



Kenta Kiuchi, JGRG 22(2012)111406

“General relativistic simulations of magnetized binary neutron
star merger”

**RESCEU SYMPOSIUM ON
GENERAL RELATIVITY AND GRAVITATION**

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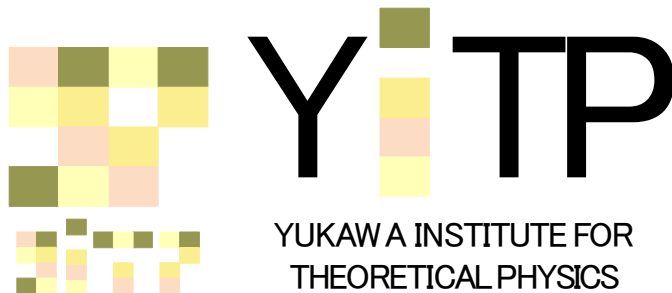
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General relativistic simulation of magnetized binary neutron star mergers

Kenta Kiuchi

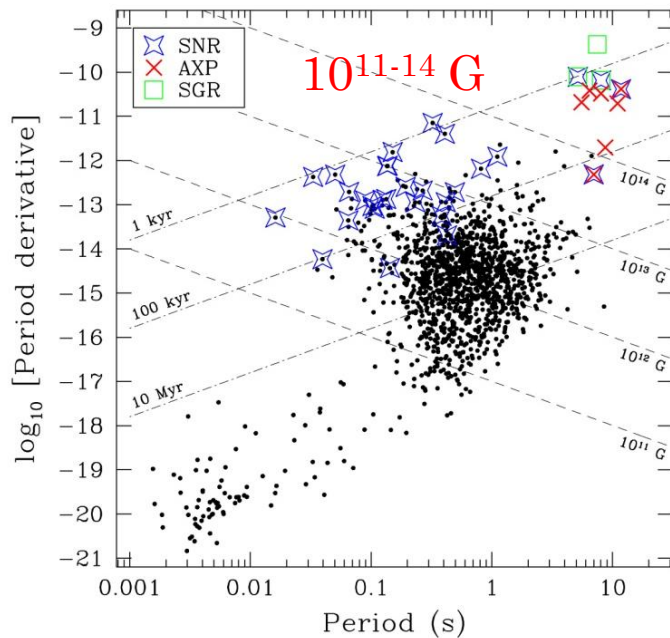
Collaborators : Masaru Shibata, Koutarou Kyutoku, Yuichiro Sekiguchi, Kenta Hotokezaka



Magnetized Binary Neutron Star Mergers

Neutron stars have a magnetic field in general.

Magnetic Fields of NS (Manchester 04)



What about in binary neutron star mergers ?

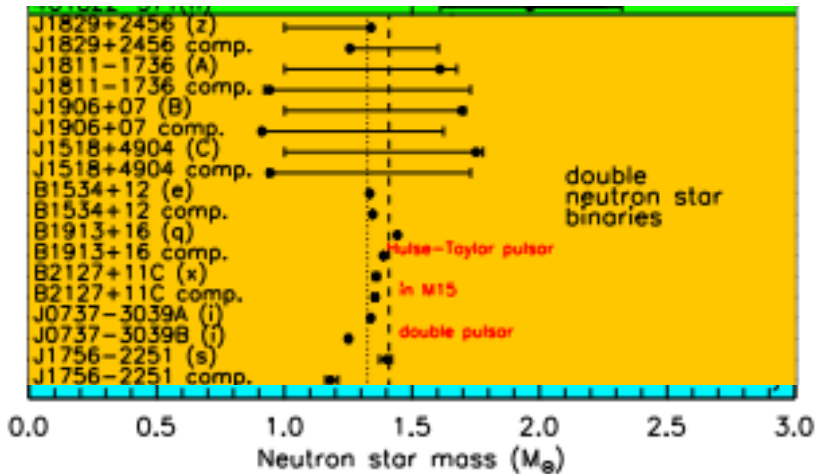
Possible amplification processes

- ▶ **Kelvin-Helmholtz instability** (Price-Rosswog 06, Gaicomazzo+ 11) @merger
- ▶ **Magnetorotational instability** (Balbus-Hawley 98, Rezzolla+ 11) in HMNS / disk
- ▶ Compression
- ▶ Magnetic winding

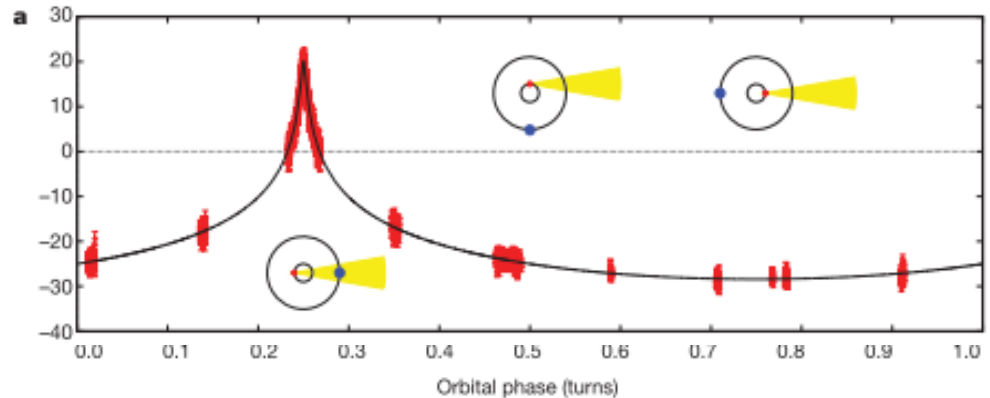
Spin period

Outcome of binary neutron star mergers

Mass of observed NSs
(Lattimer & Paraksh 06)



Shapiro-Time delay of PSR J1614-2230
(Demorest+ 10)



- ▶ Canonical mass of BNS = $2.7-2.8 M_{\odot}$
- ▶ Maximum mass of spherical NS = $1.97 \pm 0.04 M_{\odot}$

Long-lived Hyper Massive Neutron Star (HMNS) would be formed after the merger

⇒ Magnetic fields would be an important player in binary neutron star mergers, e.g., angular momentum transport etc.

NR simulations for magnetized BNS mergers

- ✓ Albert Einstein Institute (Giacomazzo+ 09, 11, Rezzolla+ 11)
 - Γ -law EOS
- ✓ Illinois University (Liu+ 08)
 - Γ -law EOS
- ✓ Louisiana University+ (Anderson+ 08)
 - Γ -law EOS

All the simulations have been done so far

- **Relatively short duration $\lesssim 20$ ms** after merger or BH formation
- Applied only **Γ -law EOS**

Our motivation

- **Long term simulation** for exploring the magnetic amplification process
- Adopt **the nuclear theory based EOS**



GRMHD simulation of magnetized BNS mergers

Set up

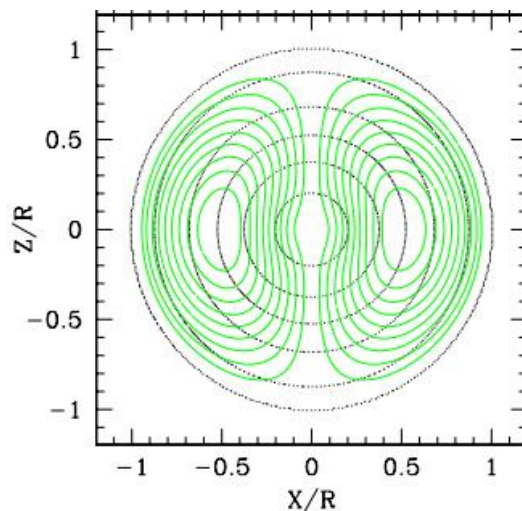
- ▶ Equation of State : H4 based on RMF (Gledenning & Moszkowski 91)

