

Hajime Sotani, JGRG 22(2012)111407

“Shear oscillations in hadron-quark mixed phase”

**RESCEU SYMPOSIUM ON
GENERAL RELATIVITY AND GRAVITATION**

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Shear Oscillations in Hadron-Quark Mixed Phase

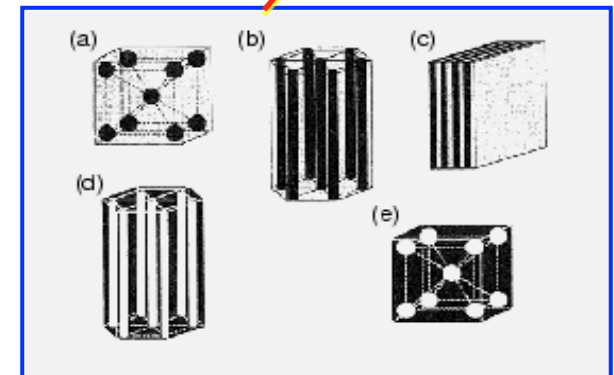
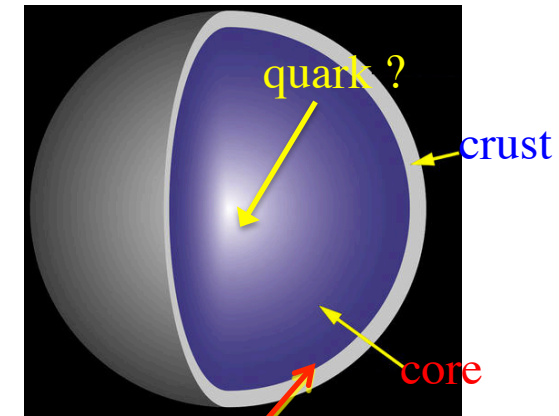
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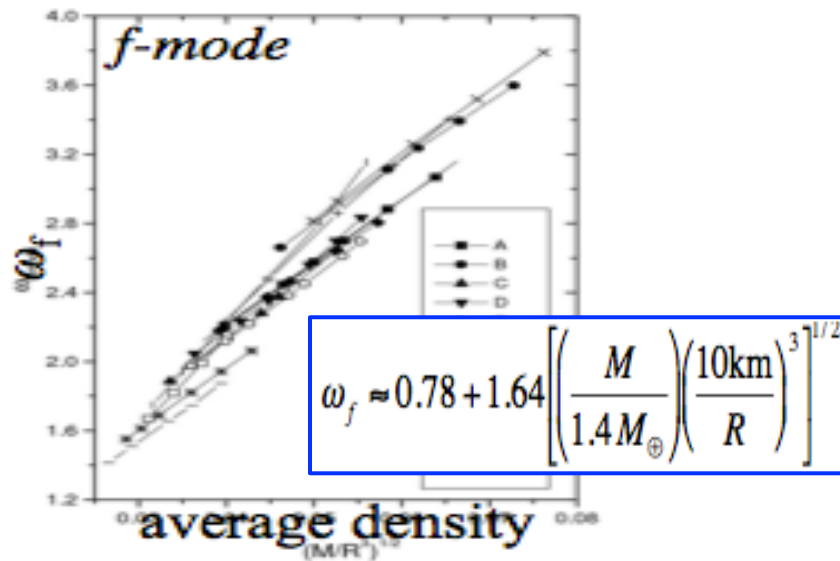
Hadron-Quark Mixed Phase

- Nonuniform structure between the crust and core (**pasta**).
- As increasing the density, hadronic matter could change to quark matter with the *phase transition*.
- Similar to the pasta in crust region, the **hadron-quark mixed phase** may become nonuniform structure, whose properties depend strongly on the **surface tension**.
 - $10 \text{ MeV fm}^{-2} < \sigma < 70 \text{ MeV fm}^{-2}$
- *How can we see such properties ??*

