

# Cosmological constraints on sterile neutrino mass in $f(R)$ gravity

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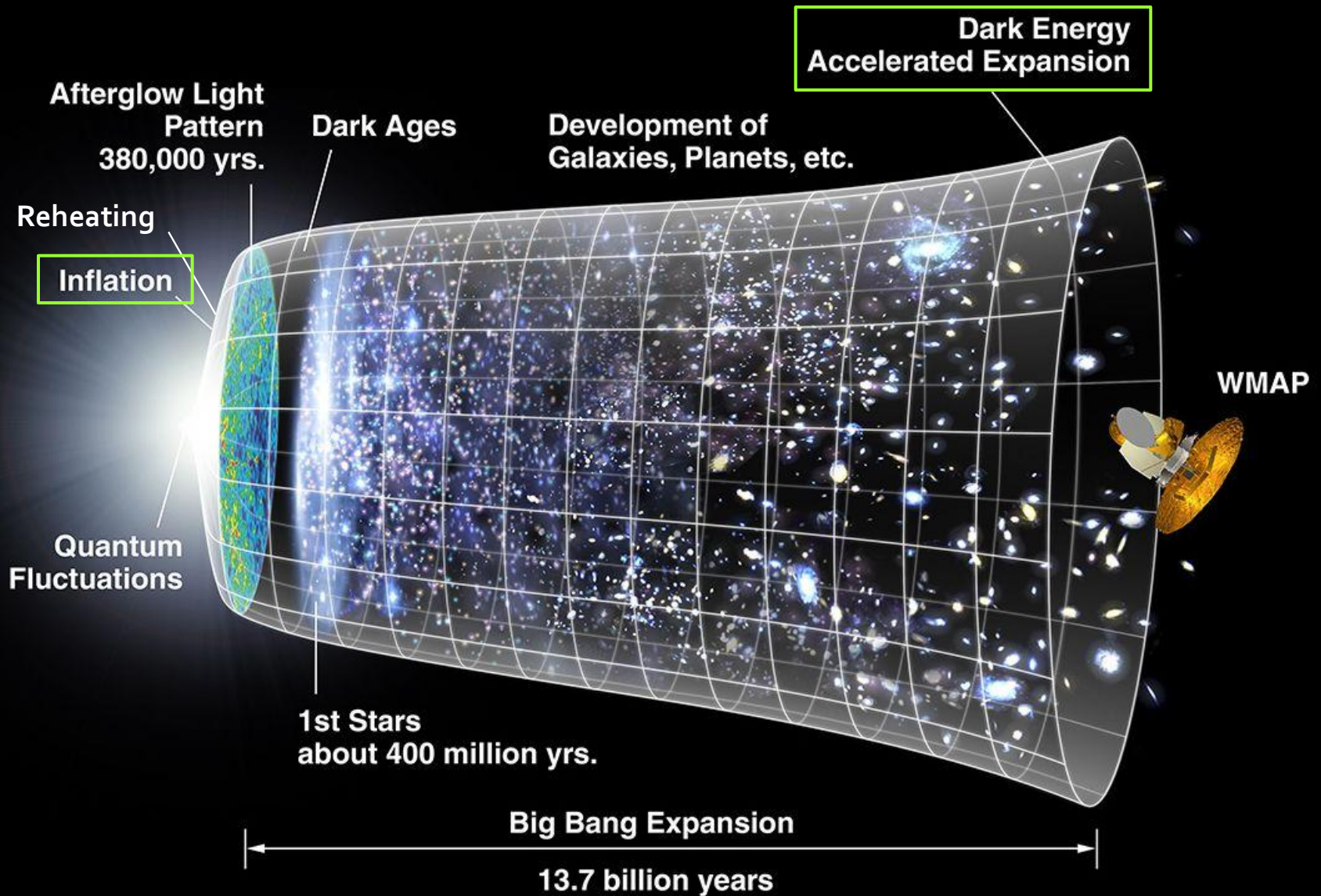
in collaboration with

Alexei A. Starobinsky (Landau Inst.)

Jun'ichi Yokoyama (RESCEU)



# Two regimes of accelerated expansion



# $f(R)$ gravity

can describe the accelerated expansion.

$$S = \frac{1}{16\pi G} \int d^4x \sqrt{-g} f(R) + S_m$$

Primordial inflation

Starobinsky, Phys.Lett. B91 (1980) 99

$$f(R) = R + \frac{R^2}{6M^2}$$

Late-time acceleration

Starobinsky, JETP Lett. 86, 157 (2007)  
[arXiv:0706.2041]

