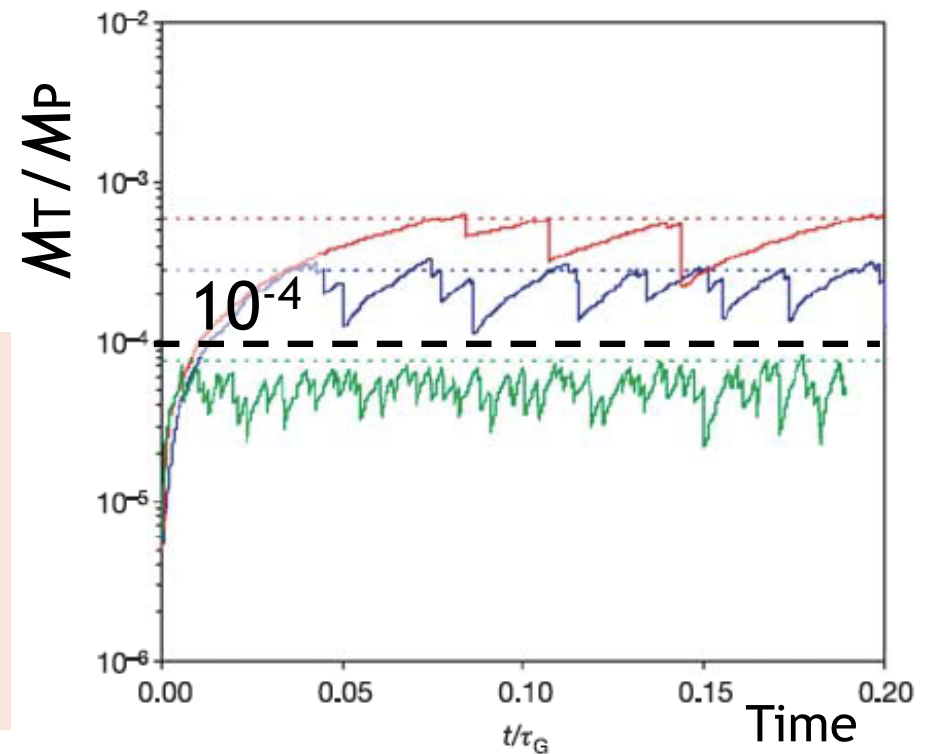
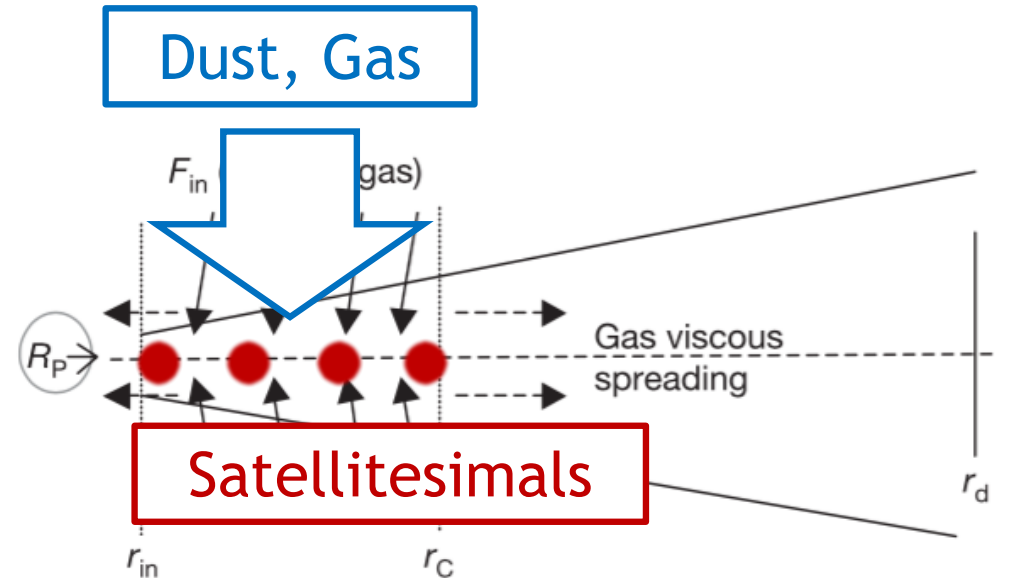
- Ice and rock
- Orbits are on the same plane