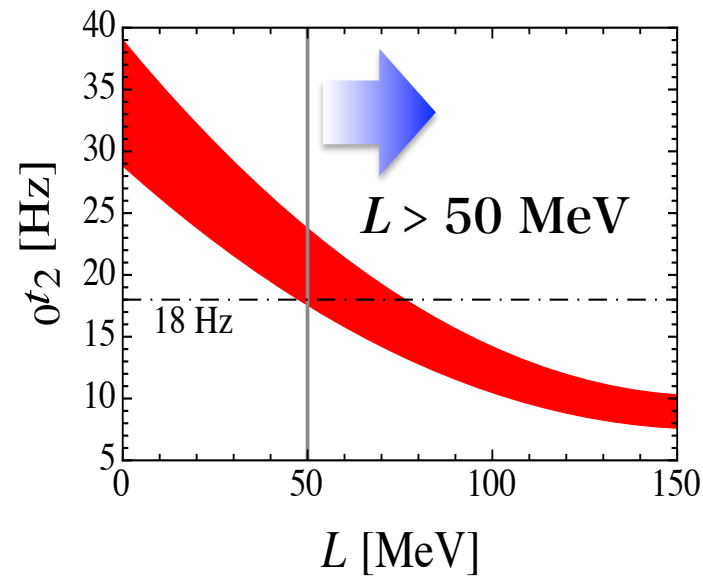


Asteroseismology

- Via the observations of stellar oscillations
 - One can get the interior information (**asteroseismology**)
e.g., helioseismology for Sun
- With this technique, the possibilities to get the information of NSs have been suggested.

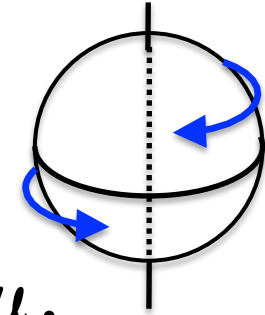


Andersson & Kokkotas (1998)

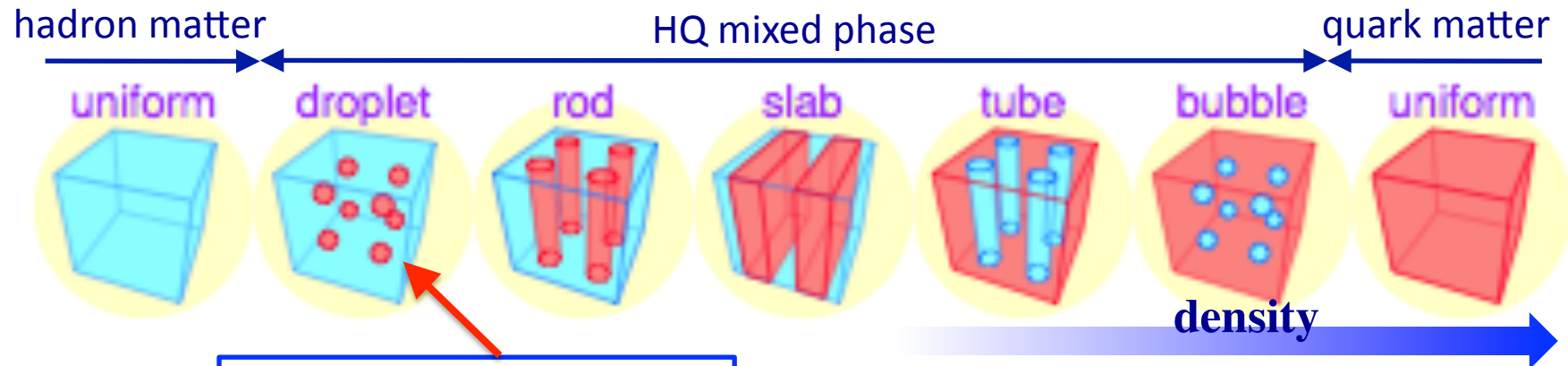


HS+2012

Shear Oscillations



- Shear oscillations can be characterized by μ .
- We know the formula of μ only in bcc lattice.
 - considering the shear only in quark spherical droplet.
 - frequency of fundamental oscillation $\propto v_s$ ($v_s^2 \sim \mu/\rho$)
 - calculated frequencies could be lower limit