$M_{\max} \gtrsim 2.03 M_{\odot}$ and Γ -law for thermal part ($\Gamma_{\text{th}}=1.8$)

$$P = P_{\text{cold}} + P_{\text{th}}$$

- ▶ BNS mass : $2.7 M_{\odot}$, $2.8 M_{\odot}$ (Equal mass system)
- ▶ Magnetic fields configuration : Confined

Confined field line (Liu+08)



GRMHD simulation of magnetized BNS mergers

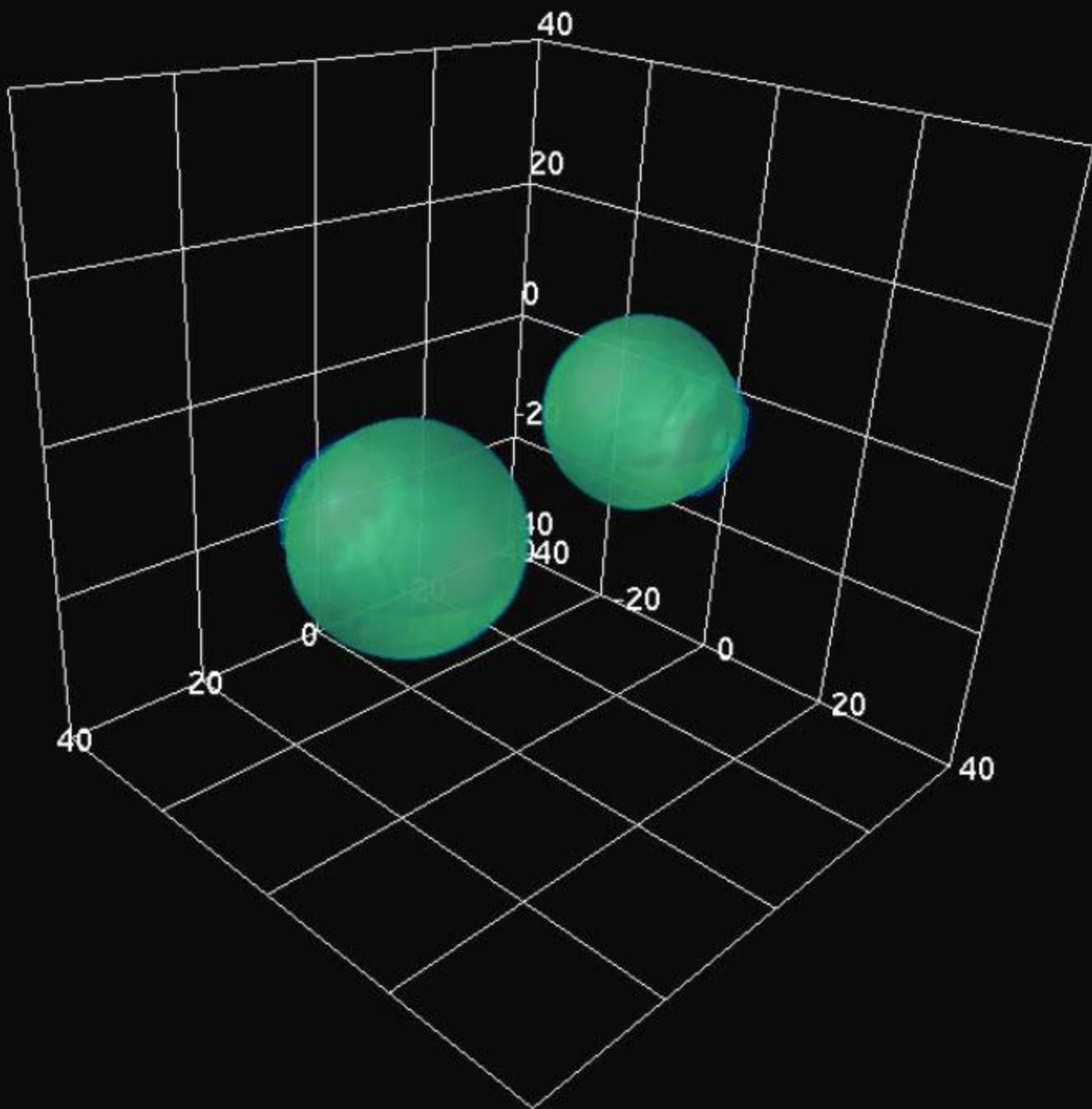
- Code description : FMR – GRMHD code based on Balsara's method preserving $\text{Div} \cdot \mathbf{B} = 0$ as well as **the magnetic flux conservation** (KK+ 12)