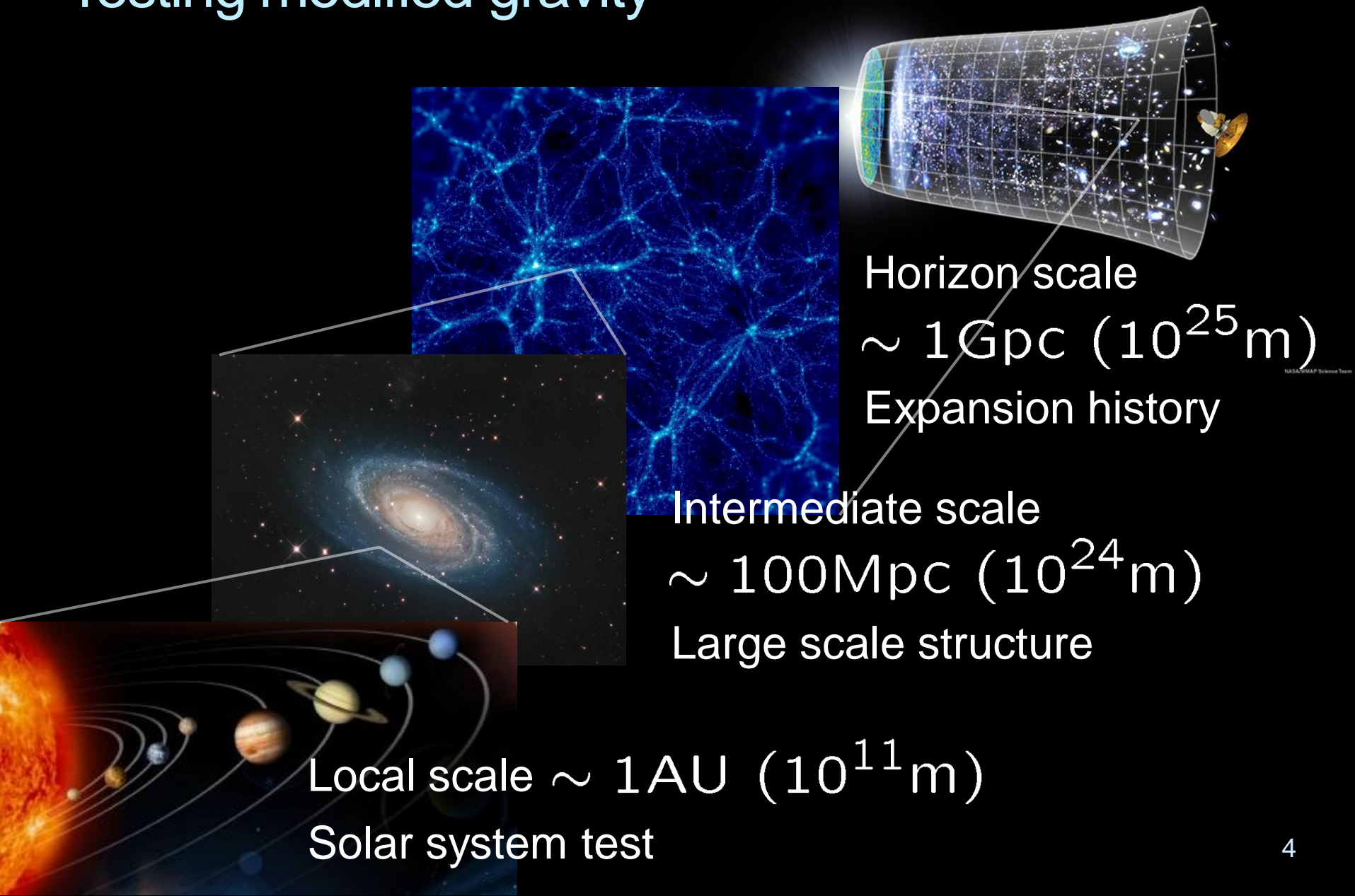
$$f(R) = R + \lambda R_s \left[ \left( \frac{R^2}{R_s^2} + 1 \right)^{-n} - 1 \right]$$

cf.  $f(R)$  model for both accelerated expansion

Appleby, Battye, Starobinsky, JCAP 1006, 005 (2010) [arXiv:0909.1737]

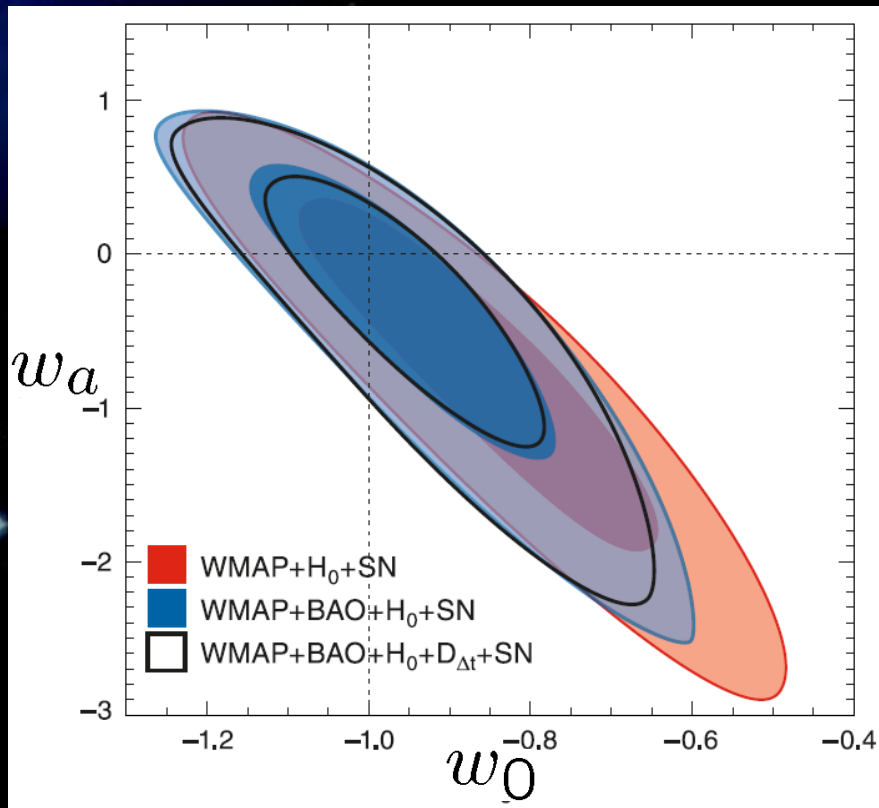
H.M., Nishizawa, PRD 86 (2012) 093514 [arXiv:1204.1472]