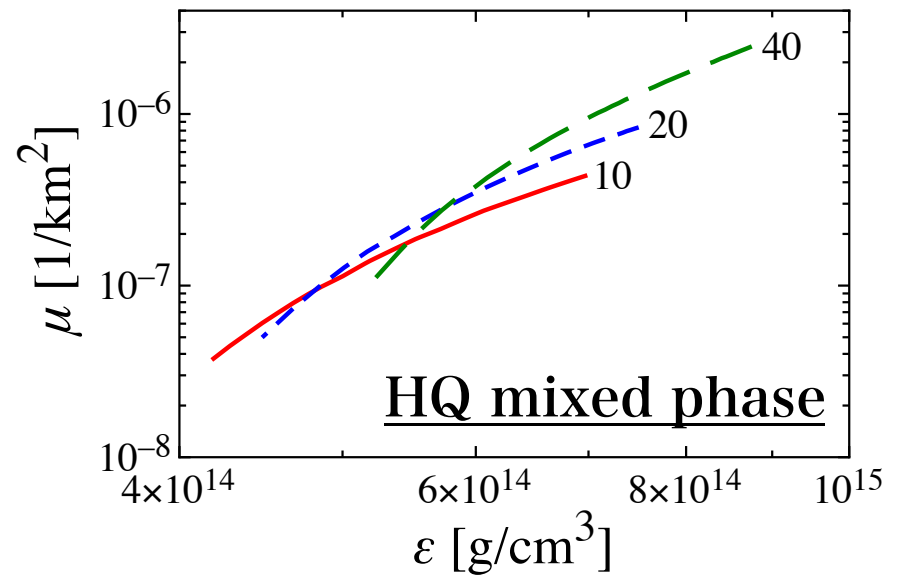
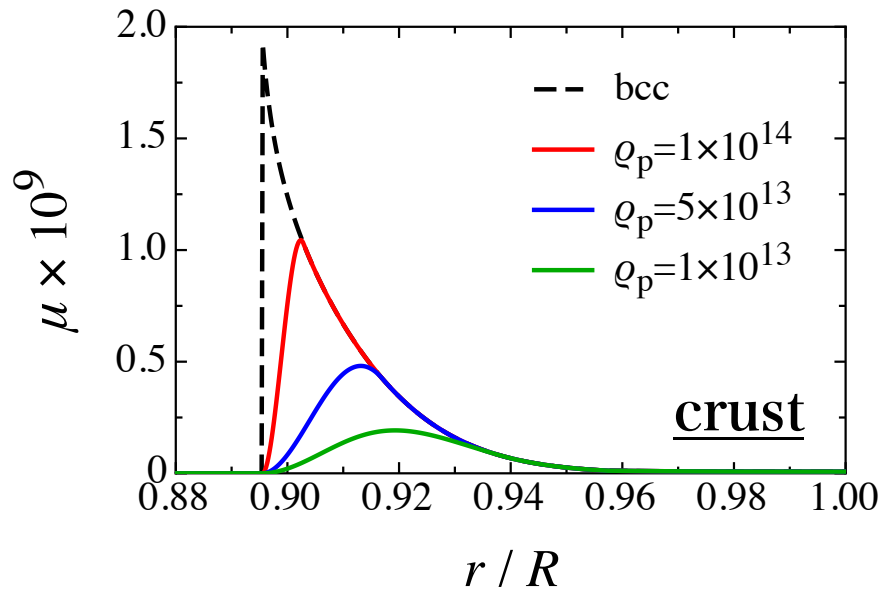
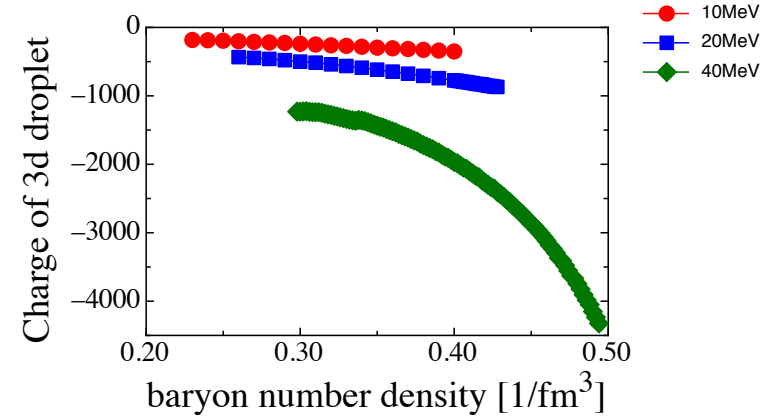
$$\mu = 0.1194 \frac{n_i (Ze)^2}{a}$$