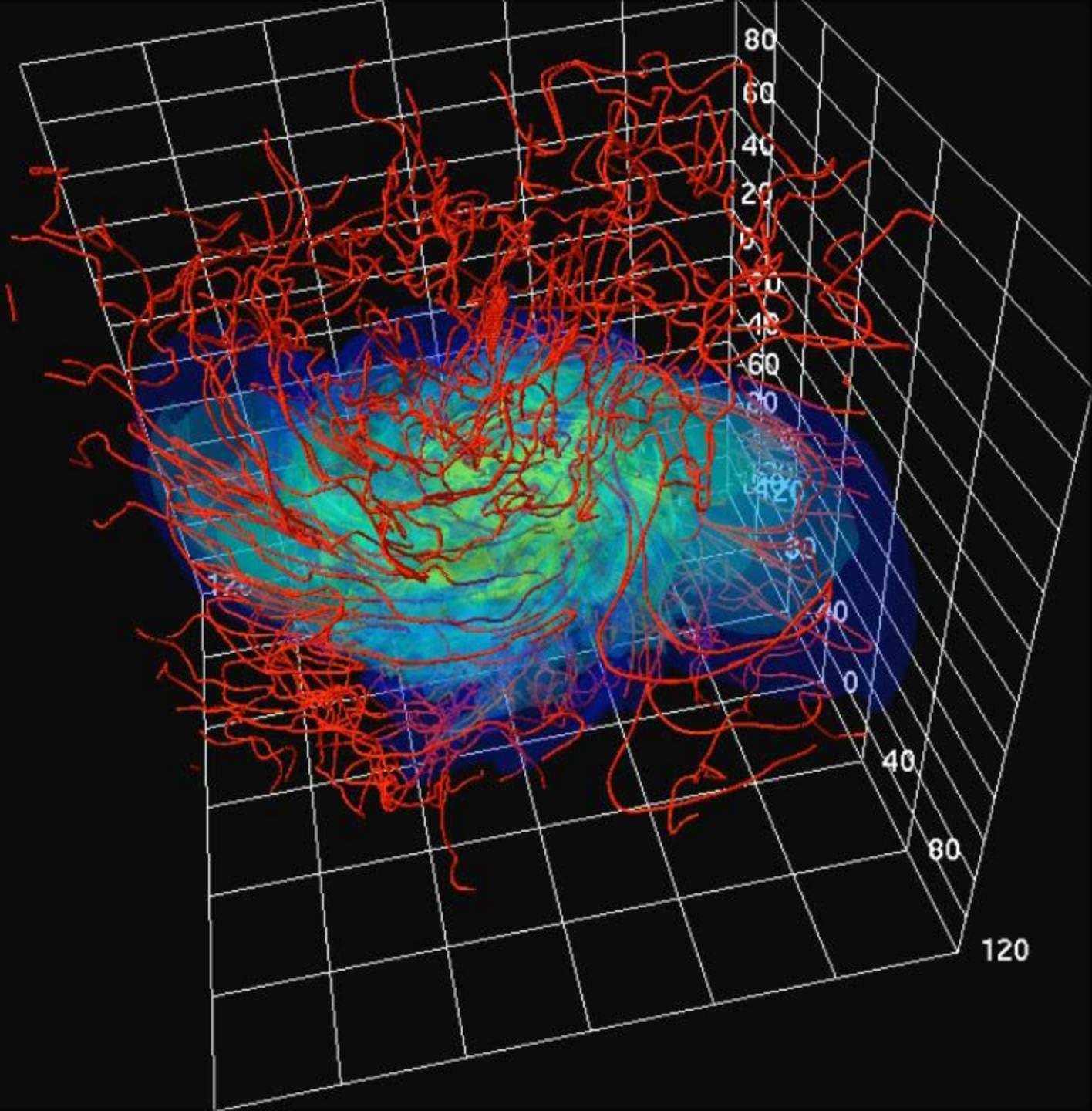
Formulation and Numerical scheme

- Baumgarte-Shapiro-Shibata-Nakamura formulation (Shibata-Nakamura 95, Baumgarte-Shapiro 99)
- 4th-order FD in space and time for the Einstein eqs.
- LLF flux and 3rd-order reconstruction for MHD
- Weno5 for reconstruction in the refinement boundary

Resolution Study

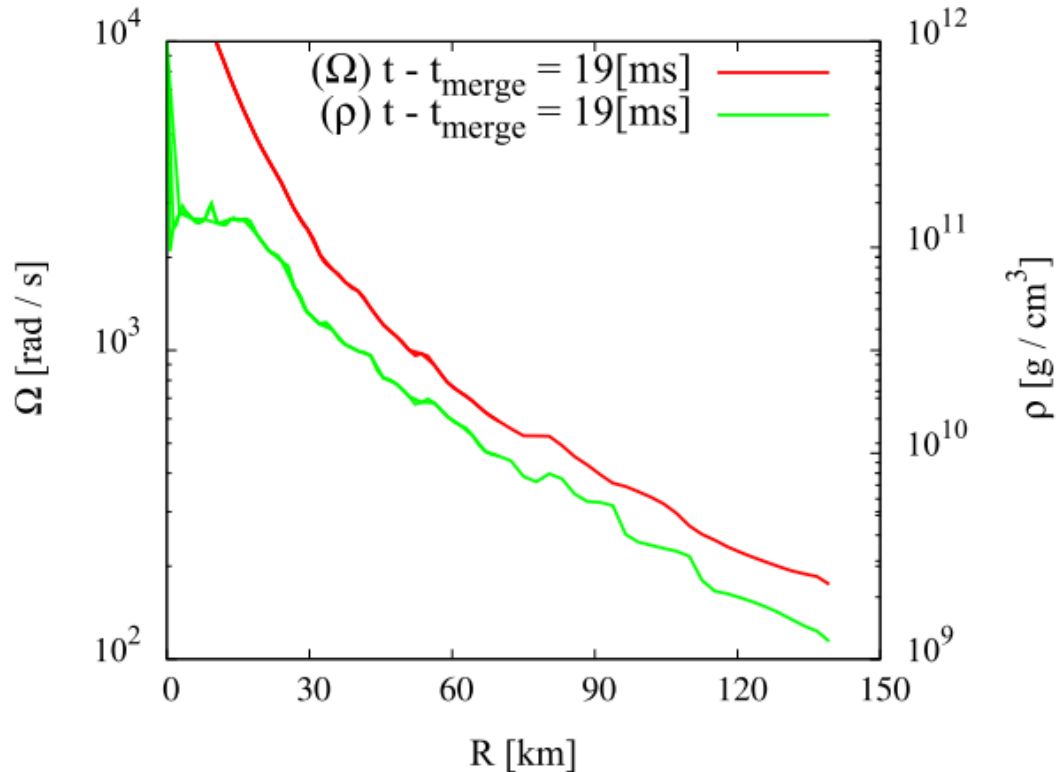
- High resolution $\Delta x = 230$ m (NS covered by 100 grid points)
- Medium resolution $\Delta x = 288$ m (NS covered by 80 grid points)
- Low resolution $\Delta x = 384$ m (NS covered by 60 grid points)





Property of BH and torus

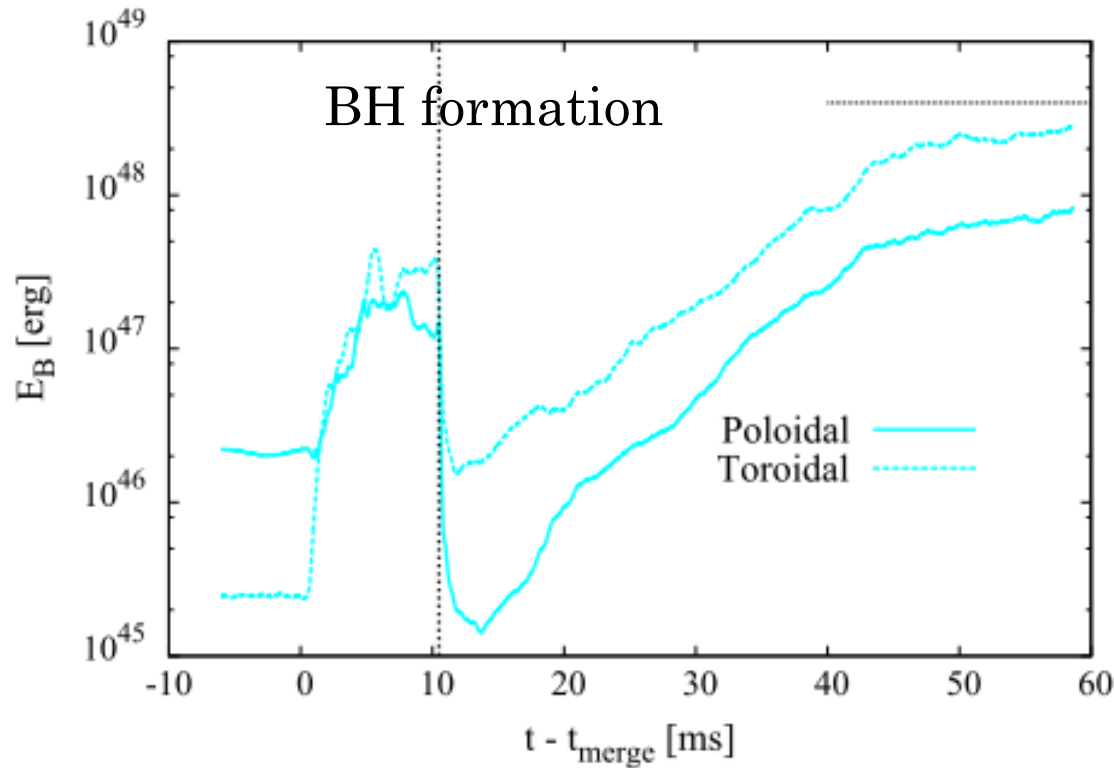
Density and angular velocity profile along x-axis