They formed in a circumplanetary disk around Jupiter

# Satellite formation in CPDs

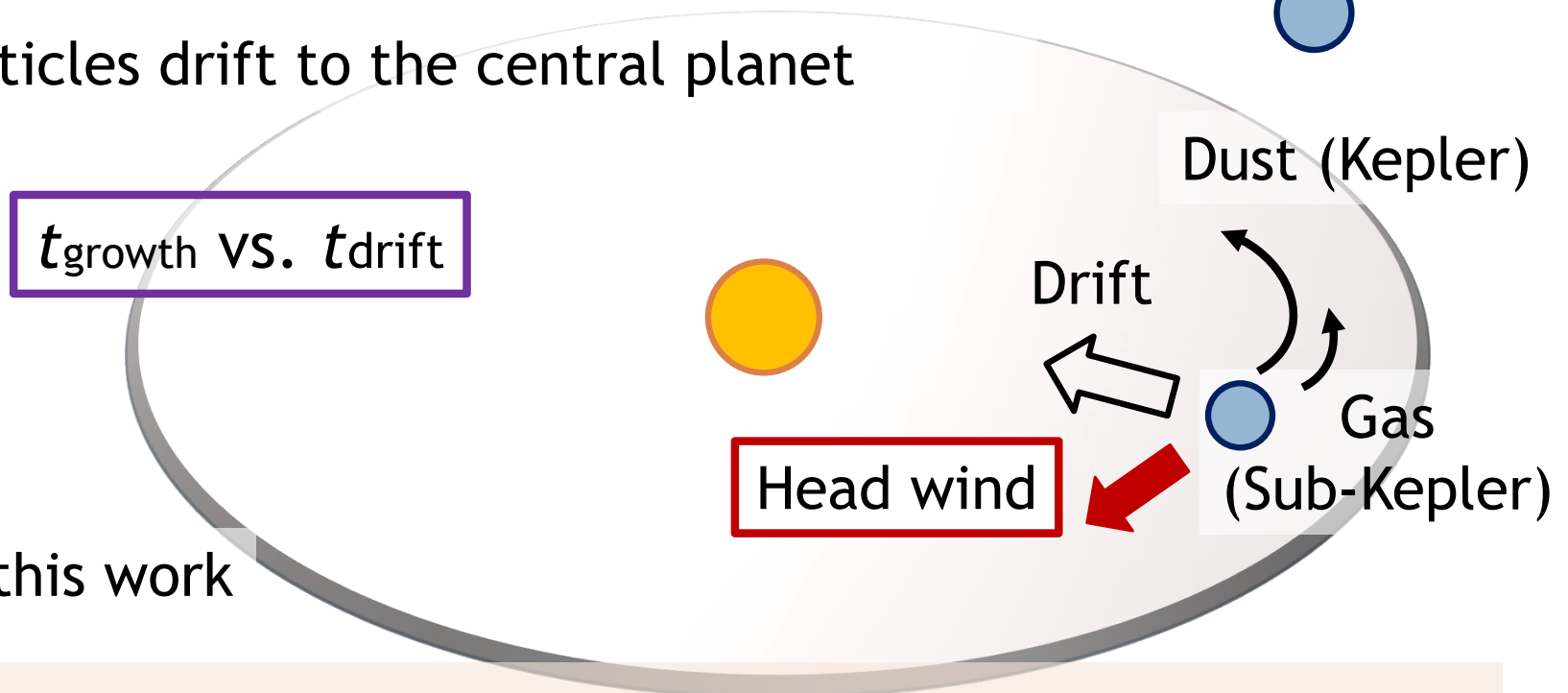
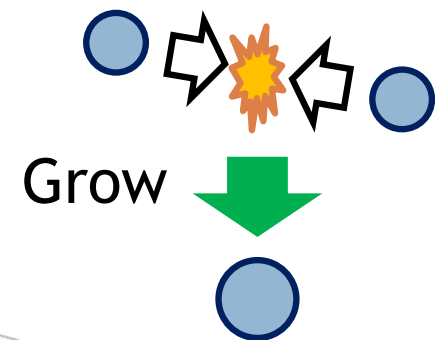
- ✓ Canup and Ward (2006) etc.
  - Gas and dust are supplied from the high altitude of CPD
    - They assumed the dust particles grow rapidly to satellitesimals
  - Satellitesimals grow to satellites
    - $t_{\text{growth}}$  vs.  $t_{\text{TypeI}}$
    - $M_T/M_P=10^{-4}$



- ✓ How to form satellitesimals?
  - **In-situ formation**  
(Shibaike et al. 2017)
  - Planetesimals capture  
(e.g. Fujita et al. 2013)

# Satellitesimal formation via collisional growth of dust particles

- ✓ Dust particles grow larger by pairwise collisions
- ✓ Dust particles drift to the central planet