strohmayer et al., 1991

n_i : number density of quark droplet
 Z : charge of quark droplet
 a : spacing of quark droplet

Shear Modulus

- $\mu \sim 10^{-10} - 10^{-9}$ in crust
- $\mu \sim 10^{-7} - 10^{-6}$ in HQ mixed phase
 - number of “charge” is quite different

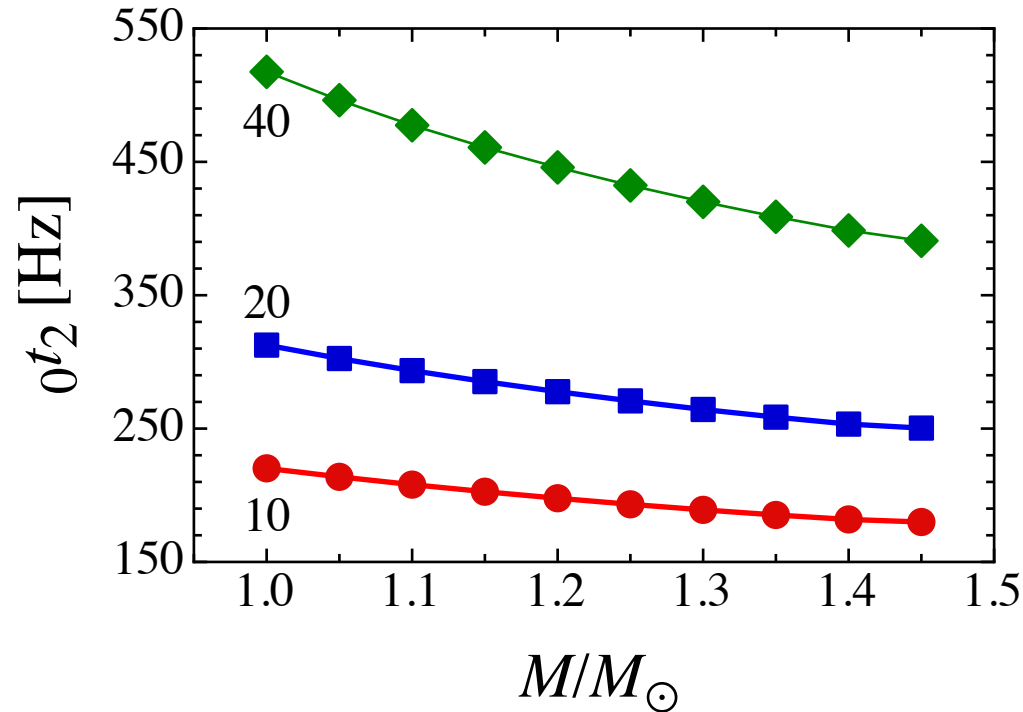


Estimations

- Compared with crust properties,
 - μ becomes $\sim 10^3$ times larger
 - ρ becomes ~ 10 times larger
 - $v_s = (\mu / \rho)^{1/2}$ could be ~ 10 times larger
- Frequencies of shear oscillations $\propto v_s$
 - In HQ mixed phase, the frequencies of shear oscillations could become ~ 10 times larger than that in crust.