- ▶ Mass of BH is $2.6\text{-}2.7 M_{\odot}$ and spin of BH is ≈ 0.7
- ▶ Almost Keplerian profile ($\propto R^{-3/2}$)
- ▶ Torus mass $\approx 0.03\text{-}0.04 M_{\odot}$ @ 30 ms after BH formation
- ▶ MRI wavelength would be larger compared to HMNS, e.g.,
 $\rho \approx 10^{15} \text{ g / cm}^3$

Magnetic field amplification ($2.8 M_{\odot}$ - confined model)

Magnetic field energy



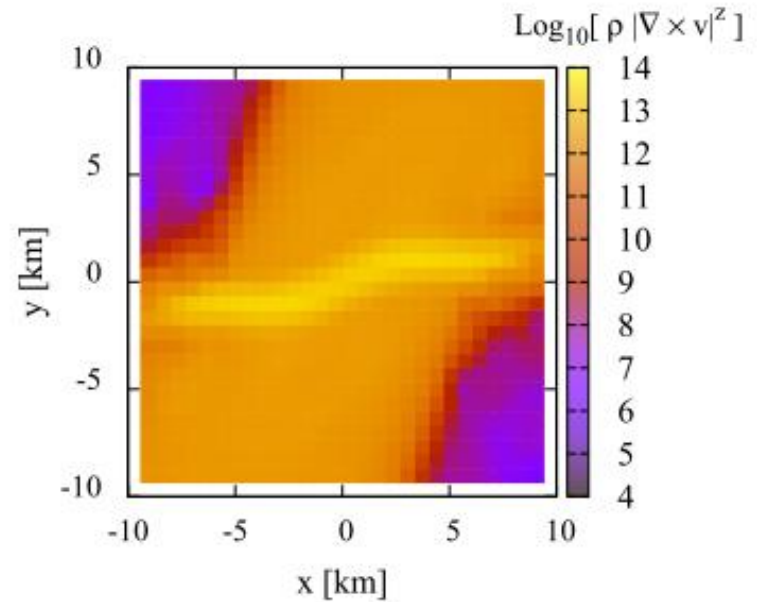
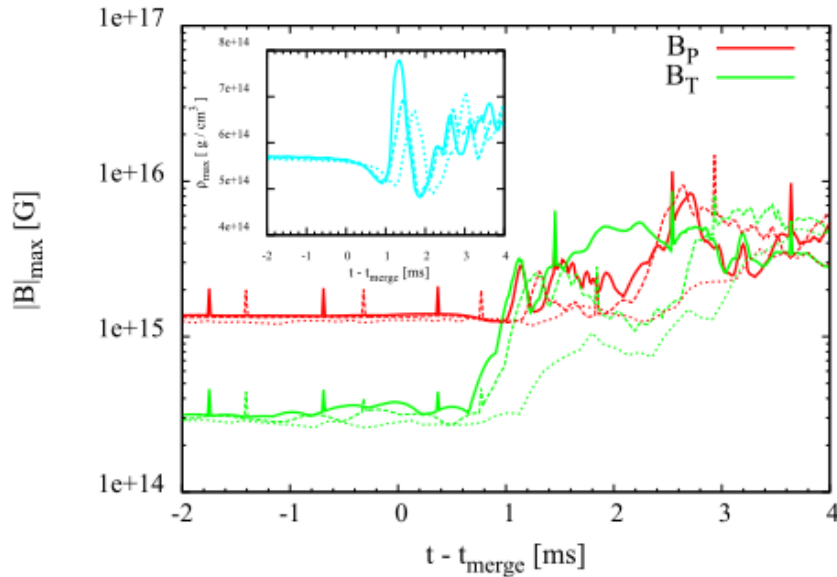
- ▶ Rapid increase at $t - t_{\text{merge}} \approx 0$ ms
- ▶ Slow increase in the HMNS phase
- ▶ Exponential growth after the BH formation (inside the torus)



Rapid increase at $t - t_{\text{merge}} \approx 0$ ms

Vorticity @ $t - t_{\text{merge}} \approx 0$ ms

Magnetic field strength

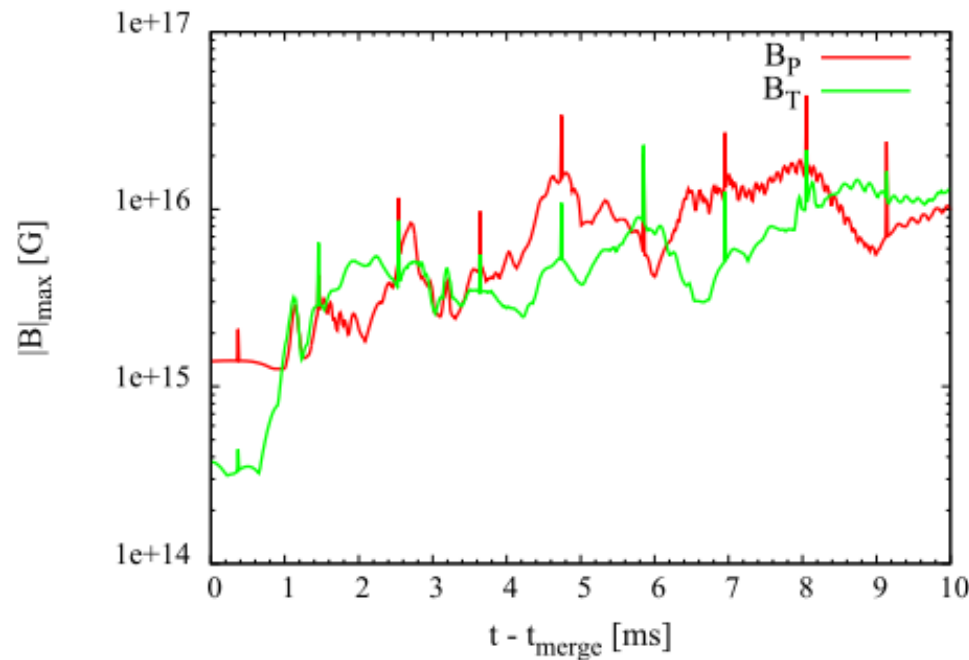


- ▶ **Poloidal field** increases by compression $\sim \rho^{2/3}$
- ▶ **Toroidal field** increases by the Kelvin-Helmholtz instability (Price-Rosswog 06, Anderson + 08, Gaicomazzo+ 11)
- ▶ Vortexes appear in the shear layer forming the two stars come into contact.