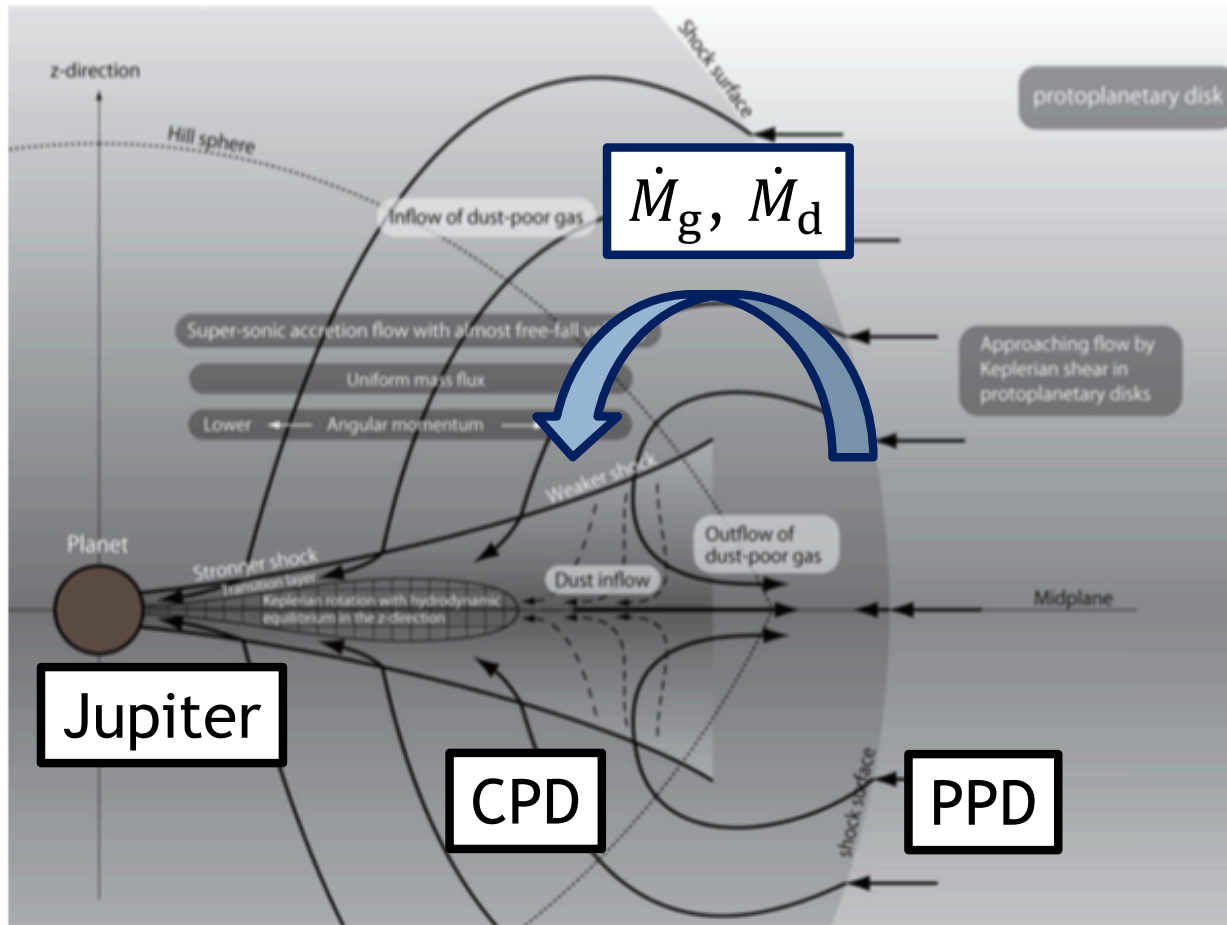
- ✓ Aim of this work

Calculate the collisional growth and drift of dust particles



Dust particles can grow to satellitesimals or not?

# Model: Dust and gas inflow



(Tanigawa et al. 2012)

- ✓ Gas is supplied from the high altitude of CPD
  - $\dot{M}_g$ : Gas inflow mass flux
- ✓ Dust flows to CPD with gas
  - $\dot{M}_d$ : Dust inflow mass flux

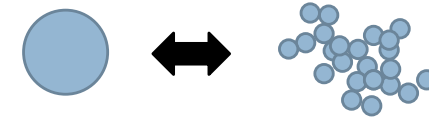
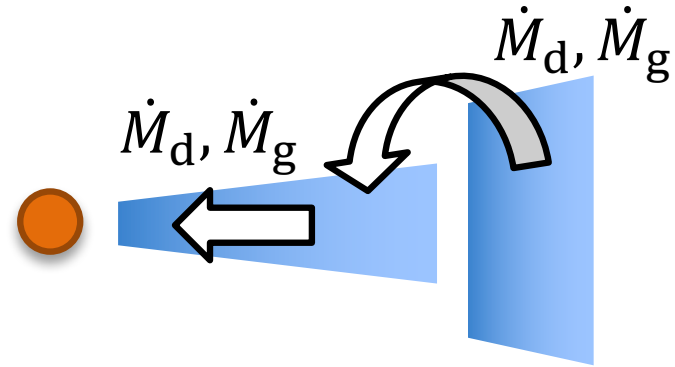
Dust to gas inflow mass flux ratio:

$$\dot{M}_d / \dot{M}_g = 1, 0.1, 0.01, \text{ and } 0.001$$



# Model

- ✓ **Steady** condition
- ✓ Viscous accretion disk
- ✓ No local structure
- ✓ Viscous heating
- ✓ Simple dust collisional growth model
  - Representative size
  - Perfect sticking
  - Compact dust ( $\leftrightarrow$  fluffy dust)
  - Supply at the outer edge of the gas inflow region
- ✓ Calculate the size(mass) and surface density of dust particles at each  $r$ 
  - Equation of continuity
  - Collisional growth