# Testing modified gravity

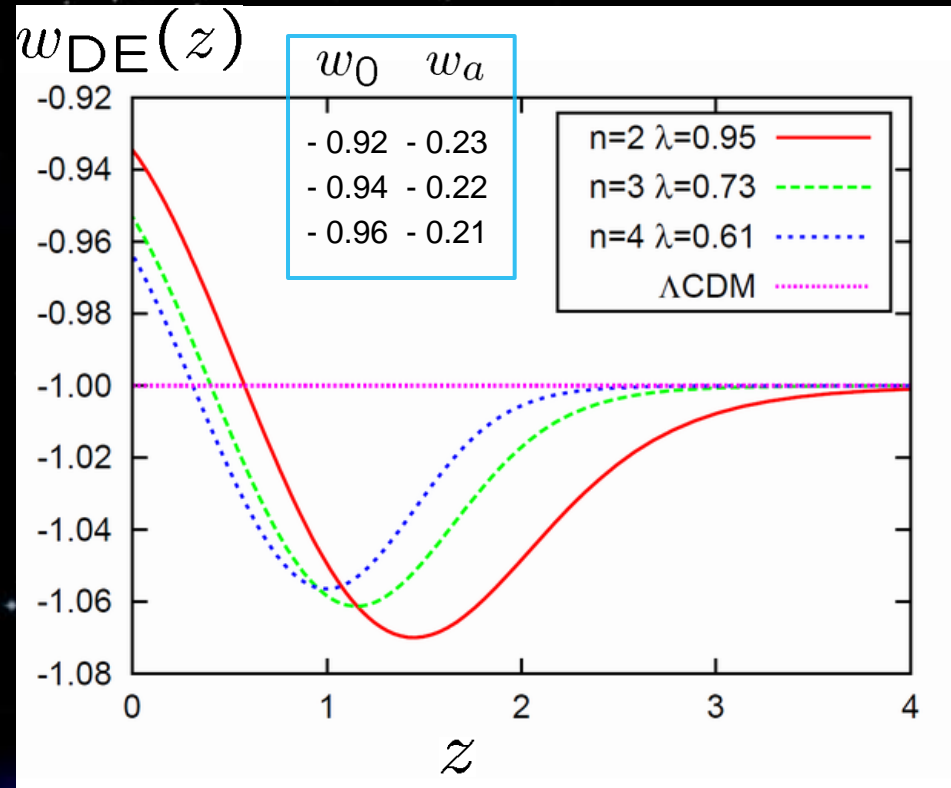


# Time variation of EoS parameter $w \equiv P/\rho$

$$w_{\text{DE}} = w_0 + \frac{w_a z}{1+z}$$



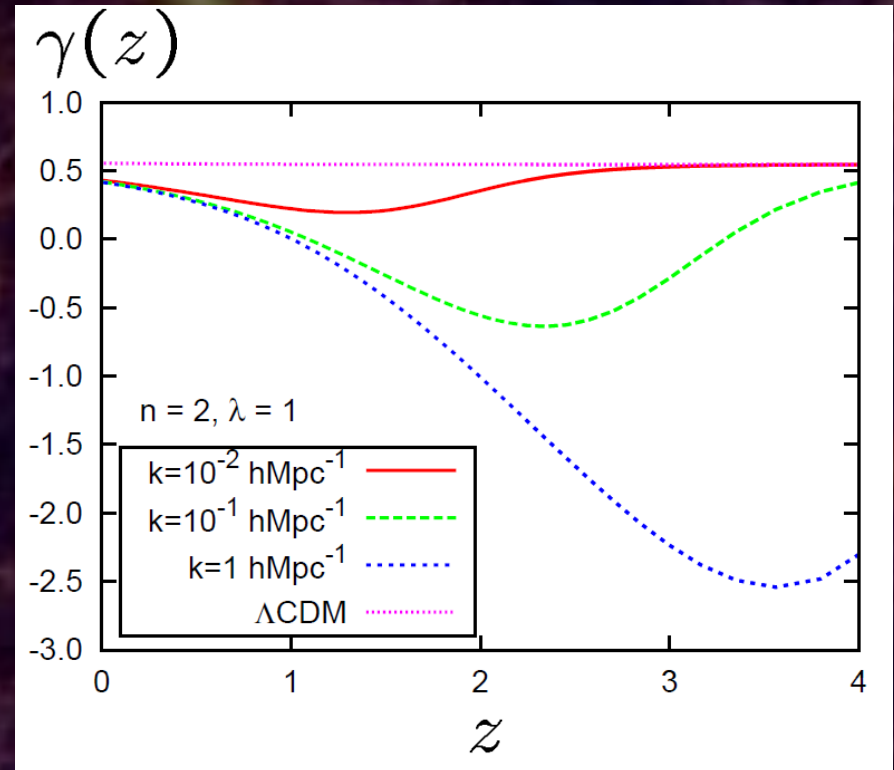
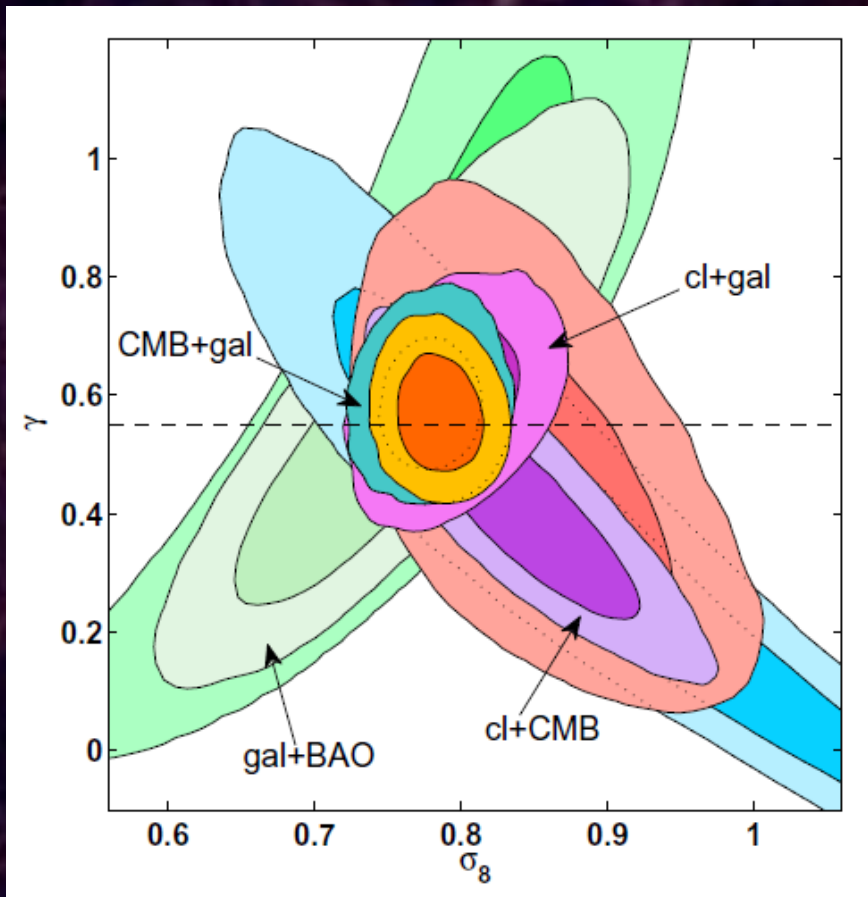
Komatsu et al.,  
 APJ Suppl. 192, 18 (2011)  
 [arXiv:1001.4538]



