

**ARE REDSHIFT-SPACE DISTORTIONS
ACTUALLY A PROBE OF
GROWTH OF STRUCTURE**

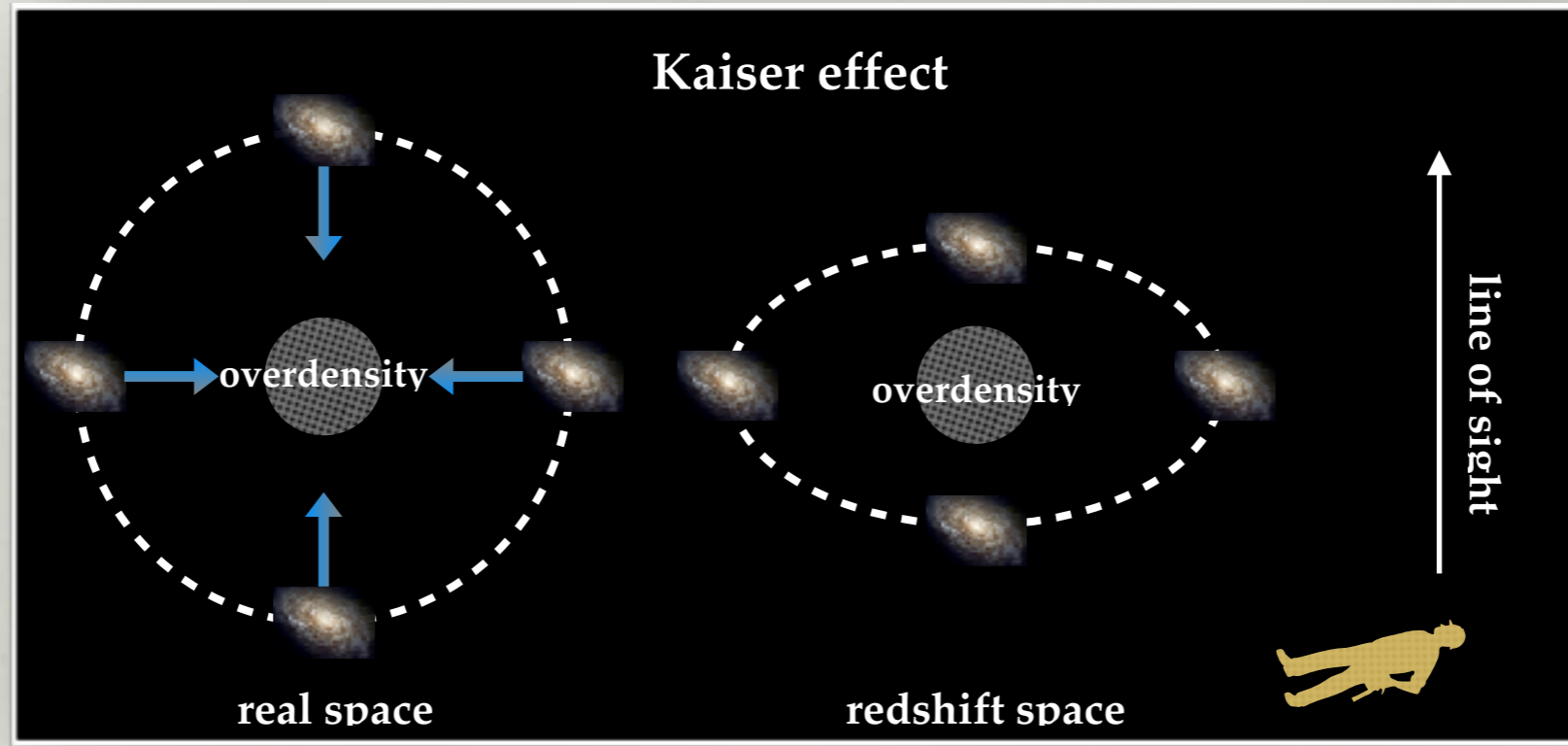
**RAMPEI KIMURA
TOKYO INSTITUTE OF TECHNOLOGY**

COSPA 2017

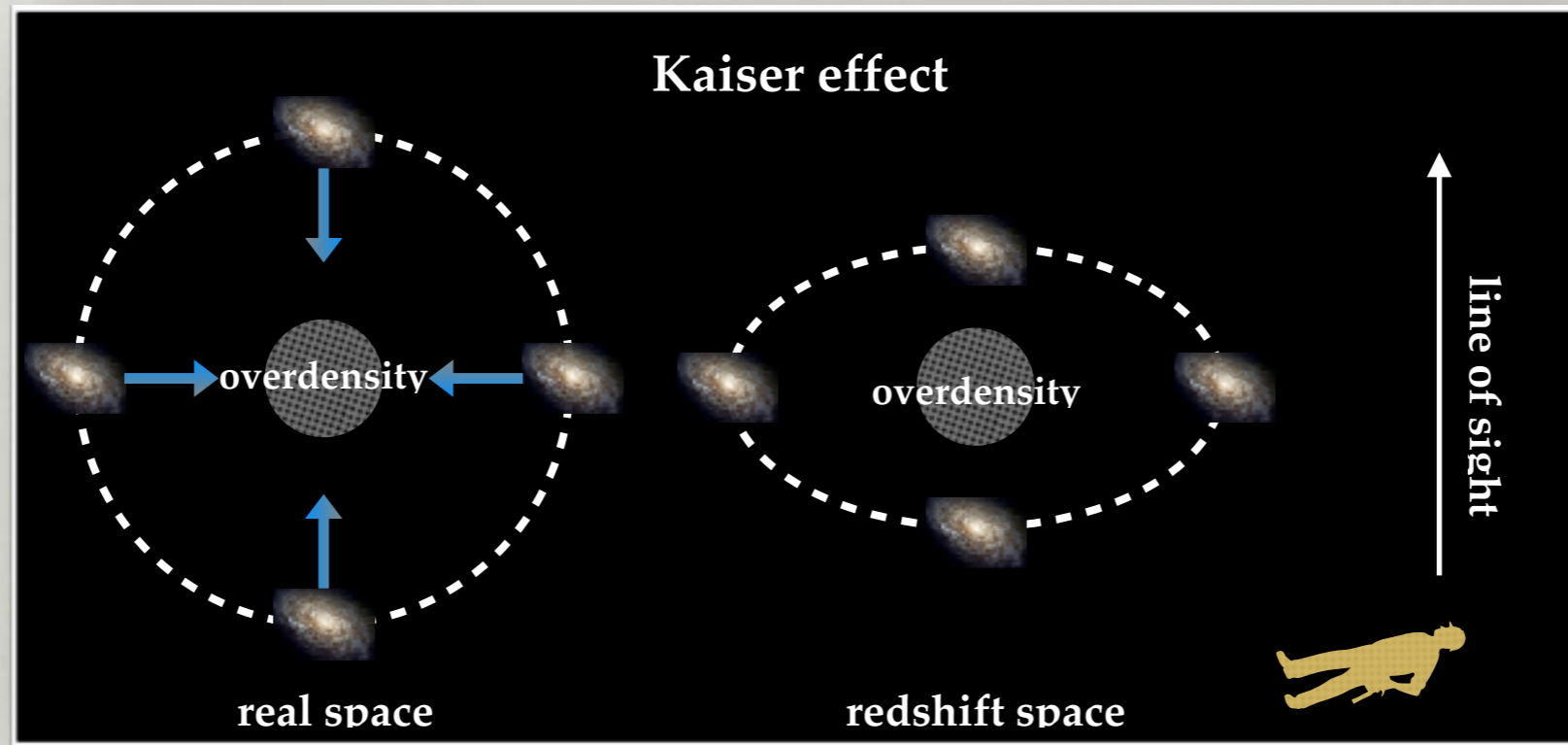
BASED ON ARXIV : 1709.09371

**COLLABORATORS : TERUAKI SUYAMA, MASAHIDE YAMAGUCHI,
DAISUKE YAMAUCHI, SHUICHIRO YOKOYAMA**

STANDARD COSMOLOGY I



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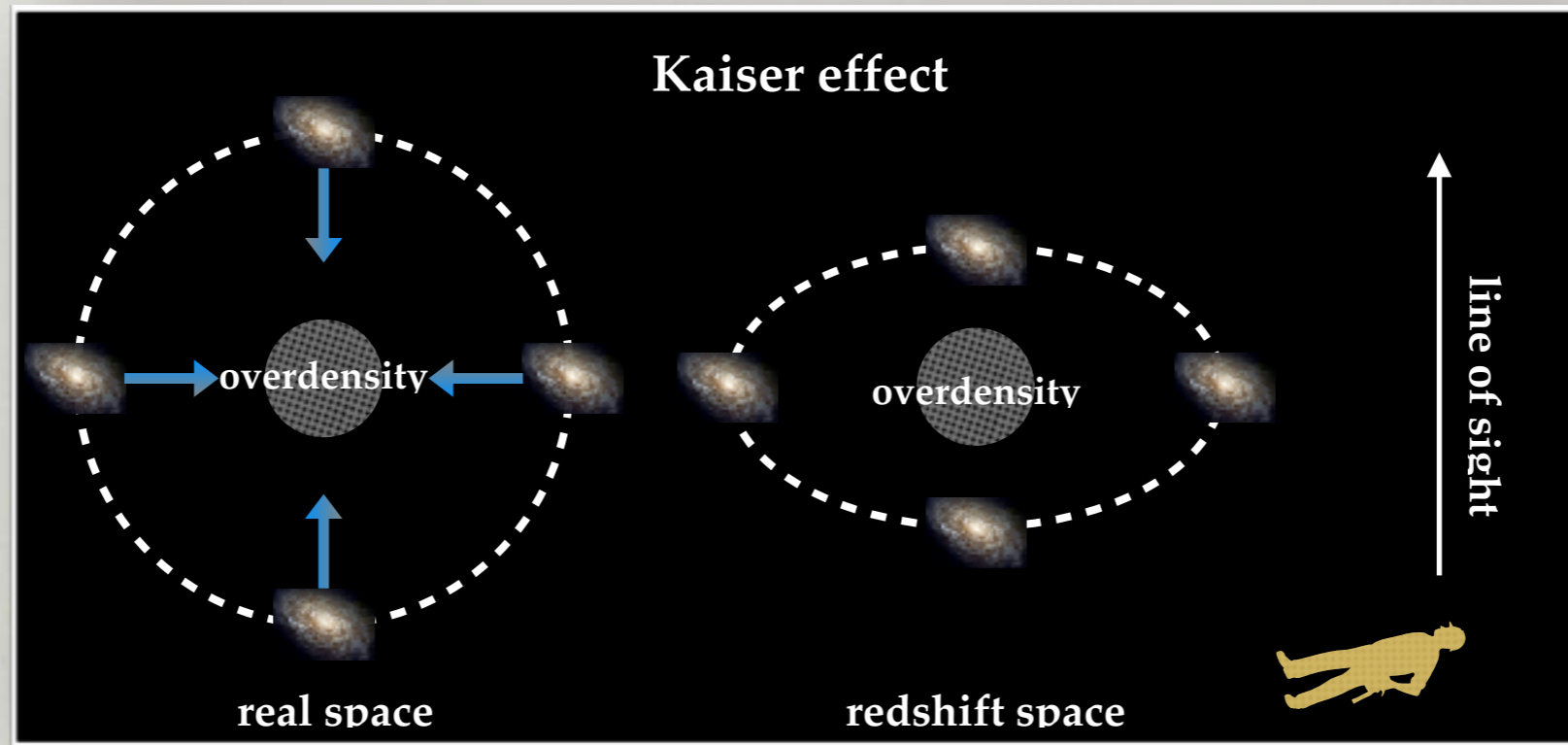


Mapping to redshift space

galaxy density contrast in redshift space \rightarrow $\delta_{g,s} = \delta_g - \frac{1}{aH} \nabla_z v_{g,z}$ \leftarrow line of sight component of galaxy peculiar velocity

galaxy density contrast in real space

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Galaxy vs. matter distribution

$$\delta_g = b_g \delta_m \quad (\text{linear bias})$$

$$v_g = v_m$$

STANDARD COSMOLOGY II

- Newtonian gauge $ds^2 = -[1 + 2\Phi(t, \mathbf{x})]dt^2 + a^2(t)[1 - 2\Psi(t, \mathbf{x})]d\mathbf{x}^2$
- Basic equations (sub-horizon approximation)

$$\frac{k^2}{a^2}\Psi = \frac{k^2}{a^2}\Phi = -4\pi G\rho_m\delta_m \quad (\text{Poisson equation})$$

$$\dot{\delta}_m + \frac{k^2}{a^2}v_m = 0 \quad \dot{v}_m - \Phi = 0 \quad (\text{continuity \& Euler equation})$$