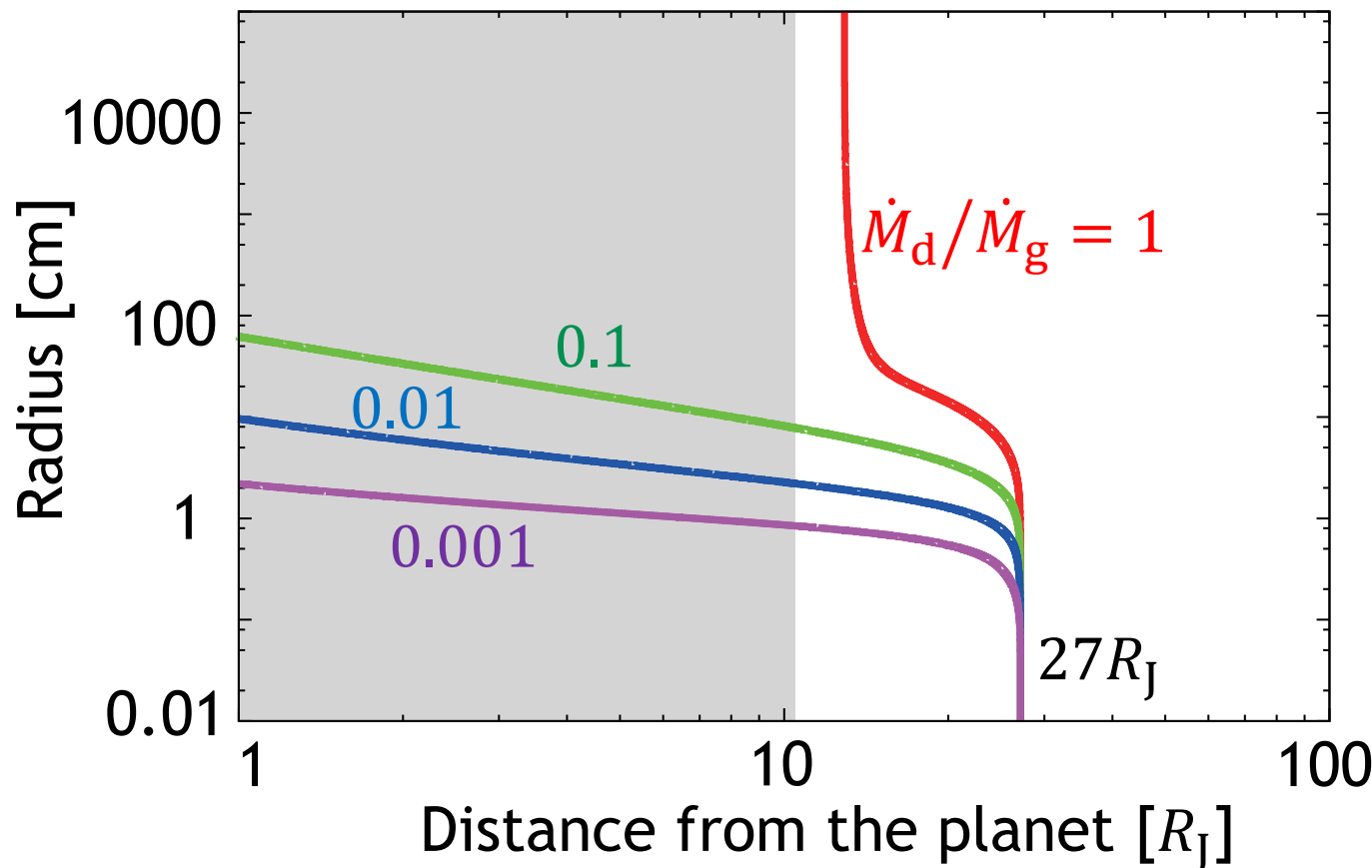


$$\dot{M}_d = 2\pi r |v_r| \Sigma_d$$

$$v_r \frac{\partial m_d}{\partial r} = \frac{2\sqrt{\pi} R_d^2 \Delta v_{dd}}{H_d} \Sigma_d$$

