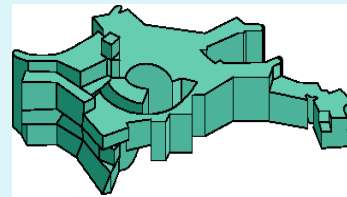


Recent Progress in Type Ia Supernova Modeling and its Implication for Cosmology

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Physics and Cosmology
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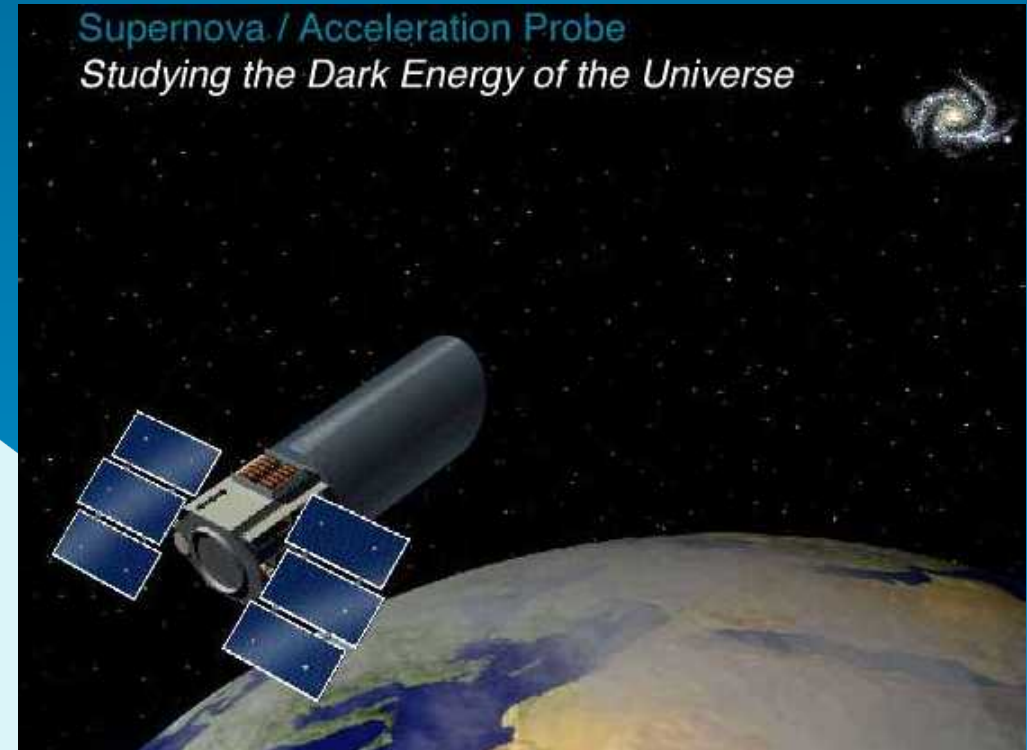
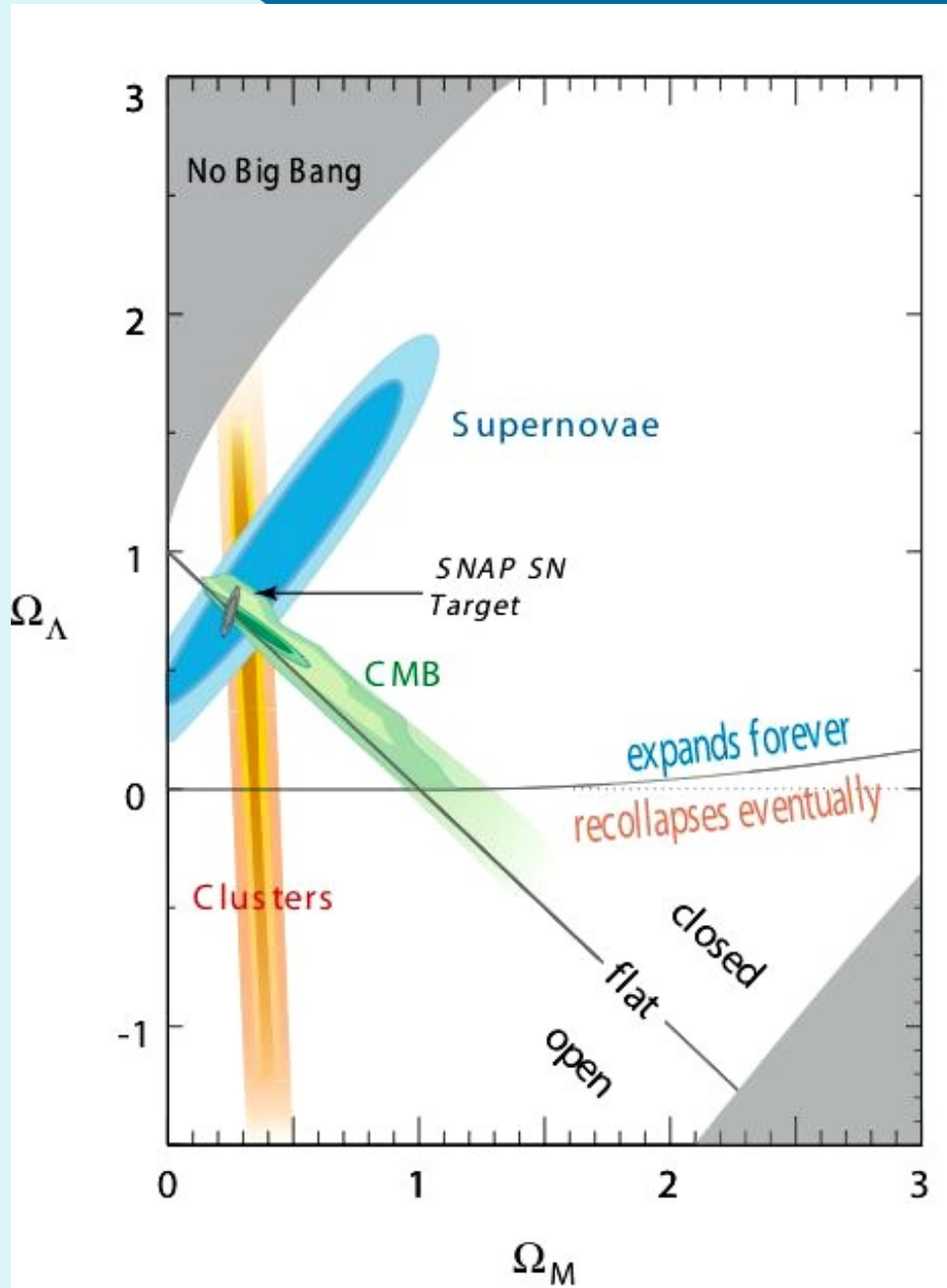
Stan Woosley (UC Santa Cruz),

.....