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- Linear growth rate f_m $f_m(t) \equiv \frac{d \ln D_m}{d \ln a}$

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STANDARD COSMOLOGY III

Kaiser formula

$$P_{g,s}(\mathbf{k}; t) = b_g^2 (1 + \beta(t) \mu^2)^2 P_m(k; t)$$

the cosine of the angle between the line of sight & Fourier momentum

Power spectrum in redshift space

matter power spectrum

$$\beta \equiv \frac{f_m}{b_g}$$

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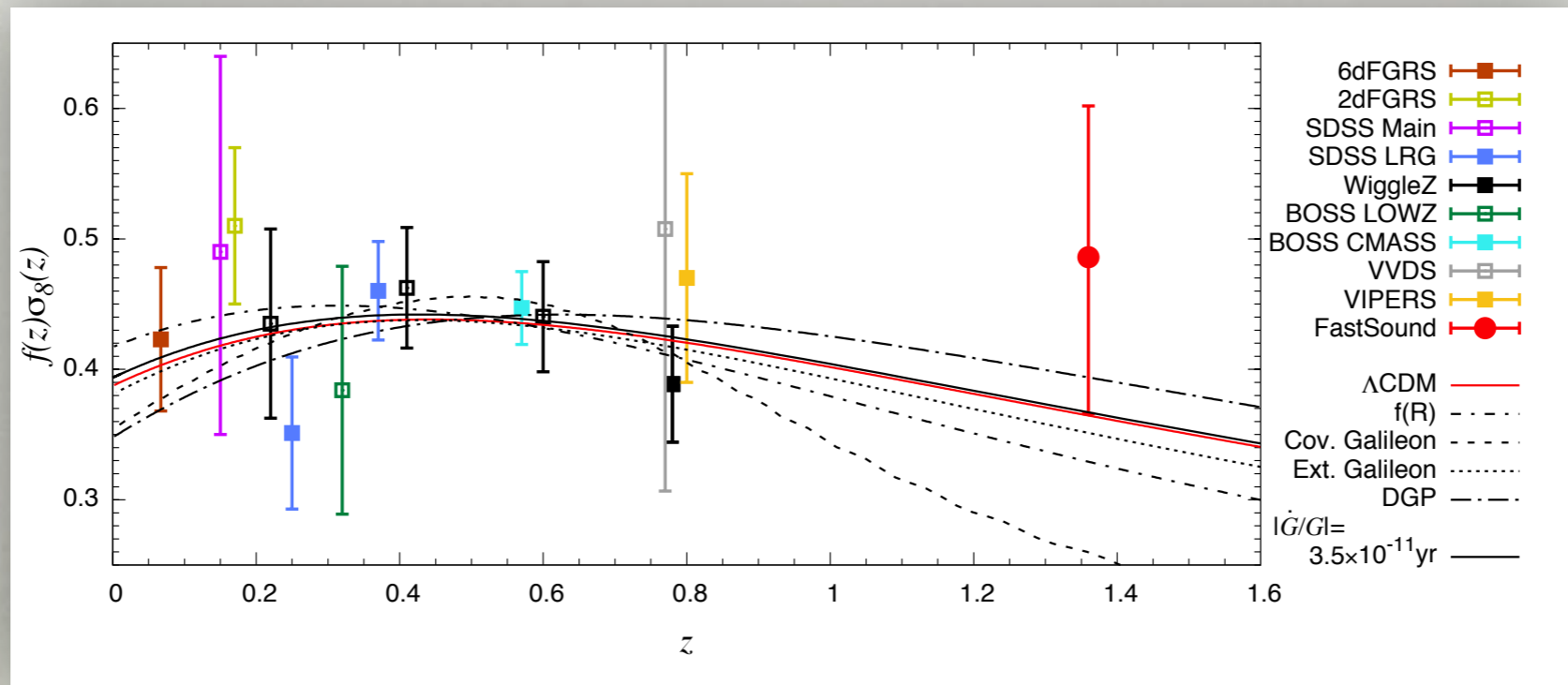