# Results: Radius

$$\alpha = 10^{-4}, \dot{M}_g = 0.02 M_J/\text{Myr}$$



1. Dust particles flow to the CPD at the outer edge of the gas inflow region (assumption)
2. They grow rapidly on the spot ( $t_{\text{growth}} < t_{\text{drift}}$ )
3. They start to drift ( $t_{\text{growth}} > t_{\text{drift}}$ )

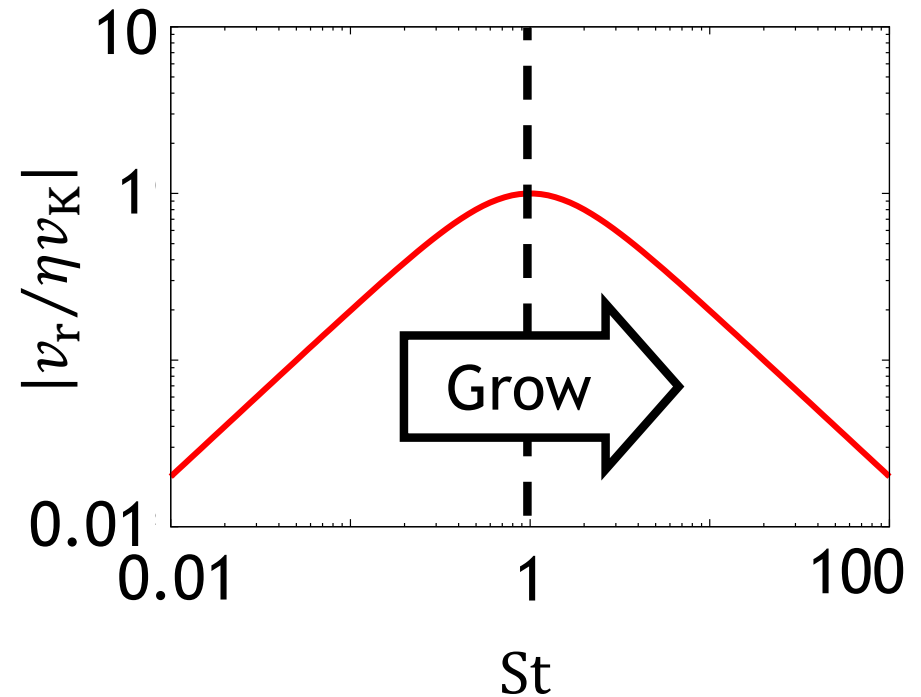
4. They stop drifting and grow to satellitesimals ( $\dot{M}_d/\dot{M}_g = 1$ ) or they drift to the planet ( $\dot{M}_d/\dot{M}_g = 0.001, 0.01, 0.1$ )

# Condition for satellitesimal formation

- ✓ Stokes number  $St$  ( $\hat{=}$  Size)
  - Determining the motion of dust particles in gases
  - $St$   
= (Stopping time)/(Kepler time)

$$St = \frac{8}{3C_D} \frac{\rho_{\text{int}} R_d}{\rho_g \Delta v_{\text{dg}}} \Omega_K$$

