

Natural cliff inflation

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CosPA 2017

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12th December, 2017

Based on [JG](#) and C. S. Shin, arXiv:1711.08270 [hep-ph]

Outline

- 1 Introduction
- 2 Model
- 3 Prediction
- 4 Conclusions

1 Introduction

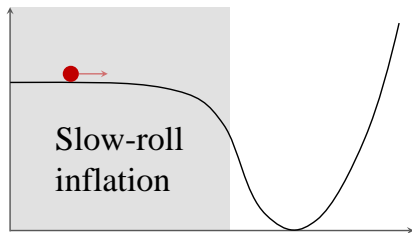
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Managing flat inflaton potential

Successful slow-roll inflation needs flat potential



$$\epsilon \equiv \frac{m_{\text{Pl}}^2}{2} \left(\frac{V'}{V} \right)^2 \ll 1$$

(potential is flat)

$$\eta \equiv m_{\text{Pl}}^2 \frac{V''}{V} \ll 1$$

(flatness lasts long enough)

Flatness is fragile under corrections, e.g. η problem (Copeland et al. 1994)

$$\Delta V \sim \frac{\phi^2}{\Lambda^2} V_0 \rightarrow \Delta \eta \sim \frac{m_{\text{Pl}}^2}{\Lambda^2} \gtrsim 1$$

Inflaton with symmetry

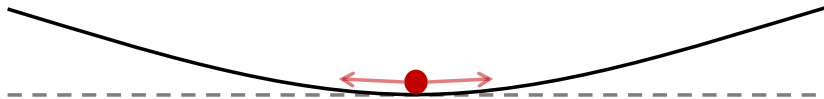
Inflaton protected by symmetry is good, e.g. shift symmetry



Shift symmetry $\phi \rightarrow \phi + c$

Inflaton with symmetry

Inflaton protected by symmetry is good, e.g. shift symmetry



Shift symmetry $\phi \rightarrow \phi + c$ is (softly) broken at a scale f so that

$$V(\phi) = \Lambda^4 \left[1 + \cos\left(\frac{\phi}{f}\right) \right]$$

“Natural inflation” (Freese, Frieman & Olinto 1990; Adams et al. 1993)

But CMB observations prefer $f \sim 5m_{\text{pl}}$, so EFT is doubtful

How to realize natural inflation

We can realize natural inflation by either

- ① obtaining (effective) super-Planckian f
 - Extranatural inflation (Arkani-Hamed, Cheng, Creminelli & Randall 2003)
 - Aligned axion (Kim, Nilles & Peloso 2005)
 - N-flaton (Dimopoulos, Kachru, McGreevy & Wacker 2008)
- ② finding working models with sub-Planckian f
 - ✓ We present an explicit model that allows $f \ll m_{\text{Pl}}$

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5D angular field with a zero mode

A 5D angular field $\theta(x, y)$ with shift symmetry ($\theta \rightarrow \theta + c$)

$$S[\theta] = \int d^5x f_5^3 \left[-\frac{1}{2} (\partial_M \theta)^2 \right]$$

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$$S[\theta] = \int d^5x f_5^3 \left[-\frac{1}{2} (\partial_M \theta)^2 - V_{\text{bulk}}(\theta) \right]$$

- 1 $V_{\text{bulk}}(\theta)$: Bulk potential with a mass parameter m
 - Shift symmetry is (softly) broken
 - No massless mode

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$$S[\theta] = \int d^5x f_5^3 \left[-\frac{1}{2} (\partial_M \theta)^2 - V_{\text{bulk}}(\theta) - V_{\text{boundary}}(\theta) \right]$$

- ① $V_{\text{bulk}}(\theta)$: Bulk potential with a mass parameter m
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- ② $V_{\text{boundary}}(\theta)$: Potential localized at boundaries
 - With S_1/Z_2 , $y_b = 0$ and $y_b = \pi R$
 - Massless mode with a non-trivial profile along y

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Consider e.g. the following potential (Choi, Im & Shin 2017):

$$V_{\text{bulk}} + V_{\text{boundary}} = -\frac{1}{4} m^2 \cos(2\theta) + \frac{1}{4} m^2 - 2m \cos\theta \left[\delta(y) - \delta(y - \pi R) \right]$$

Profile of zero mode in 5D

- Massless mode can be found from 5D action

$$S[\theta] = \int d^5x \frac{-f_5^3}{2} \left[(\partial_\mu \theta)^2 + (\partial_y \theta + m \sin \theta)^2 \right]$$