H.M., Starobinsky, Yokoyama  
 PTP 123 (2010) 887 [arXiv:1002.1141] 5

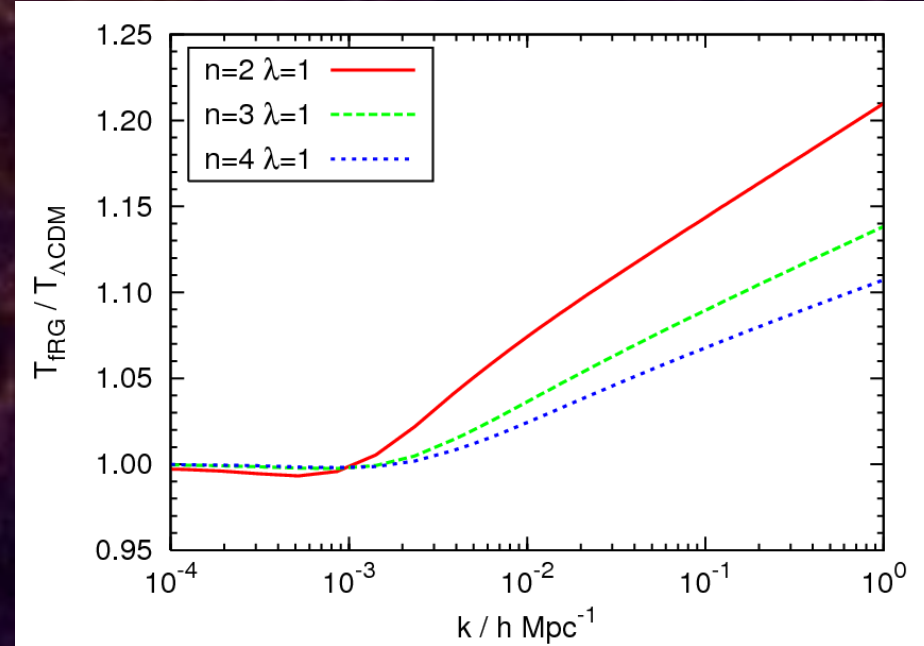
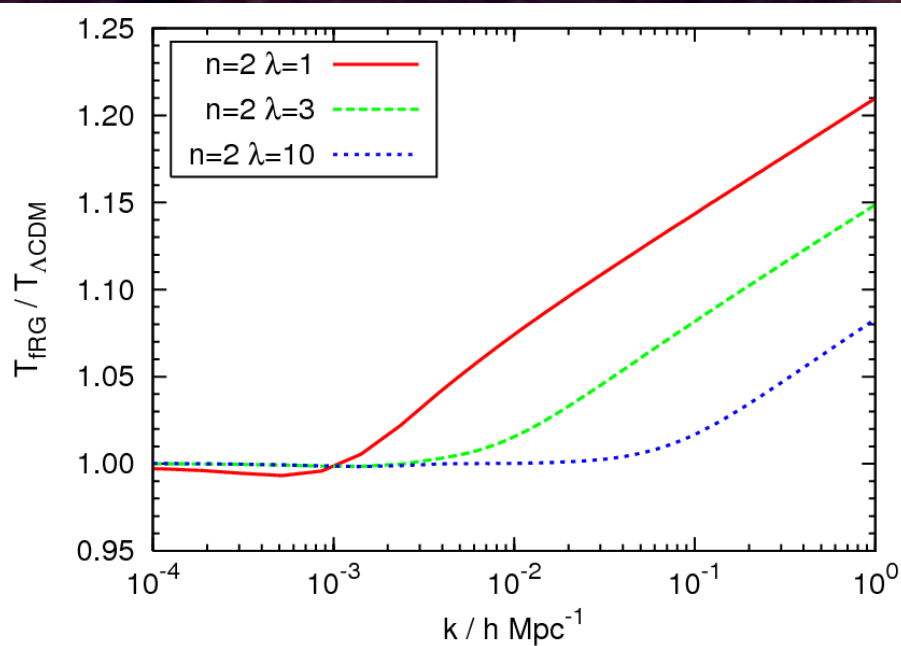
# Growth index $\gamma(z)$