- ✓ Drift speed  $v_r$  becomes the fastest when  $St = 1$

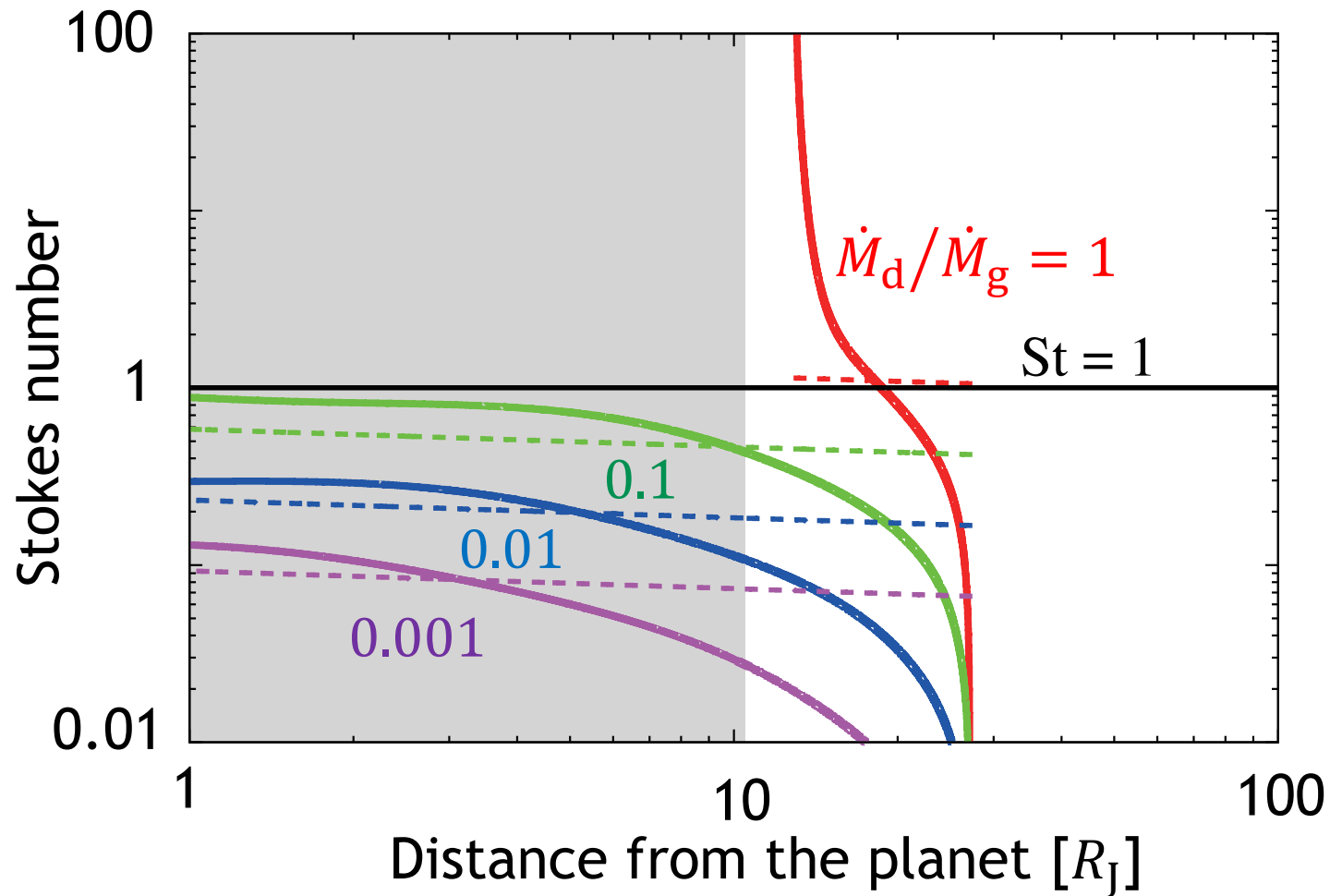


Dust particles have to grow to over  $St = 1$   
to form satellitesimals



# Results: Stokes number

$$\alpha = 10^{-4}, \dot{M}_g = 0.02 M_J/\text{Myr}$$



- Dust particles grow to satellitesimals only when  $St > 1$
- The  $\dot{M}_d/\dot{M}_g$  is larger, the Stokes number is larger
- Satellitesimals can form only when  $\dot{M}_d/\dot{M}_g = 1$

# Effects of $\dot{M}_d/\dot{M}_g$

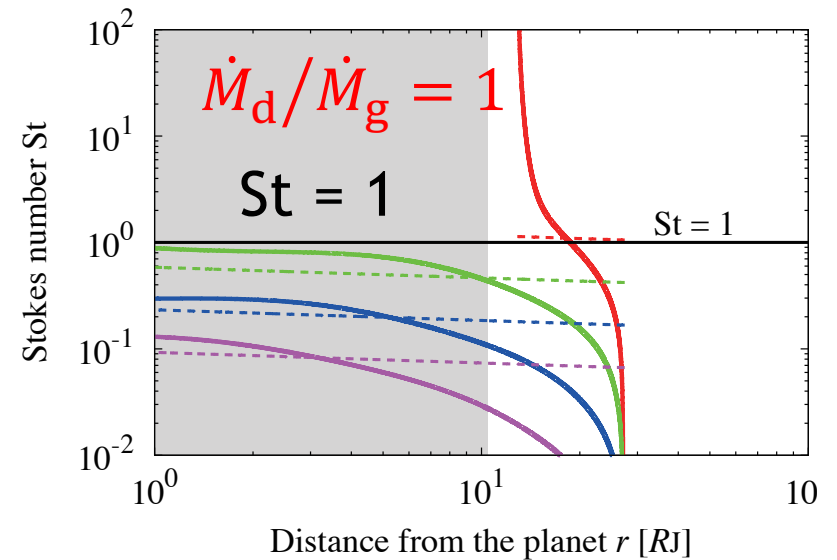
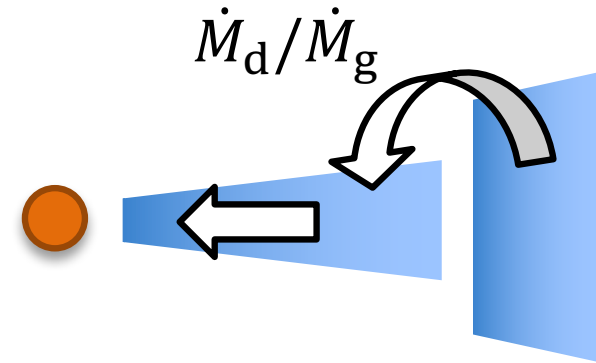
- ✓ When  $r \rightarrow 0$   
the Stokes number can be approximated as

$$St \approx 1.2 \left( \frac{\dot{M}_d/\dot{M}_g}{1} \right)^{2/5} \left( \frac{\alpha}{10^{-4}} \right)^{1/5} \times \left( \frac{T}{160 \text{ K}} \right)^{-2/5} \left( \frac{M_{cp}}{1 M_J} \right)^{2/5} \left( \frac{r}{10 R_J} \right)^{-2/5}$$