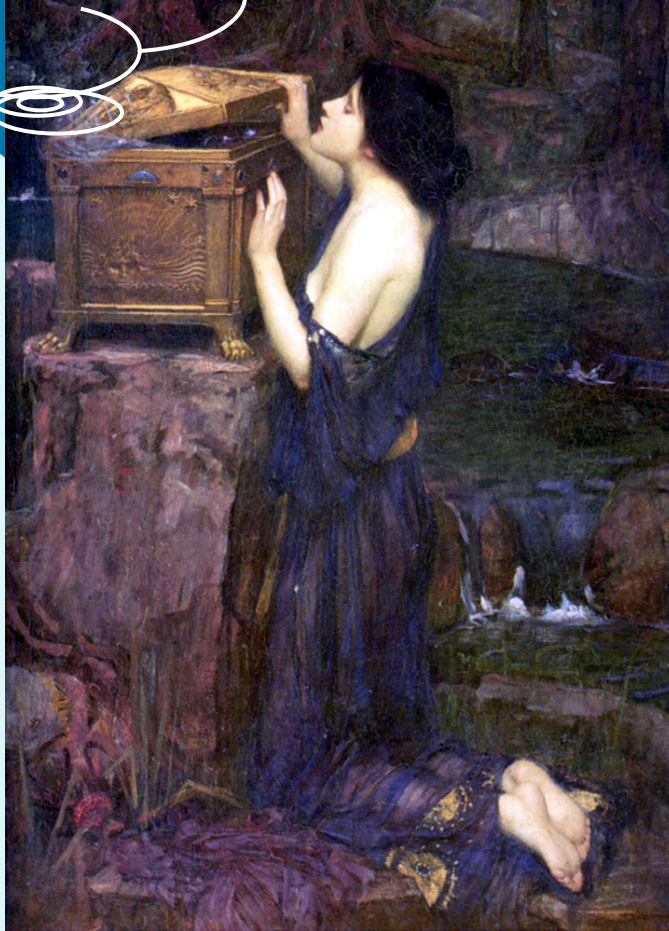
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The promise of supernova cosmology:



But ...

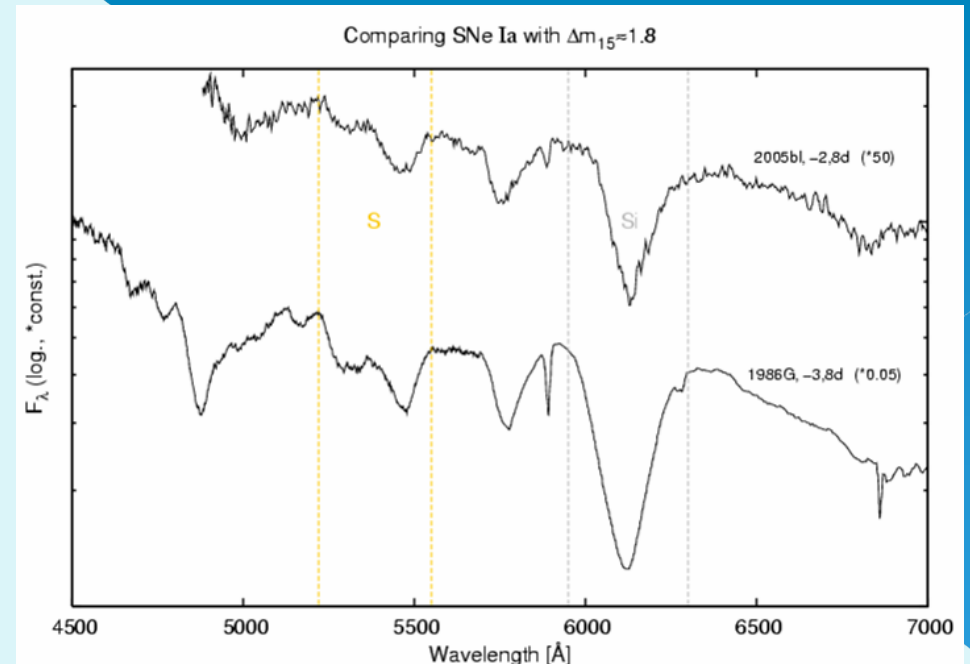
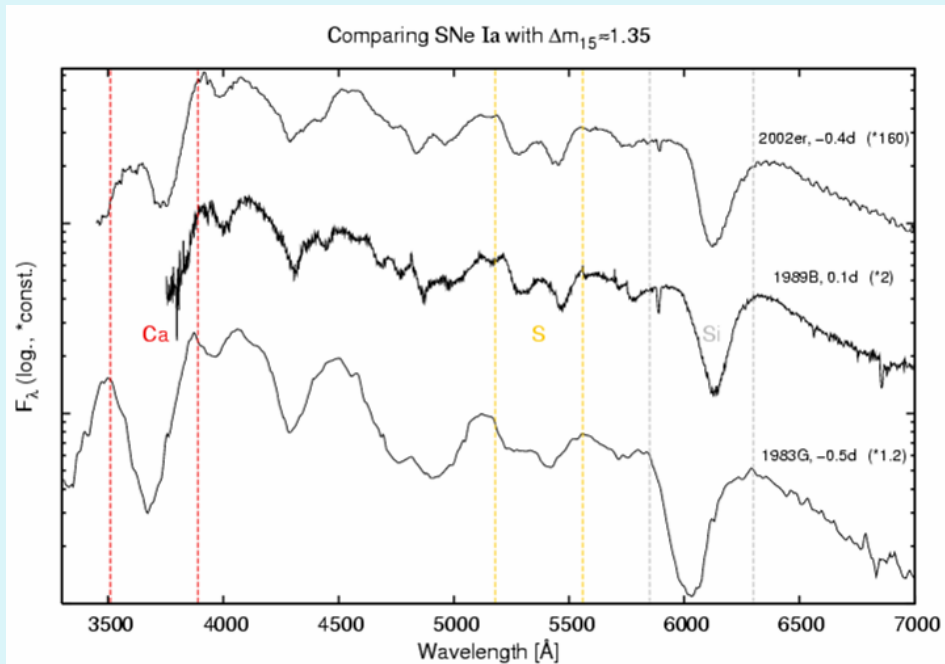
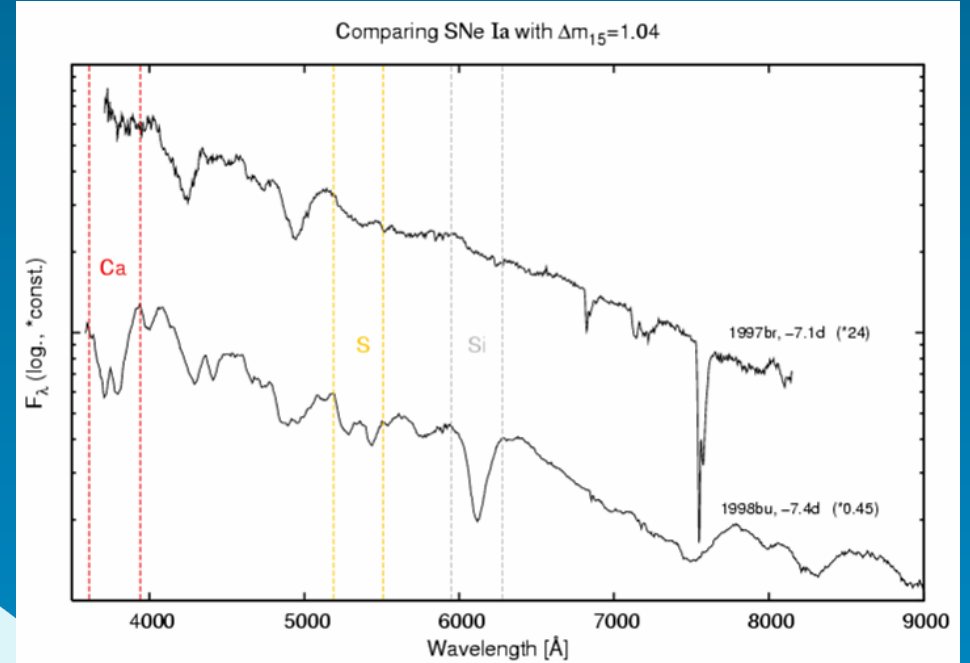