$$\frac{d \log \delta}{d \log a} = \Omega_m(z) \gamma(z)$$



H.M., Starobinsky, Yokoyama  
PTP 123 (2010) 887 [arXiv:1002.1141]

# Additional transfer function in $f(R)$ gravity



$f(R)$  gravity enhances matter power spectrum.

↕ cancel

Massive neutrino suppresses matter power spectrum.

# Constraint on $N_{eff}$ from BBN

Abazajian et al [arXiv:1204.5379]

Model	Data	$N_{eff}$	Ref.
$\eta+N_{eff}$	$\eta_{CMB}+Y_p+D/H$	$3.8^{(+0.8)}_{(-0.7)}$	[331]
	$\eta_{CMB}+Y_p+D/H$	$< (4.05)$	[332]
	$Y_p+D/H$	$3.85 \pm 0.26$	[333]
		$3.82 \pm 0.35$	[333]
$\eta+N_{eff}, (\Delta N_{eff} \equiv N_{eff} - 3.046 \geq 0)$	$\eta_{CMB}+D/H$	$3.8 \pm 0.6$	[122]
	$\eta_{CMB}+Y_p$	$3.90^{+0.21}_{-0.58}$	[122]
	$Y_p+D/H$	$3.91^{+0.22}_{-0.55}$	[122]

[331] Izotov, Thuan, *Astrophys.J.* 710, L67 (2010) [arXiv:1001.4440]

[332] Mangano, Serpico, *Phys.Lett. B* 701, 296 (2011) [arXiv:1103.1261]

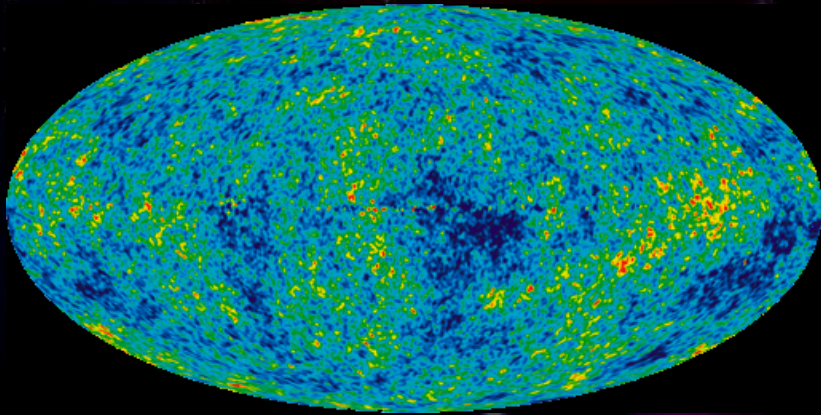
[333] Nollett, Holder [arXiv:1112.2683]

[122] Hamann et al, *JCAP* 1109, 034 (2011) [arXiv:1108.4136]



# Constraints on $N_{\text{eff}}$ and $\sum m_\nu$ in $\Lambda\text{CDM}$

CMB



Komatsu et al.,  
APJ Suppl. 192, 18 (2011)  
[arXiv:1001.4538]