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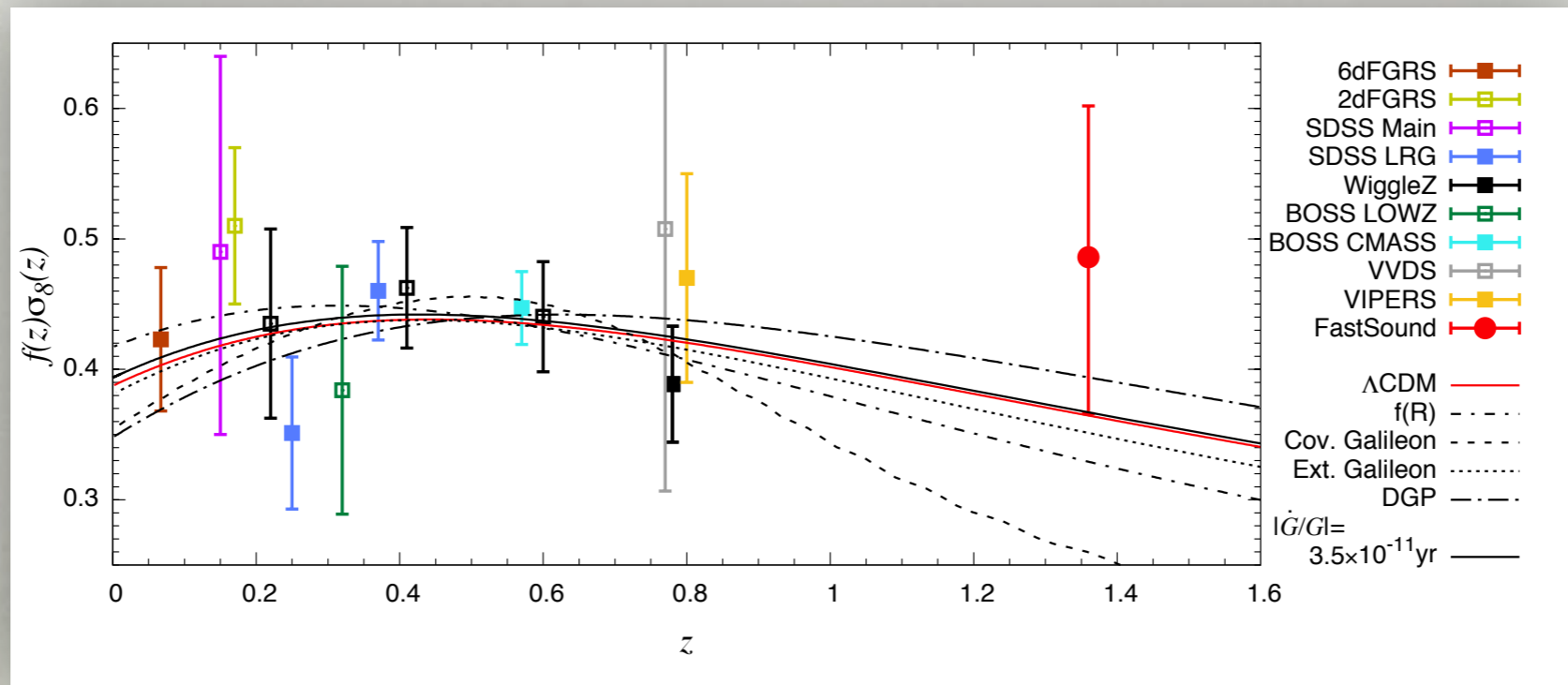
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Okumura et al. Publ. Astron. Soc. Japan (2015) 00(0), 1–23

Growth rate can directly measured by RSD

(bias can be fixed by cross-correlation of LSS & weak lensing)

NON-MINIMALLY COUPLED DM

- **GR + scalar field (Dark energy)** $S = \int d^4x \sqrt{-g} \left[\frac{M_{\text{Pl}}^2}{2} R[g] + \mathcal{L}_\phi[g, \phi] \right] + S_b + S_c$