Slow increase in the HMNS phase

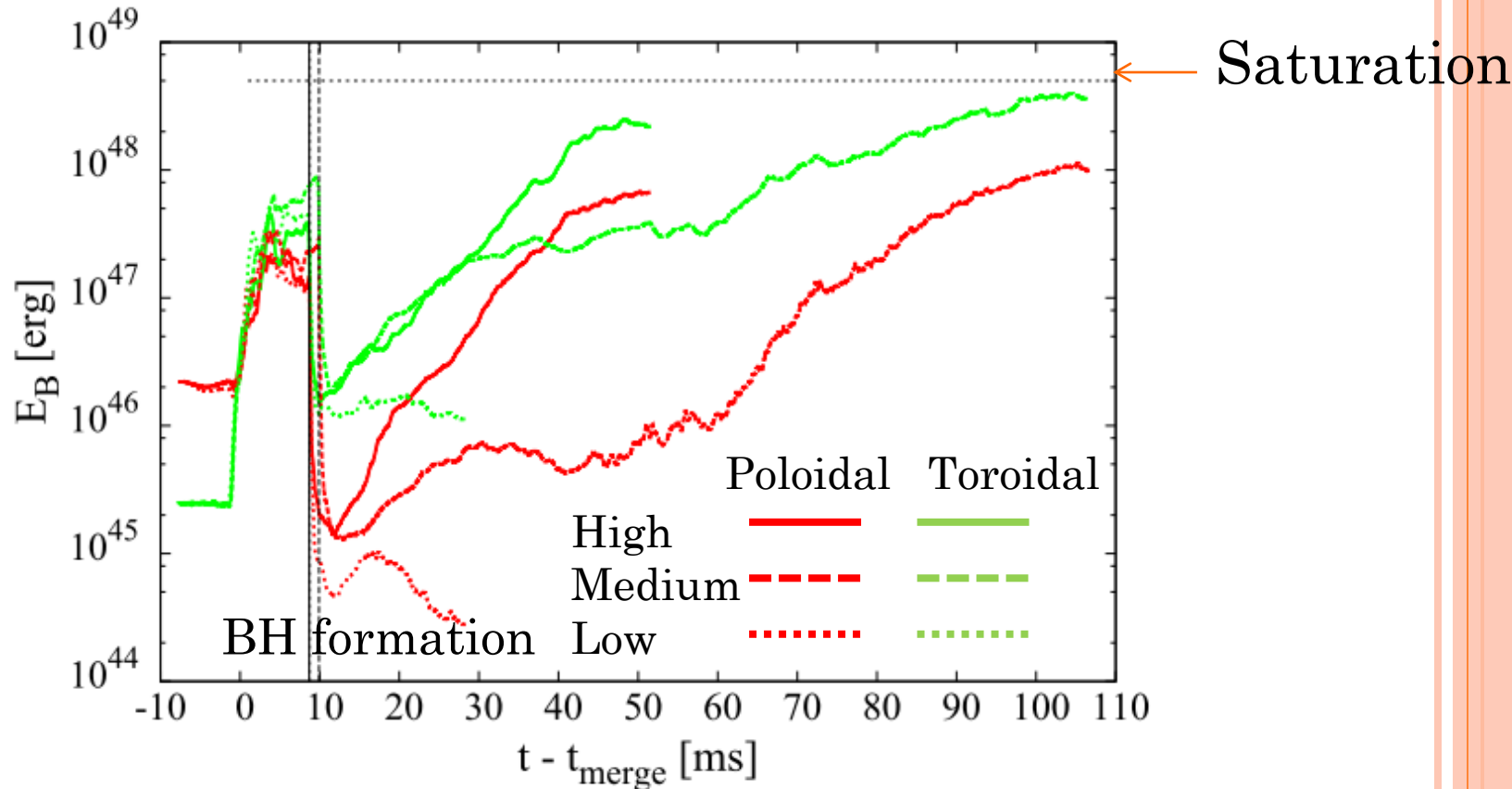
Magnetic field strength



- ▶ **Poloidal field** increases due to the compression
- ▶ **Toroidal field** increases by the magnetic winding
- ▶ Very short MRI wavelength, i.e., $\rho \sim 10^{15} \text{ g / cm}^3$

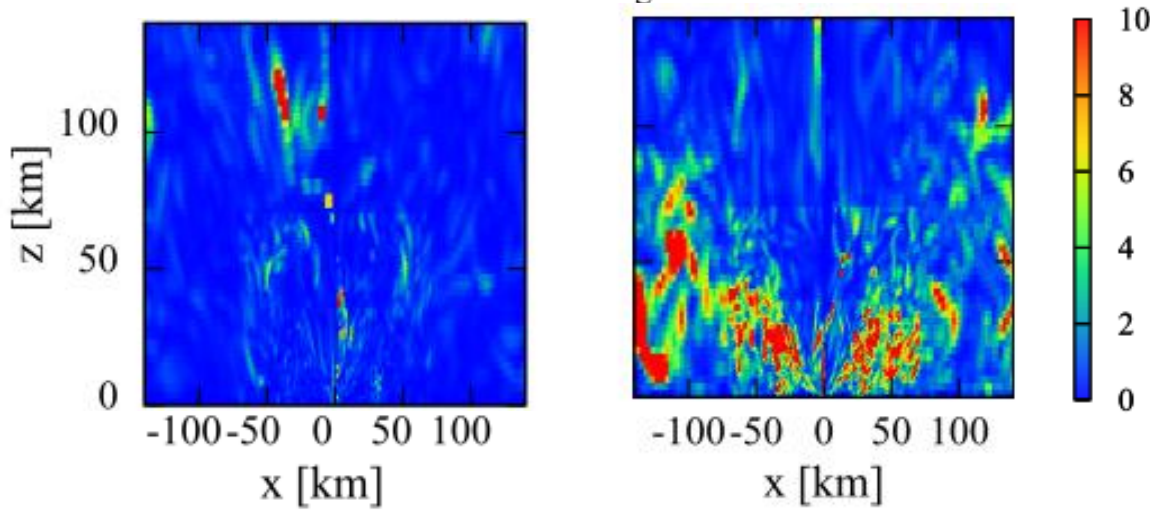
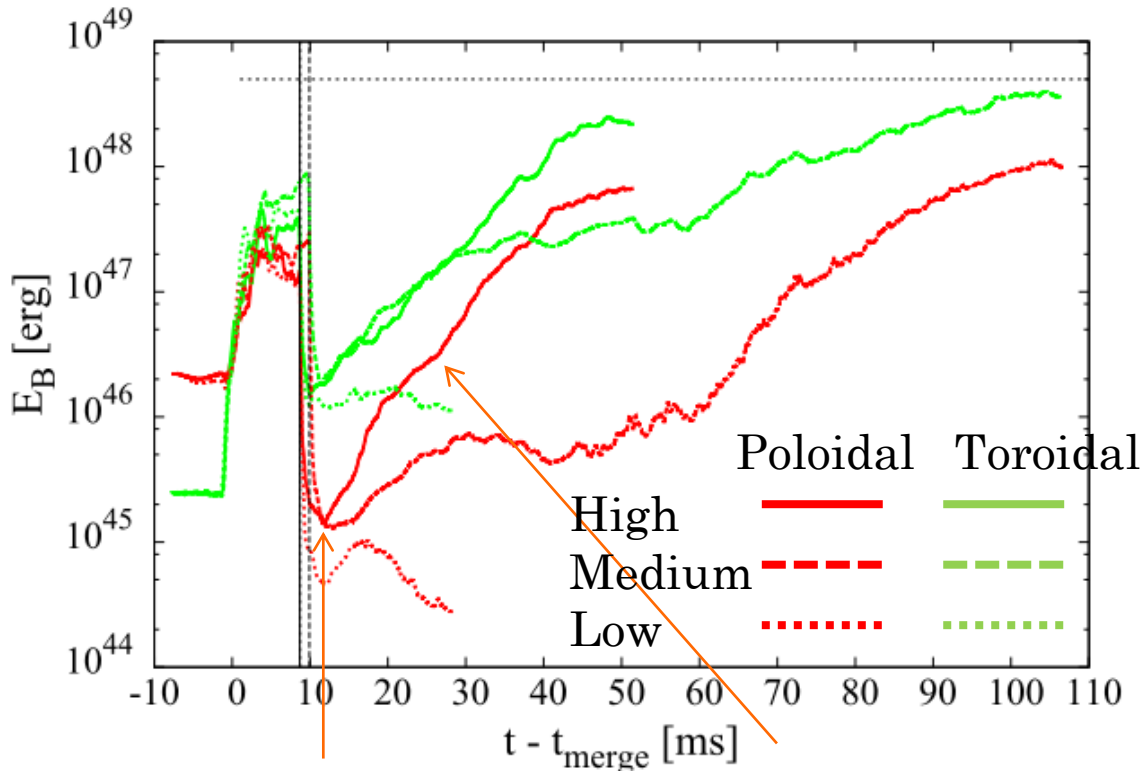