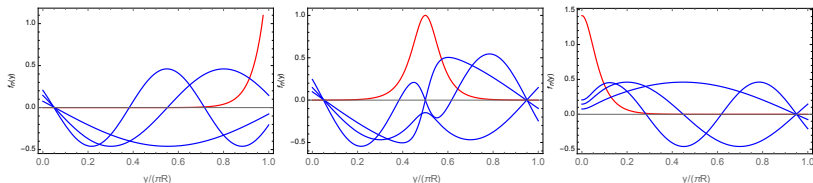
- Mode expansion: $\theta(x, y) = \langle \theta \rangle + \sum_{n=0} f_n(y) \phi_n(x)$ with

$$\langle \theta \rangle = 2 \tan^{-1} \left[e^{-my} \langle u(\phi) \rangle \right] \equiv 2 \tan^{-1} \left[e^{-m(y-y_0)} \right]$$

Zero mode is localized according to $\langle \phi \rangle$

- Higher order profiles could be found iteratively

$$f_0(y) \sim \text{sech}[m(y - y_0)], \text{ and so on}$$



Zero mode as a 4D massless field

From the zero mode action (suppressing 4D integral notation)

$$S = \int_0^{\pi R} dy \frac{-f_5^3}{2} (\partial_\mu \theta)^2 = -\frac{1}{2} (\partial_\mu \phi)^2$$

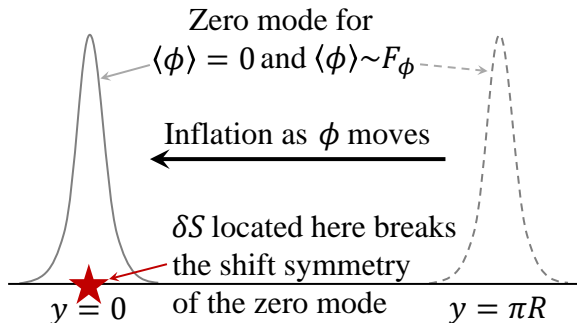
Zero mode θ_0 is explicitly

$$\theta_0(x, y) = 2 \tan^{-1} \left[i e^{-my} \operatorname{sn} \left(\frac{\phi(x)}{2if} \middle| e^{-2m\pi R} \right) \right] \quad \text{with} \quad f \equiv \sqrt{\frac{f_5^3}{2m} (1 - e^{-2m\pi R})}$$

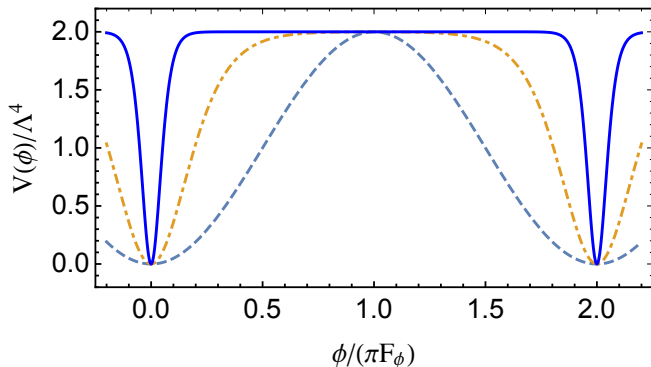
Generation of the potential

Introducing a small perturbation ($\Lambda^4 \ll 2f_5^3 m$) at $y_b = 0$

$$\delta S[\theta] = \int \delta(y) \Lambda^4 [1 - \cos \theta(x, y)] \quad \rightarrow \quad V(\phi) = -\Lambda^4 \frac{\text{sn}^2\left(\frac{\phi}{2if} \middle| e^{-2m\pi R}\right)}{1 - \text{sn}^2\left(\frac{\phi}{2if} \middle| e^{-2m\pi R}\right)}$$



Shape of the potential



- Half period $\pi F_\phi = 2fK(1 - e^{-2m\pi R})$
- Shape is exponentially sensitive to mR

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Full analytic results

Given the potential for a canonical field we can find

$$A_{\mathcal{R}} = \frac{1}{6\pi^2} \frac{\Lambda^4}{m_{\text{Pl}}^4} \frac{f^2}{m_{\text{Pl}}^2} \frac{\text{sn}^4(1 - \text{sn}^2)}{\text{cn}^2 \text{dn}^2} \approx 2.21 \times 10^{-9}$$

$$n_{\mathcal{R}} = 1 + \frac{m_{\text{Pl}}^2}{f^2} \frac{(1 - \text{sn}^2)(\text{cn}^2 + \text{dn}^2 + \text{cn}^2 \text{dn}^2) - \text{cn}^2 \text{dn}^2}{\text{sn}^2(1 - \text{sn}^2)^2} \approx 0.96$$

$$r = \frac{m_{\text{Pl}}^2}{f^2} \frac{-8\text{cn}^2 \text{dn}^2}{\text{sn}^2(1 - \text{sn}^2)^2} \lesssim 0.07$$

But not very illuminating...