+

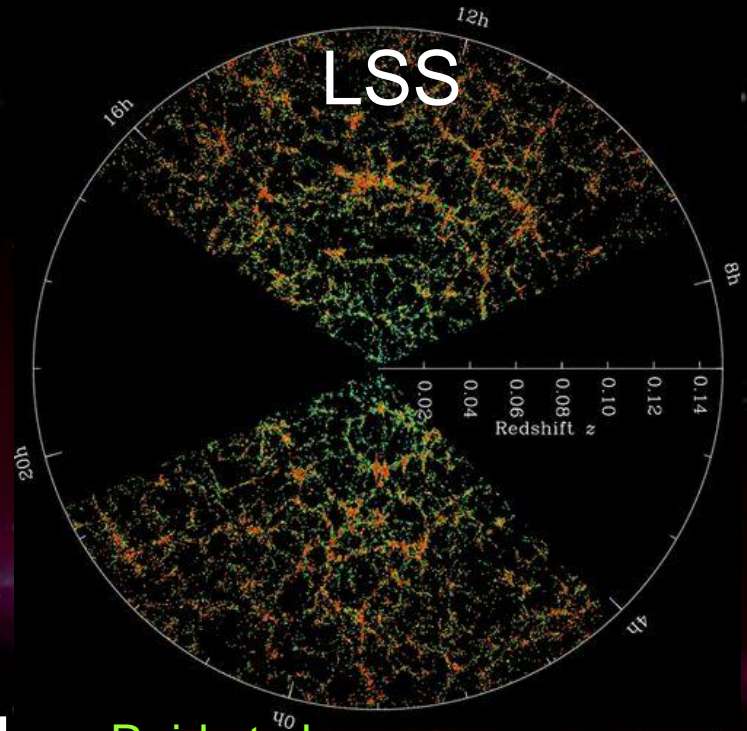
$\Lambda\text{CDM}$



$$\sum m_\nu < 0.44\text{eV} \quad (95\% \text{ CL})$$

$$N_{\text{eff}} = 4.34^{+0.86}_{-0.88} \quad (68\% \text{ CL})$$

LSS

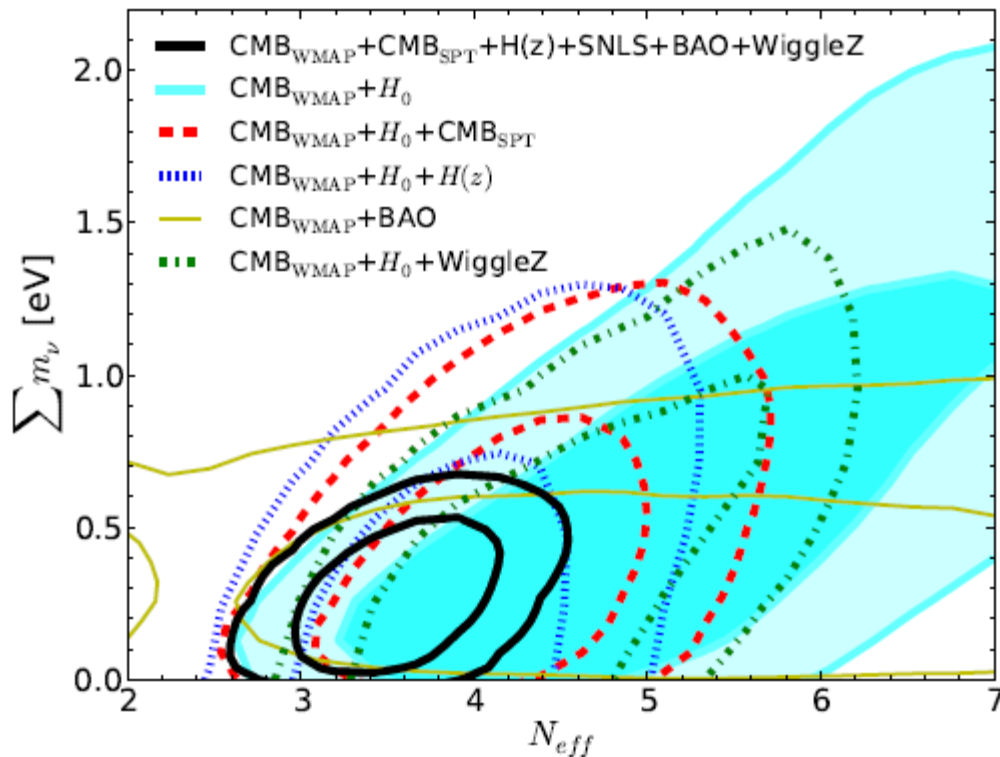


Reid et al,  
Mon.Not.Roy.Astron.Soc. 404  
(2010) 60 [arXiv:0907.1659]

# Constraints on $N_{\text{eff}}$ and $\sum m_\nu$ in $\Lambda$ CDM

## ABSTRACT

Recent indications from both particle physics and cosmology suggest the existence of more than three neutrino species. In cosmological analyses the effects of neutrino mass and number of species can in principle be disentangled for fixed cosmological parameters. However, since we do not have perfect measurements of the standard  $\Lambda$  Cold Dark Matter model parameters some correlation remains between the neutrino mass and number of species, and both parameters should be included in the analysis. Combining the newest observations of several cosmological probes (cosmic microwave background, large scale structure, expansion rate) we obtain  $N_{\text{eff}} = 3.58^{+0.15}_{-0.16}$  (68% CL)  $^{+0.55}_{-0.53}$  (95% CL) and  $\sum m_\nu < 0.60$  eV (95% CL), which are currently the strongest constraints on  $N_{\text{eff}}$  and  $\sum m_\nu$  from an analysis including both parameters. The preference for  $N_{\text{eff}} > 3$  is now at a  $2\sigma$  level.



Riemer-Sorensen et al  
[arXiv:1210.2131]