Exponential growth after the BH formation



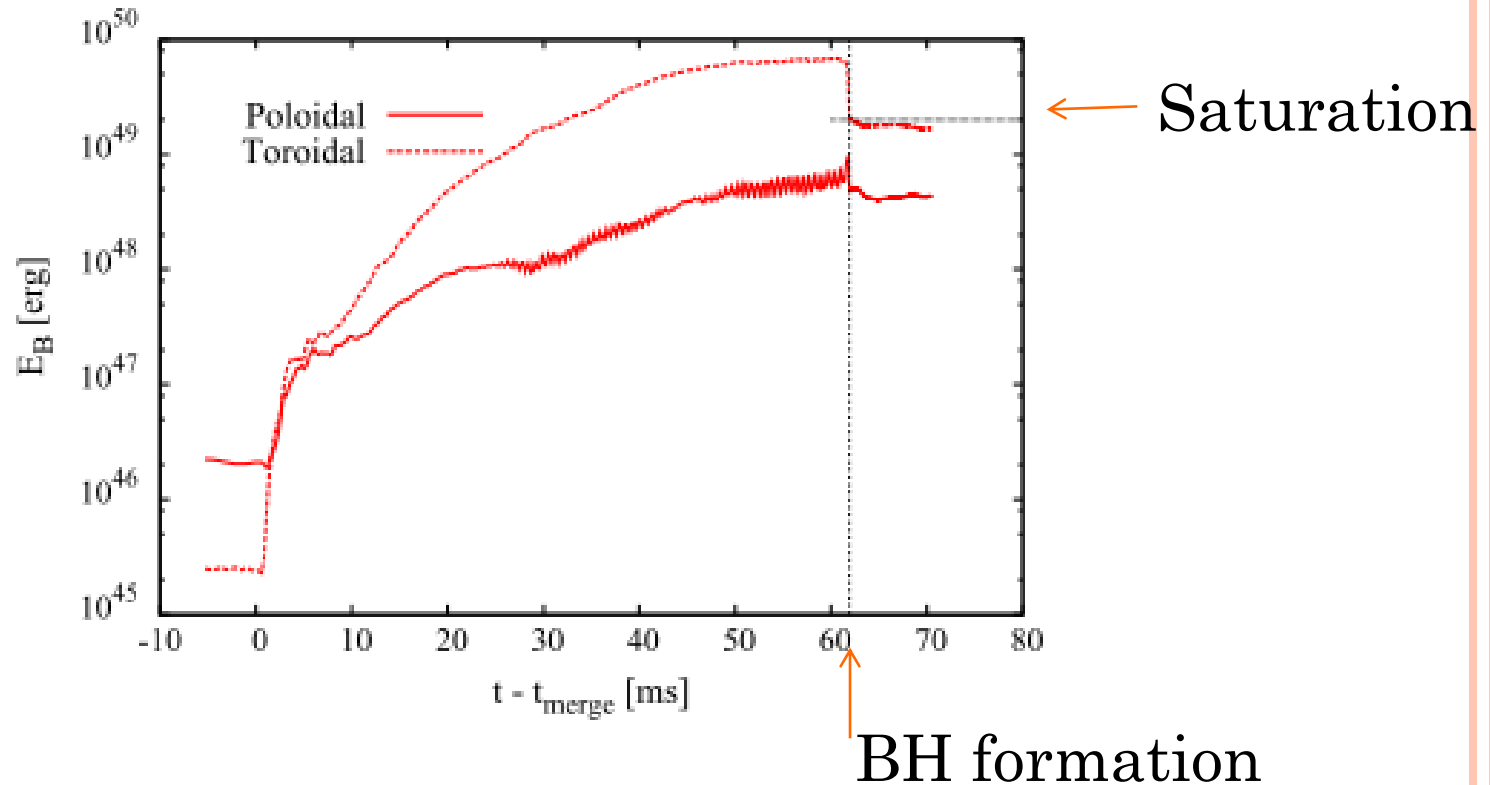
- ▶ Exponential growth in **the high resolution**, **not in the low resolution**, after the BH formation
- ▶ e-folding time ≈ 6 ms (high resolution model)
- ▶ Saturation level $\approx 3-5 \times 10^{48}$ erg (1-2 % of kinetic energy)

Grid resolution vs MRI wavelength



▶ **Red region**
 = MRI wavelength is
 covered by more than 10
 grid points

2.7 M_⊙ model



- ▶ Strong magnetic pressure for the confined model
- ▶ 2.7 M_⊙ model is marginally stable
- ▶ Already reaches to a saturation level $\approx 2 \times 10^{49}$ erg (3-5 % of kinetic energy)



Mass ejection

Mass ejection is important for the electromagnetic counter part of BNS mergers

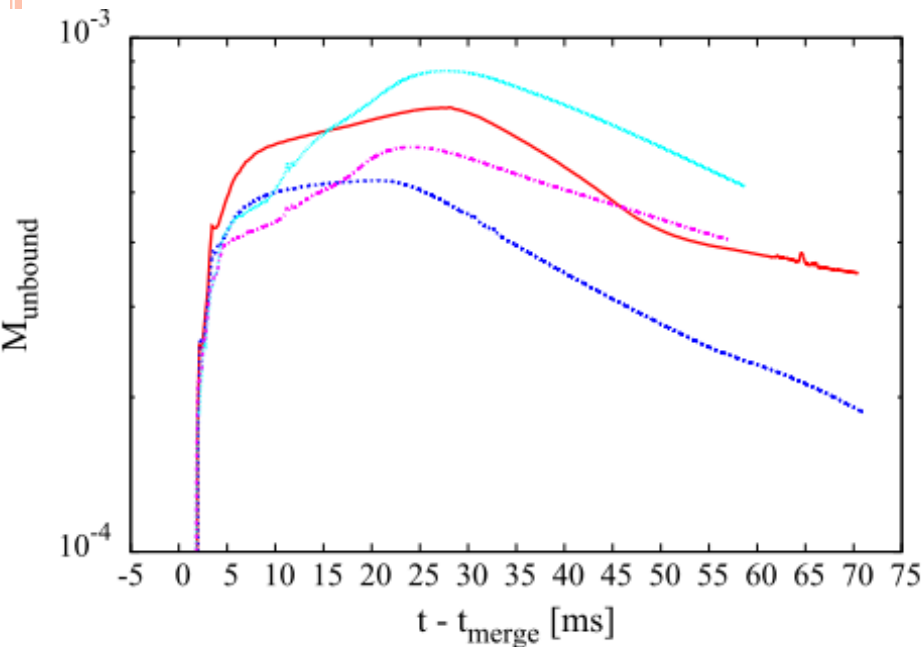
▸ synchrotron radiation (radio) (Nakar & Piran 11)

$$\sim 2.5 \text{ mJy } (E_0/10^{49} \text{ erg})(n_0/1 \text{ cm}^{-3})^{1/2} (\beta/0.2)^{-1} (D/300 \text{ Mpc})^{-2}$$