Simplified potential

For $mR = \mathcal{O}(10)$ the potential is approximately

$$V(\phi) \approx \Lambda^4 \tanh^2\left(\frac{\phi}{2f}\right)$$

$$\text{for } |\phi| < \pi F_\phi \approx 2m\pi Rf \approx \sqrt{2m\pi R} \left(\frac{f_5}{M_5}\right)^{3/2} m_{\text{Pl}}$$

Half period may well be sub-Planckian for $f_5 \ll M_5$

Inflationary predictions

- Number of e -folds

$$N = \frac{1}{m_{\text{Pl}}} \int_{\phi_e}^{\phi_i} \frac{d\phi}{\sqrt{2\epsilon}} \approx \left(\frac{f}{2m_{\text{Pl}}} \right)^2 e^{\phi_i/f}$$

- Spectral index

$$n_{\mathcal{R}} - 1 = 1 - \frac{4[1 + \cosh(\phi_i/f)] \text{csch}^2(\phi_i/f)}{(f/m_{\text{Pl}})^2} \approx 1 - \frac{2}{N}$$

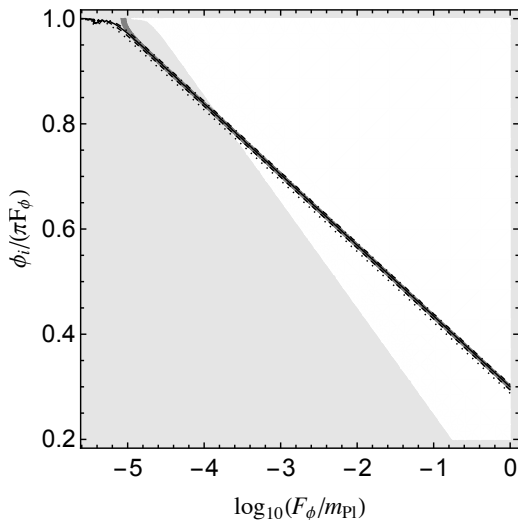
The same as many favoured models

- Tensor-to-scalar ratio

$$r = \frac{32 \text{csch}^2(\phi_i/f)}{(f/m_{\text{Pl}})^2} \approx \frac{8}{N^2} \left(\frac{f}{m_{\text{Pl}}} \right)^2$$

Compared to R^2 model, further suppressed by $(f/m_{\text{Pl}})^2$

Parameter space

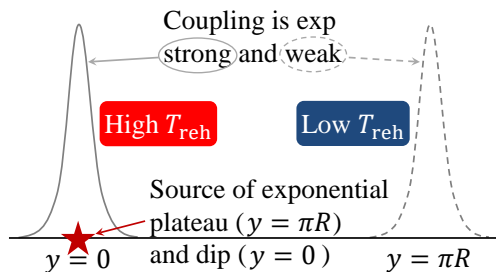


Sub-Planckian field range can do the job

Reheating after inflation

Anomalous coupling gives interaction bet inflaton and gauge fields

$$\int d^5x \delta(\text{SM location}) c_\gamma \theta(x, y) F_{\mu\nu}(x) \tilde{F}^{\mu\nu}(x) \rightarrow \delta\mathcal{L} \sim \frac{c_\gamma}{f} \delta\phi F\tilde{F}$$



For fiducial values $F_\phi \sim 10^{-3} m_{\text{pl}}$ and $mR = 5$, if SM lives at...

- $y = 0$: $T_{\text{reh}} = \sqrt{\Gamma_\phi m_{\text{pl}}} \sim 10^{13}$ GeV
- $y = \pi R$: suppressed by $e^{-m\pi R} \sim 10^{-7}$ and $T_{\text{reh}} \sim 10^6$ GeV

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Conclusions

- Realizing natural inflation concerns the value of f
- Setup
 - Zero mode of 5D angular field
 - Exponentially flat hilltop and cliff-like minimum
- Inflation
 - Simple analytic results for reasonable parameters
 - Sub-Planckian field excursion