$\Lambda$ CDM cosmology



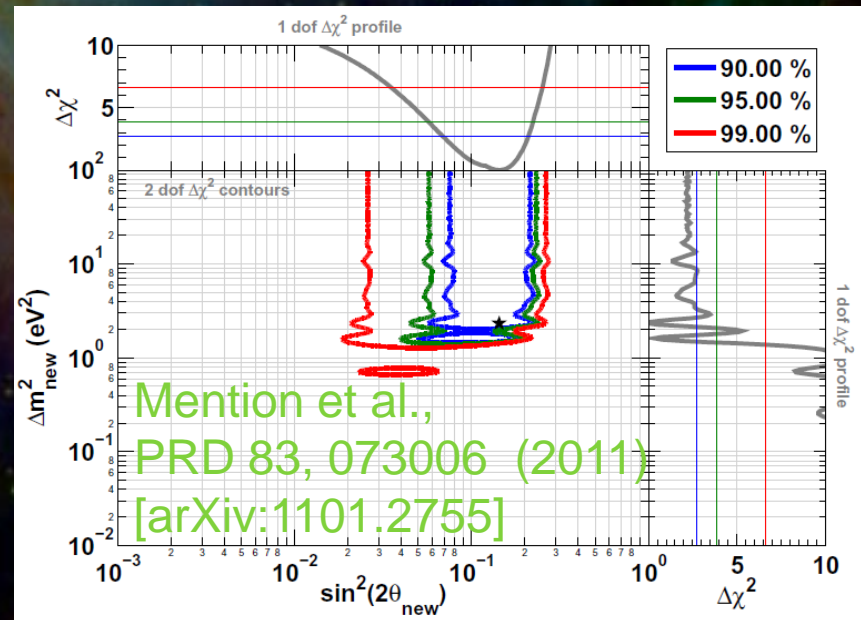
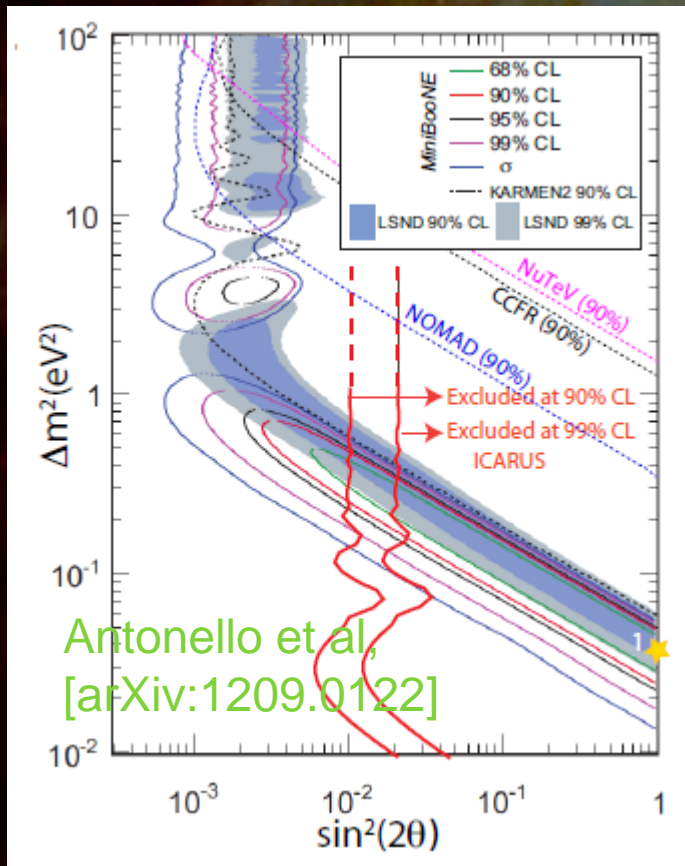
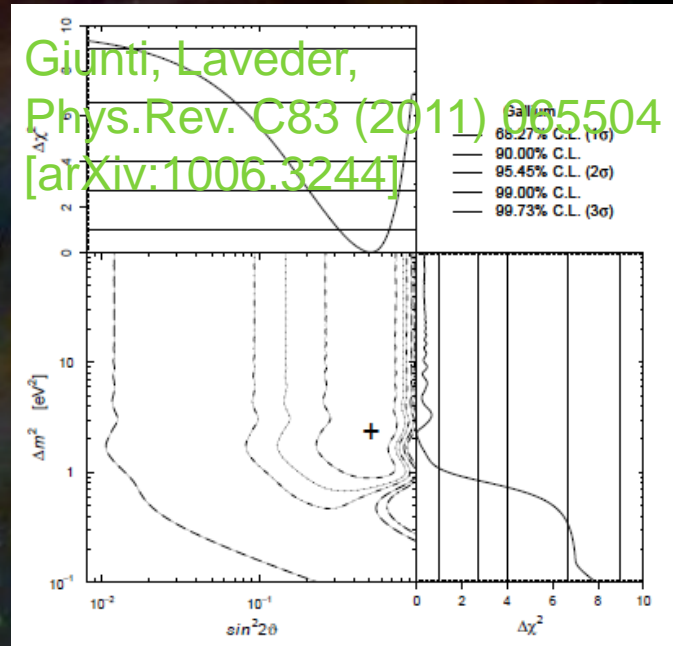
sub-eV