▸ r-process elements (optical) (Li-Paczynski 98, Metzger+10, 12)

$$t_{\text{peak}} \sim 0.1 \text{ day } (\beta/0.2)^{-1/2} (M_{\text{eje}}/10^{-3} M_{\odot})^{1/2}$$

$$L_{\text{peak}} \sim 7 \times 10^{41} \text{ erg/s } (f/3 \times 10^{-6}) (\beta/0.2)^{1/2} (M_{\text{eje}}/10^{-3} M_{\odot})^{1/2}$$



▸ Rapid rise due to the gravitational torque @ the merger

▸ $M_{\text{eje}} \approx \text{several} \times 10^{-4} M_{\odot}$

▸ Kinetic energy $E_0 \approx 10^{49-50} \text{ erg}$

Summary for magnetized BNS mergers

- ▶ Torus around the BH is subject to the MRI

Long term and high-resolution simulation is essential

- ▶ Turbulent magnetic field develops inside the torus
- ▶ Saturation of MRI : magnetic energy \approx 1-5 % of kinetic energy

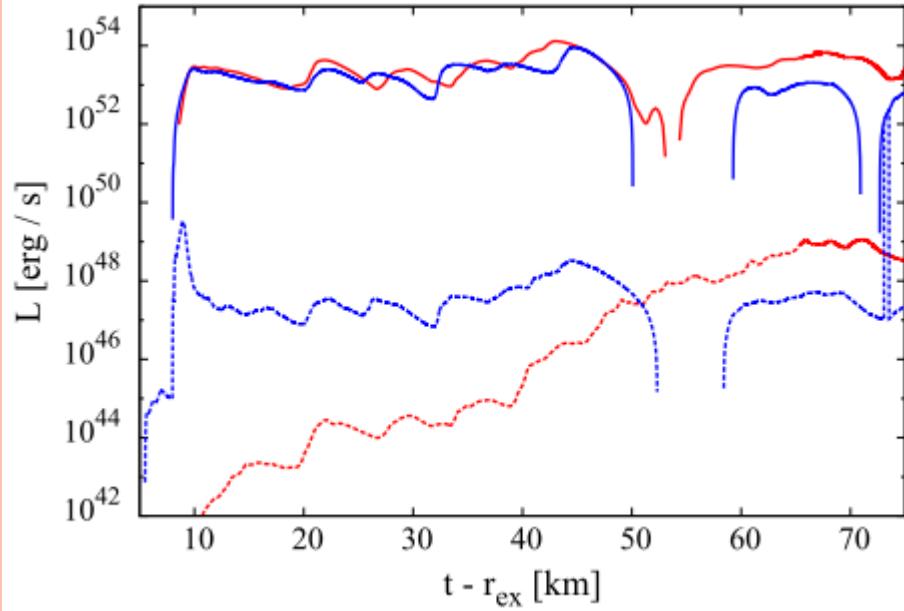
Future work

- ▶ Higher resolution simulation, ultimately $\Delta x \approx 100$ m on K computer
- ▶ Weak magnetic field, e.g., 10^{11-13} G for observed NSs
- ▶ Systematic study for EOS
- ▶ Equilibrium configuration of magnetized binary neutron stars as initial conditions

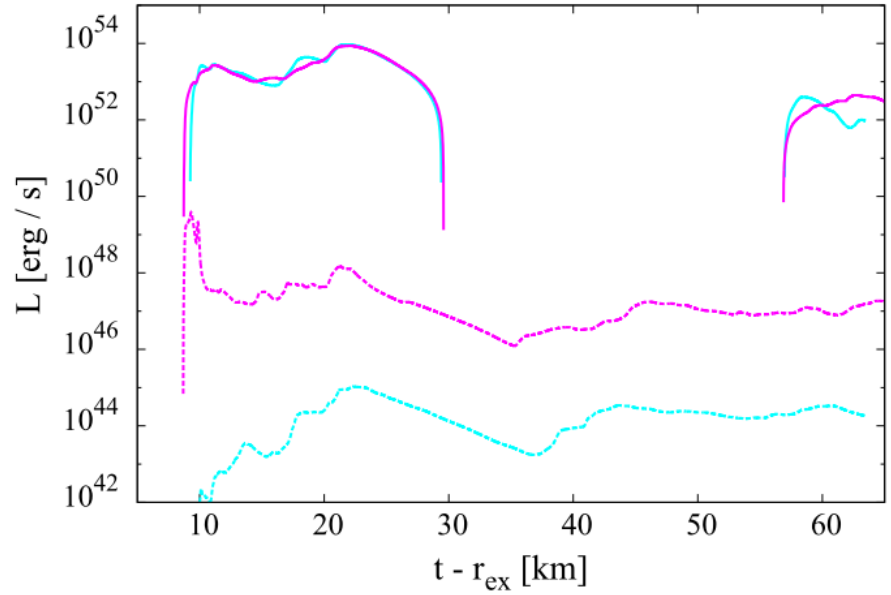


Luminosity

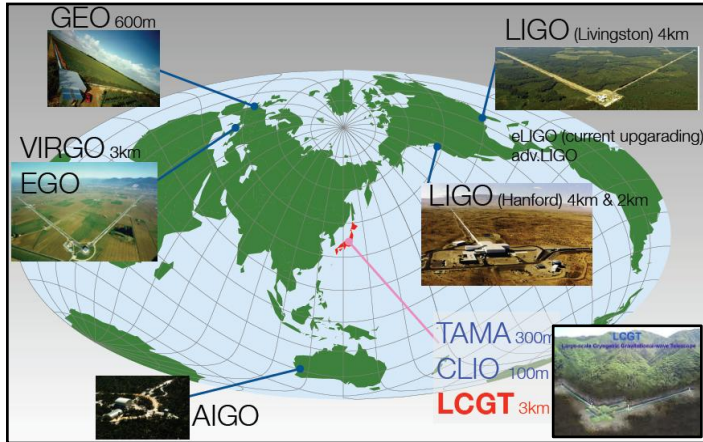
2.7 M_{\odot} model



2.8 M_{\odot} model



Gravitational wave astronomy and binary neutron star mergers



Gravitational waves

- ▶ Imprinting “raw” information of sources
- ▶ Extremely weak signal, $h_c \sim 10^{-22}$

Binary neutron star (BNS) mergers

- ▶ Promising source of GWs : 10 events / yr for KAGRA
- ▶ High-end laboratory for the nuclear theory :

Reconstruction of Mass-Radius relation

- ▶ Theoretical candidate of Short-Gamma-Ray Burst (Narayan+ 92)



Numerical Relativity

BNS mergers

- ▶ Density $\sim 10^{15}$ g / cm³ (Strong interaction)
- ▶ Temperature $\sim 10^{11}$ K (Weak interaction)
- ▶ Strong gravity (Gravity)
- ▶ Magnetic field $\sim 10^{11-14}$ Gauss (Electromagnetic force)