Fundamental Oscillations 1

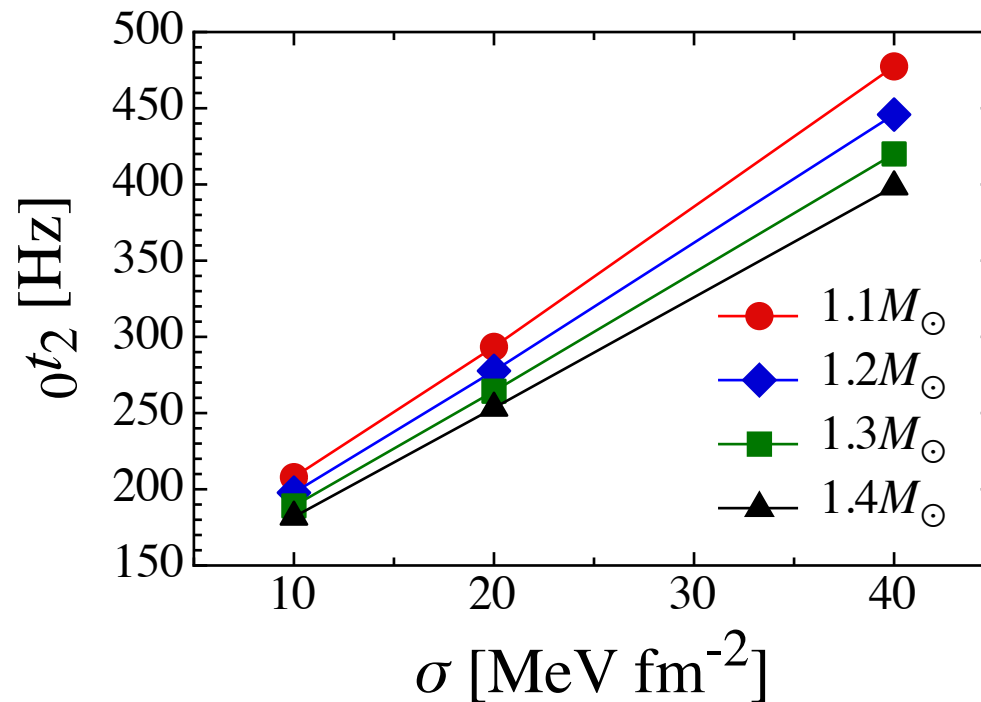
- Frequencies of fundamental shear oscillations as a function of stellar mass
 - those depend strongly on the surface tension