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- Matter = (standard) baryon + **non-minimally coupled** cold dark matter

$$S_b = \int d^4x \sqrt{-g} \mathcal{L}_b[g_{\mu\nu}, \psi_b]$$

$$S_c = \int d^4x \sqrt{-\bar{g}} \mathcal{L}_c[\bar{g}_{\mu\nu}, \psi_c] \quad \bar{g}_{\mu\nu} = A(\phi, X)g_{\mu\nu} + B(\phi, X)\partial_\mu\phi\partial_\nu\phi$$

(conformal & disformal coupling)

Baryon : **sensitive** to solar-system experiments \rightarrow **minimal** coupling

CDM : **insensitive** to solar system experiments \rightarrow **non-minimal** coupling

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Energy transfer between dark energy and CDM

BASIC EQUATIONS

- Basic equations

EM tensor for the total matter

$$T_{\mu\nu}^{(m)} := T_{\mu\nu}^{(b)} + T_{\mu\nu}^{(c)}$$

$$G_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{1}{M_{\text{Pl}}^2} \left(T_{\mu\nu}^{(m)} + T_{\mu\nu}^{(\phi)} \right)$$

(Einstein equation)

$$\nabla^\mu T_{\mu\nu}^{(b)} = 0$$

(Conservation equation for baryon)

$$\nabla^\mu T_{\mu\nu}^{(c)} = -Q \partial_\nu \phi$$

(Conservation equation for DM & DE)

$$\square\phi - V_\phi = Q$$

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- Q roughly represents **the magnitude of the coupling between DM & DE**

$$Q \equiv -\frac{1}{\sqrt{-g}} \frac{\delta(\sqrt{-g} \mathcal{L}_c)}{\delta \phi} = \nabla_\mu W^\mu - Z$$

$$Z = \frac{1}{2A} \left[\left\{ A_\phi + \frac{A_X X (A_\phi - 2B_\phi X)}{A - A_X X + 2B_X X^2} \right\} T_{(c)} + \left\{ B_\phi + \frac{B_X X (A_\phi - 2B_\phi X)}{A - A_X X + 2B_X X^2} \right\} T_{(c)}^{\mu\nu} \partial_\mu \phi \partial_\nu \phi \right]$$

$$W^\mu = \frac{1}{2A} \left[2B T_{(c)}^{\mu\nu} \partial_\nu \phi - \frac{A - 2BX}{A - A_X X + 2B_X X^2} \times (A_X T_{(c)} + B_X T_{(c)}^{\alpha\beta} \partial_\alpha \phi \partial_\beta \phi) \partial^\mu \phi \right],$$

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$$\dot{\delta}_c + \frac{k^2}{a^2} v_c = R_0 \left(\dot{\delta}_c - \frac{Q_0}{\dot{\phi}} \delta_c \right)$$

v_c depends on time-derivative of density contrast and **density contrast**

$$\dot{v}_c - \Phi = \Gamma_1 v_c + \Gamma_2 \dot{\delta}_c + \Gamma_3 \delta_c$$

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- Evolution of density contrast of CDM

$$\ddot{\delta}_c + 2H_{\text{eff}} \dot{\delta}_c - 4\pi G_{\text{eff}} \rho_m \delta_m = 0$$

Growth rate also deviates from the standard cosmology

- Total matter = baryon + CDM ($T_{\mu\nu}^{(m)} := T_{\mu\nu}^{(b)} + T_{\mu\nu}^{(c)}$)

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$$v_m(t, \mathbf{k}) = -\frac{a^2 H}{k^2} f_m^{\text{eff}}(t) \delta_m(t, \mathbf{k})$$

$$f_m^{\text{eff}} = f_m + \Delta f_m$$

Actual linear growth rate

$$f_m(t) \equiv \frac{d \ln D_m}{d \ln a}$$

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- **Single-redshift RSD observations** can not determine the actual growth rate and DM-DE coupling
- **Multiple-redshift RSD observations** can separate the actual growth rate and DM-DE coupling

SUMMARY

Growth rate obtained from RSD

= actual growth rate + **DM-DE coupling effect**

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Growth rate obtained from RSD

= actual growth rate + **DM-DE coupling effect**

- DM-DE interaction **modifies continuity and Euler equations** in a cosmological setup.
- Even in DM-DE **direct coupling** (not through conformal or disformal metric) we reach the same conclusion
- **Multiple-redshift RSD measurements** provide us information of both **the actual growth rate** and **DM-DE coupling**