➤  $St \propto (\dot{M}_d/\dot{M}_g)^{2/5}$

- $\dot{M}_d \uparrow, \Sigma_d \uparrow, \text{Collision rate} \uparrow, St \uparrow$
- $\dot{M}_g \downarrow, \Sigma_g \downarrow, St \uparrow$

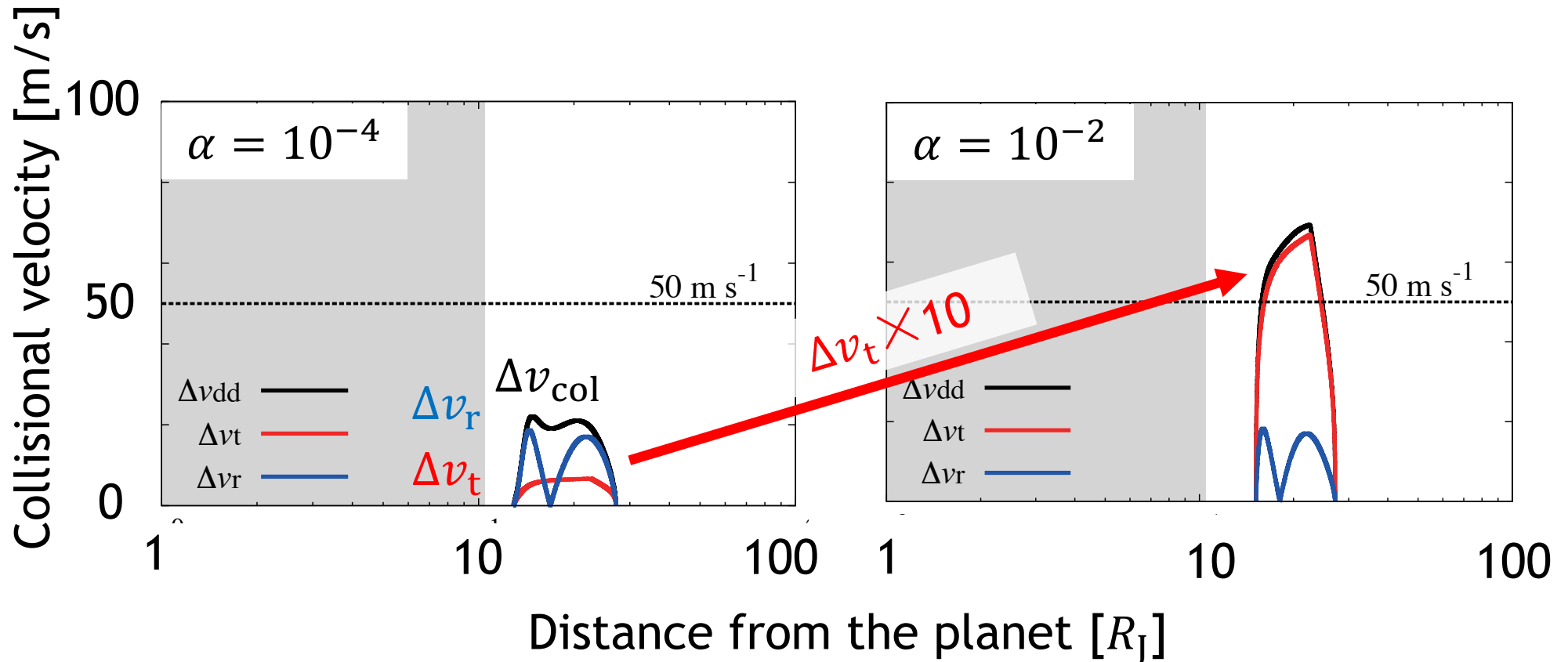
The  $\dot{M}_d/\dot{M}_g$  is larger, the Stokes number is larger