c.f.) ${}_0t_2$ in crust $\sim 20 - 30$ Hz

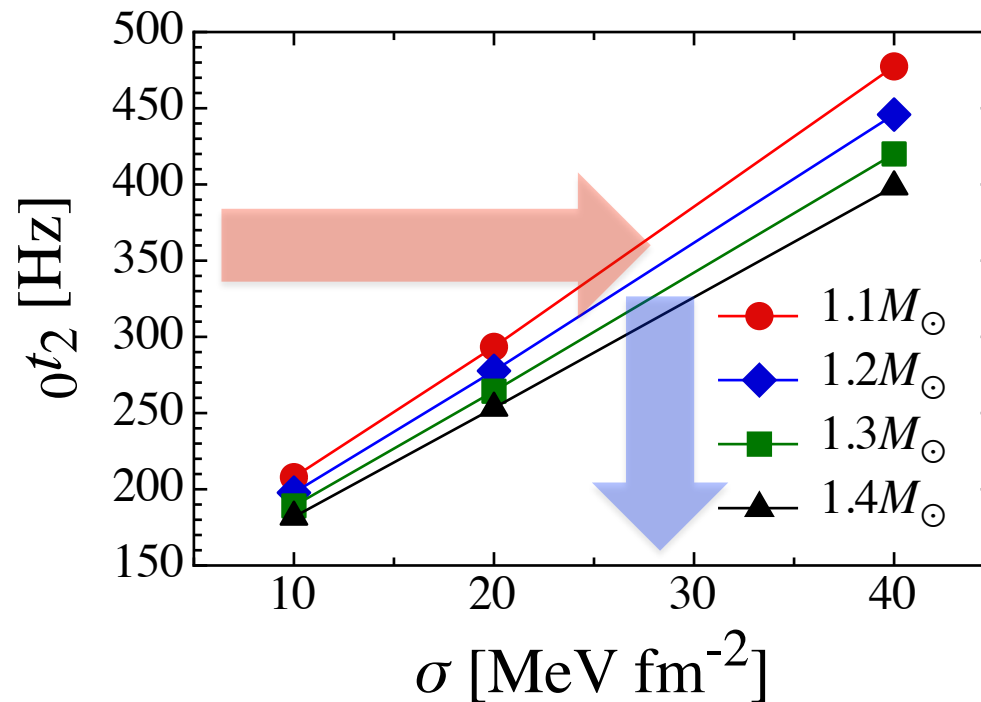
Fundamental Oscillations 2

- We find that the frequencies of fundamental shear oscillations are almost **proportional to σ** .
- With the help of the observation of stellar mass, it might be possible to obtain the value of σ .



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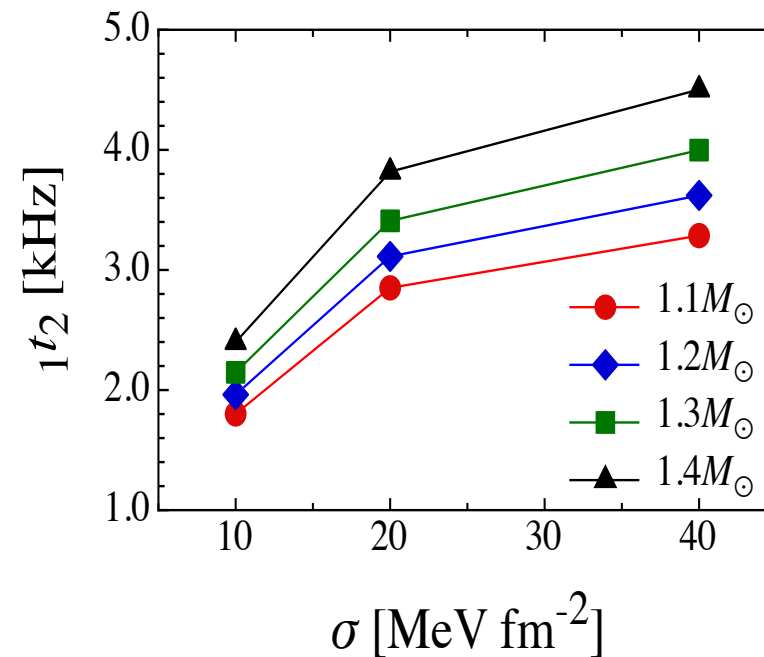
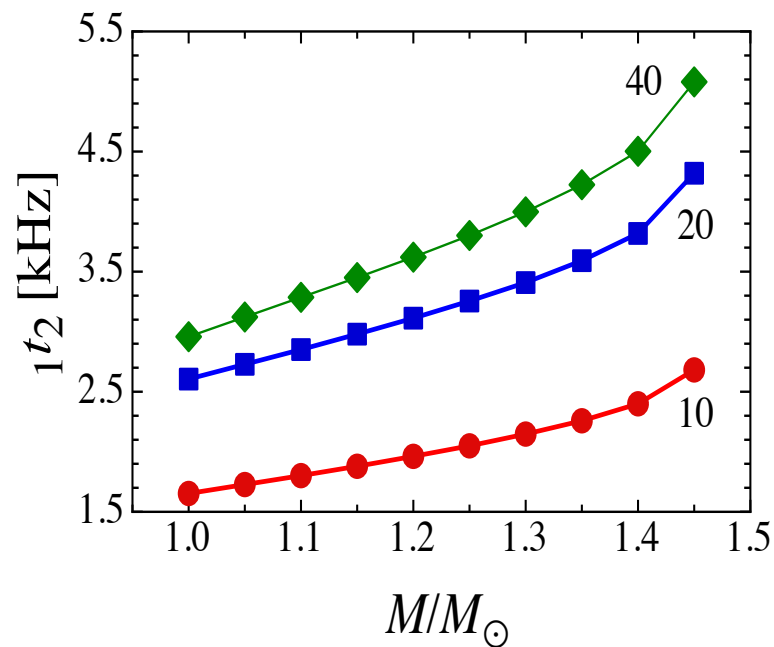