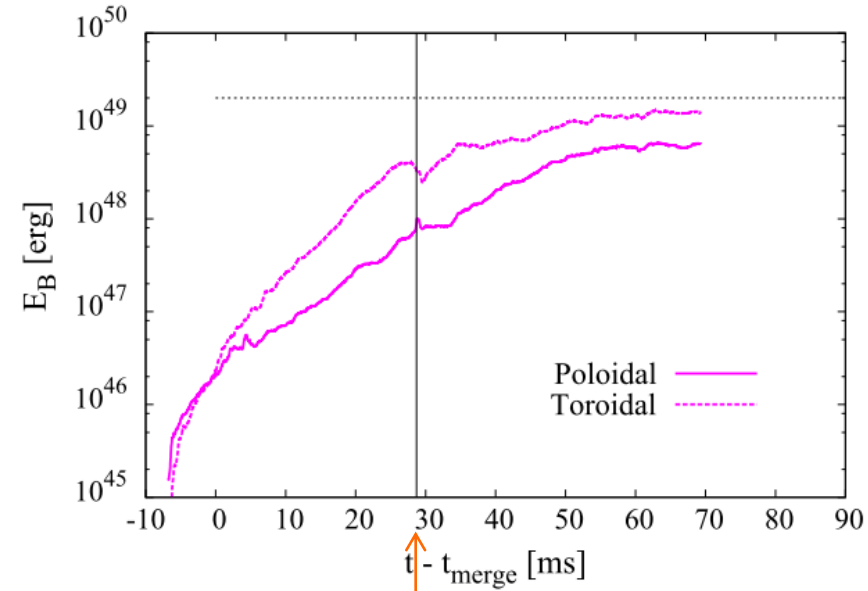
Numerical Relativity : Simultaneously solving

- ▶ the Einstein equations
- ▶ Relativistic (magneto) hydrodynamics
- ▶ Radiation field for neutrino

Unique approach to explore phenomena in strong gravity

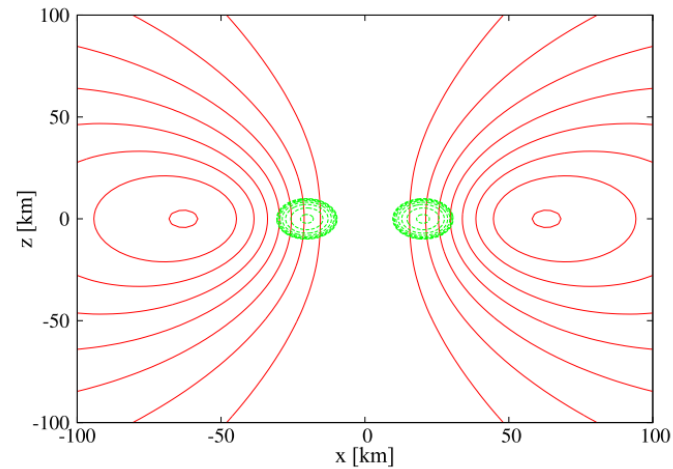


Dipole model

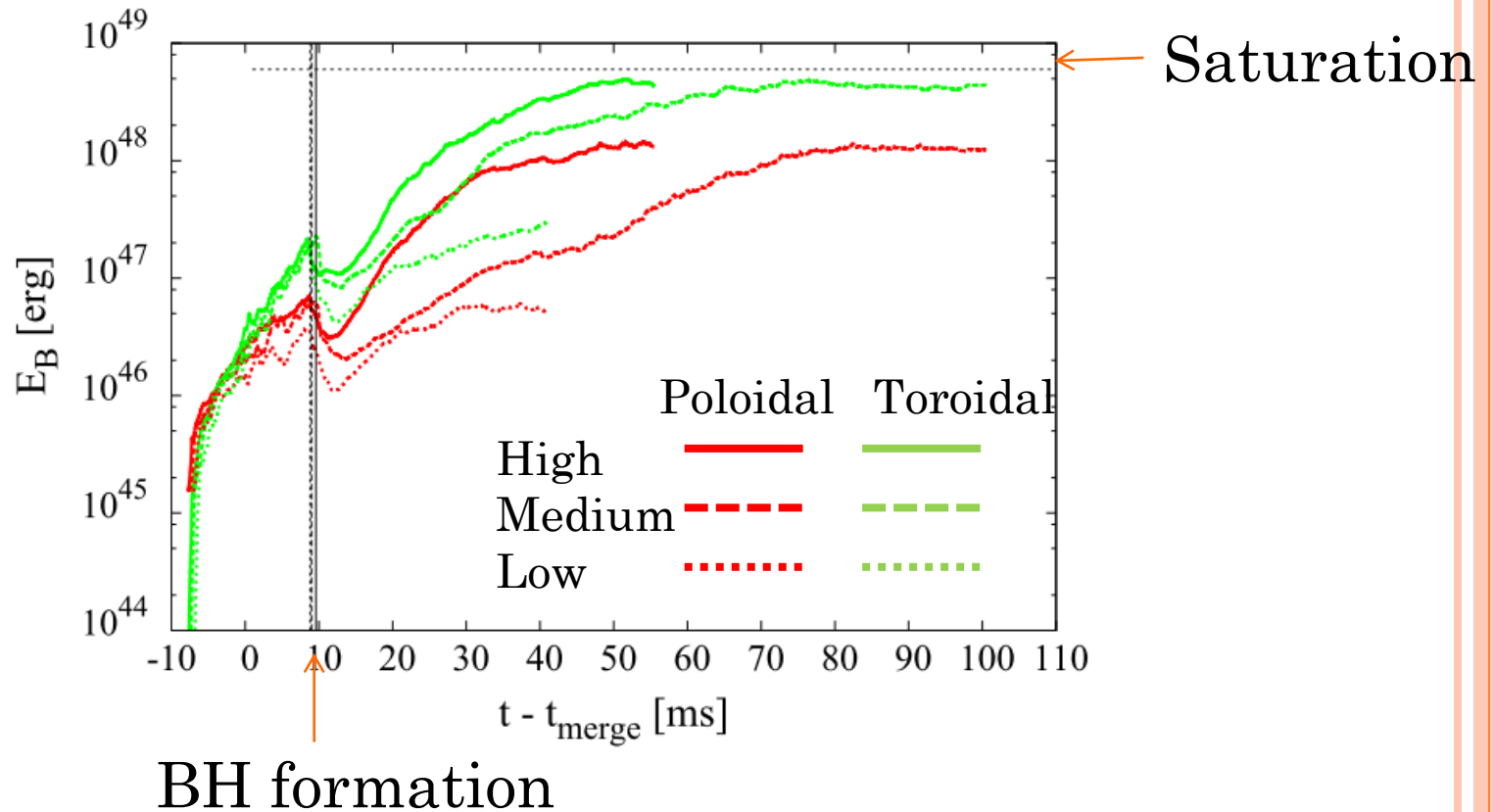


BH formation

Dipole field line



2.8 M_⊙ - Dipole model



- ▶ Exponential growth in the high and middle resolution, not in the low resolution after the BH formation
- ▶ e-folding time ≈ 6 ms (high resolution model)
- ▶ Saturation level $\approx 6-7 \times 10^{48}$ erg (2-3 % of the kinetic energy)