sterile neutrino

# Neutrino oscillation

Sterile neutrino mass  $\gtrsim 1$  eV

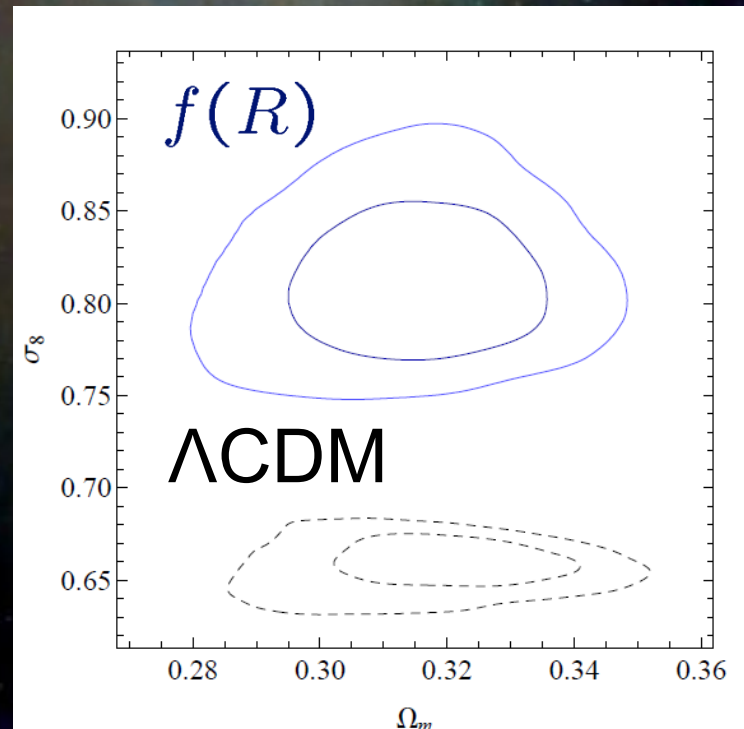
$\Leftrightarrow \Lambda$ CDM model



# MCMC analysis: $\Lambda$ CDM vs $f(R)$ gravity

H.M., Starobinsky and Yokoyama, arXiv:1203.6828

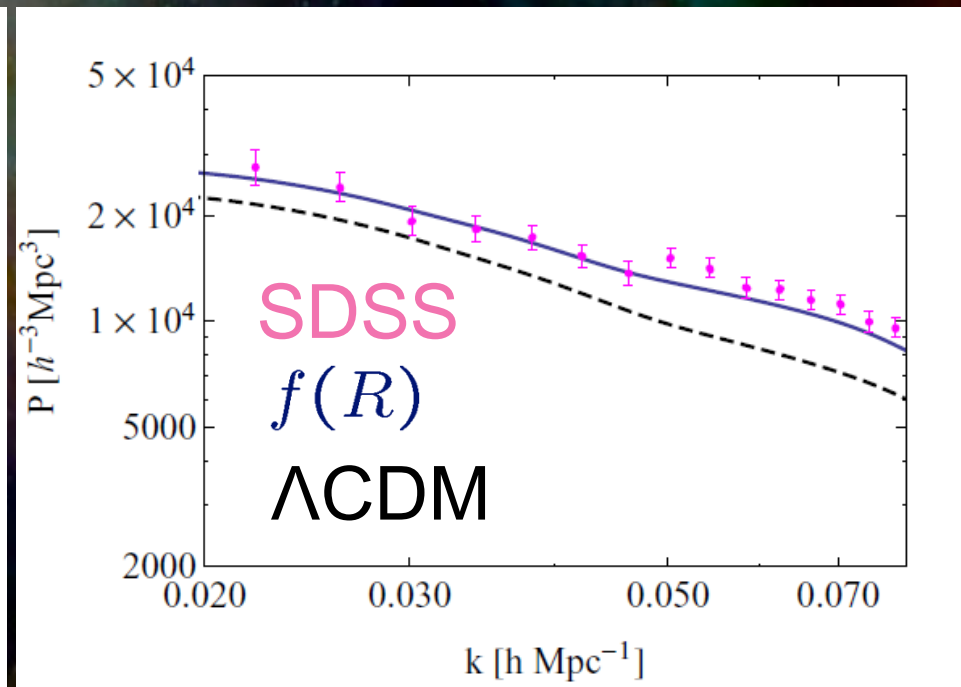
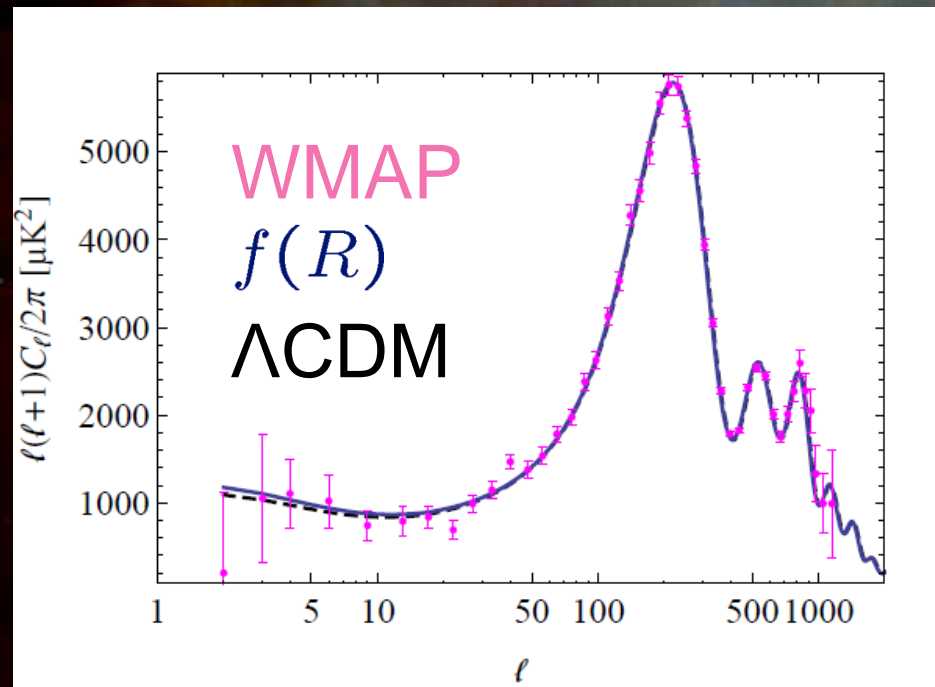
- 3 massless and 1 massive neutrino with mass = 1 eV
- WMAP7, SDSS DR 7 ( $0.02h\text{Mpc}^{-1} \leq k \leq 0.08h\text{Mpc}^{-1}$ )
- Better fit :  $\Delta\chi^2 = 10.7$  ( $\Delta\text{AIC} = 8.7$ )
- GR :  $\sigma_8 = 0.661_{-0.027}^{+0.023}$ ,  $f(R)$  :  $\sigma_8 = 0.815_{-0.066}^{+0.105}$



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# Summary

- Cosmology based on  $\Lambda$ CDM model  
Sterile neutrino mass  $< 1$  eV
- Neutrino oscillation experiments  
Sterile neutrino mass  $\gtrsim 1$  eV
- $f(R)$  gravity can resolve the tension.