Conclusion

- We consider the **shear oscillations in hadron-quark mixed phase**, whose properties depends strongly on the surface tension.
- **Frequencies of shear oscillations in HQ phase becomes ~10 times larger** than those in crust.
- Frequencies of fundamental oscillations are **proportional to surface tension**.
- We show the possibility to determine the value of σ .
 - With the help of the observation of stellar mass, one might be possible to obtain the value of σ via the observation of shear oscillations.

1st Overtones

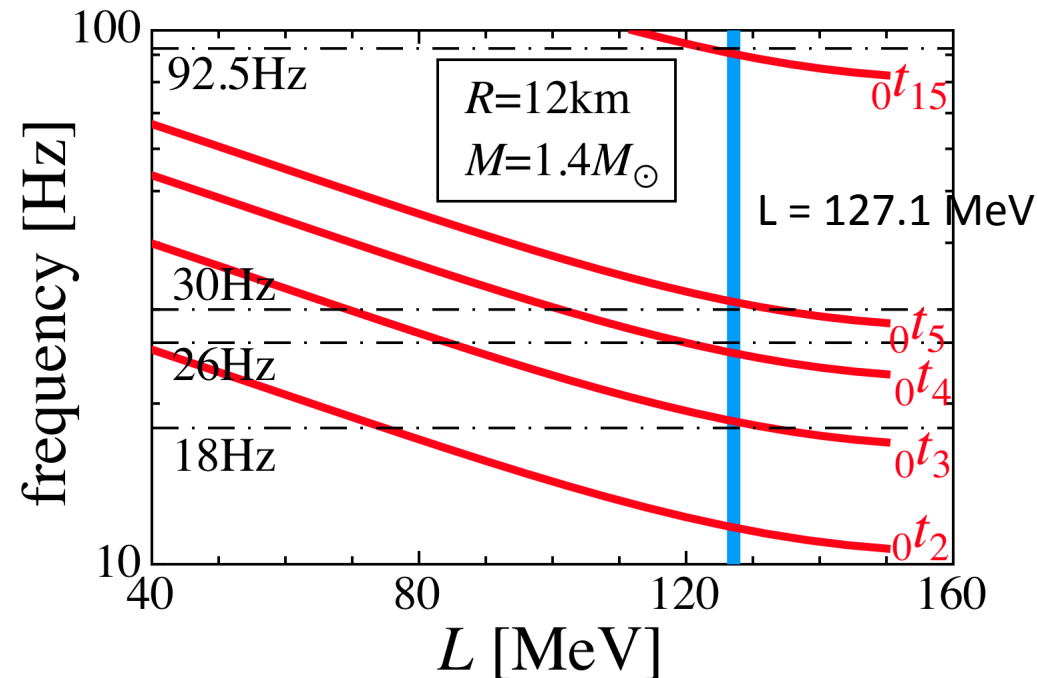
- Frequencies of 1st overtone shear oscillation as a function of stellar mass
- We can not see the linearity with respect to σ .



Comparison with QPO frequencies

HS+(2012b)

- Comparison of frequencies of torsional oscillations with the QPO frequencies observed in SGR 1806-20



- less than 5% accuracy