$$\dot{M}_d/\dot{M}_g = 1, \dot{M}_g = 0.02 M_J/\text{Myr}$$

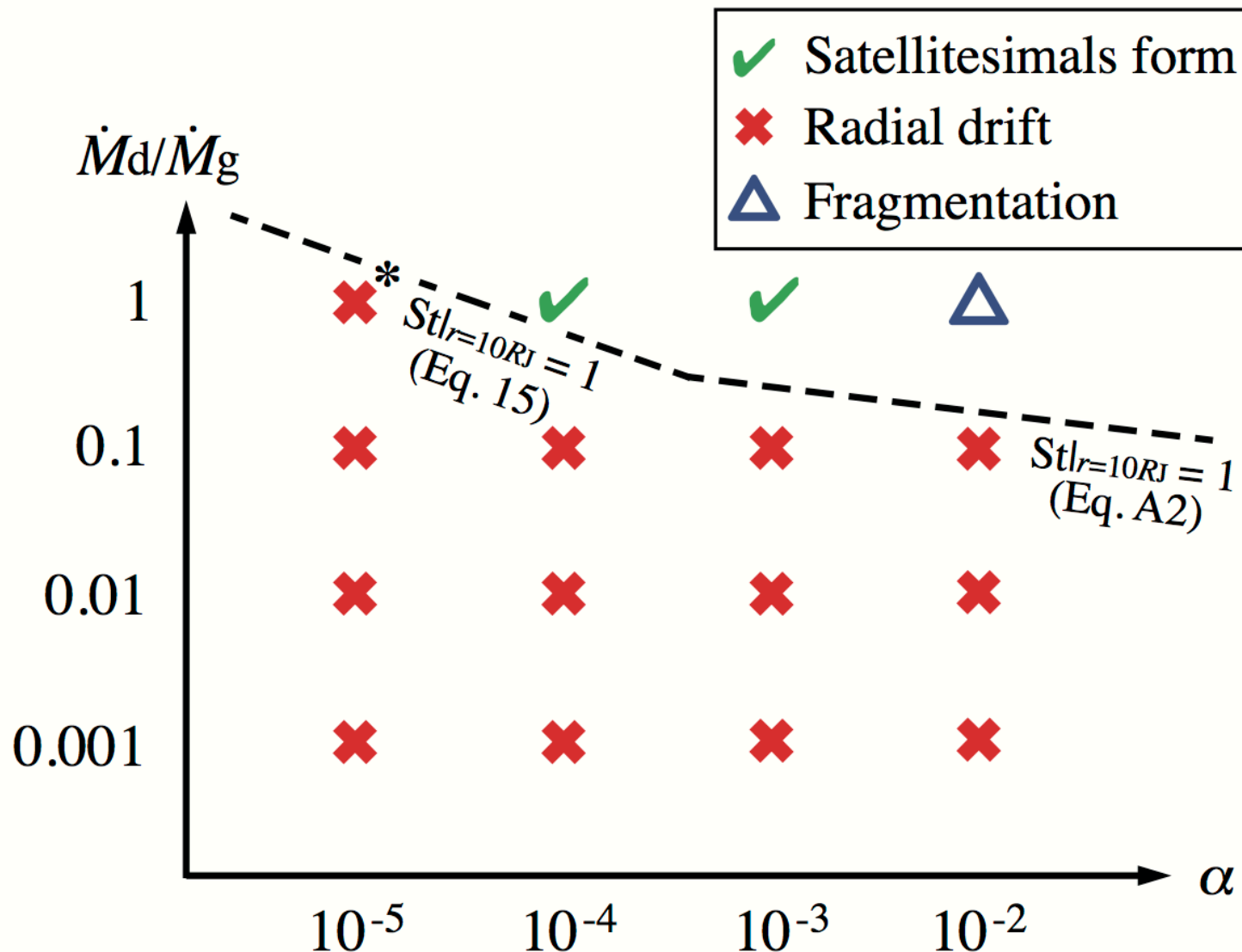
# Fragmentation

- ✓ Fragmentation occurs when the collisional velocity is faster than 50 [m/s] (Wada et al. 2009)



When  $\alpha = 10^{-2}$ , the collisional velocity is faster than 50 m/s  
→ Difficult to form satellitesimals

# Condition for satellitesimal formation



Condition for satellitesimal formation is

$$\dot{M}_d/\dot{M}_g \geq 1 \text{ and } 10^{-4} \leq \alpha < 10^{-2}$$

→ This condition is generally difficult to achieve...

# Summary

- ✓ We examined if dust particles can grow to satellitesimals
  - We calculated the size and surface density of dust particles at each  $r$  (distance from Jupiter)
  - We changed the dust-to-gas inflow mass flux ratio and strength of turbulence
- ✓ We found that...
  - The  $\dot{M}_d/\dot{M}_g$  is larger, the Stokes number is larger
  - When  $\alpha = 10^{-2}$ , fragmentation occurs
  - Condition for satellitesimal formation in steady CPDs is  $\dot{M}_d/\dot{M}_g \geq 1$  and  $10^{-4} \leq \alpha < 10^{-2}$
  - This condition is generally difficult to achieve