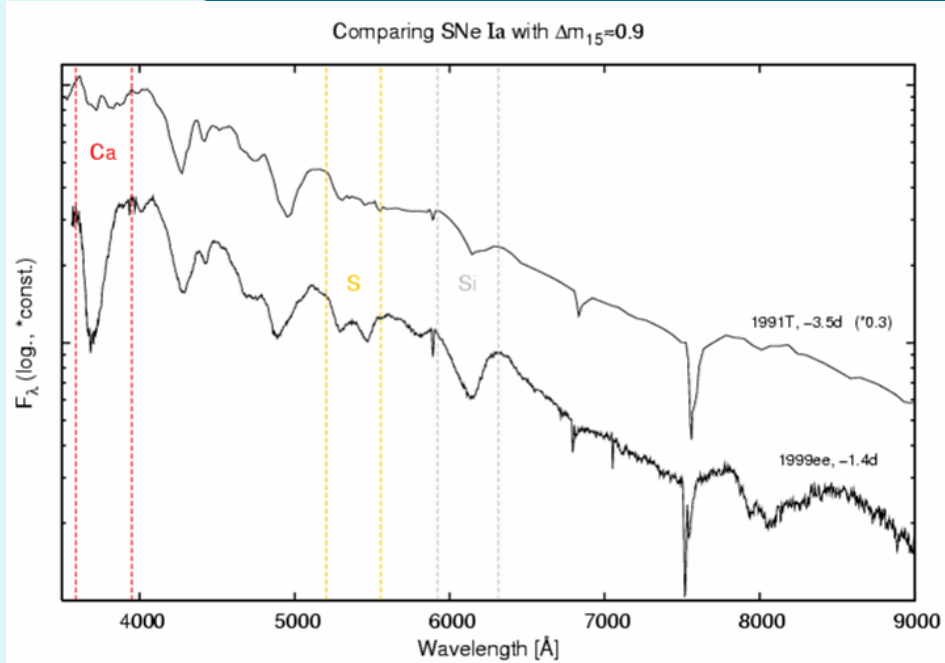
Systematics!



Is Hope left in Pandora's box ?

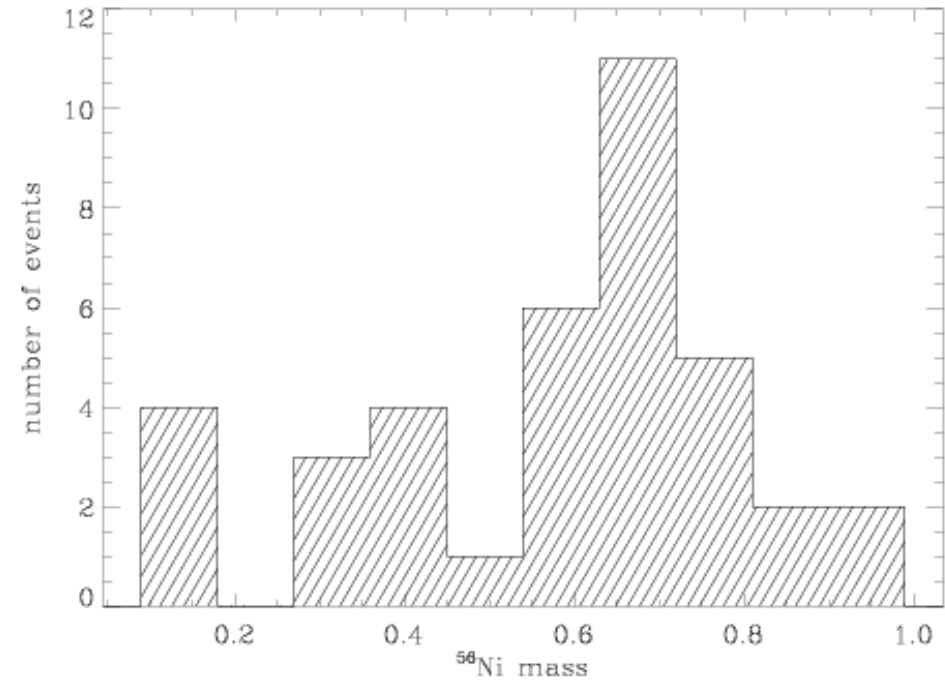
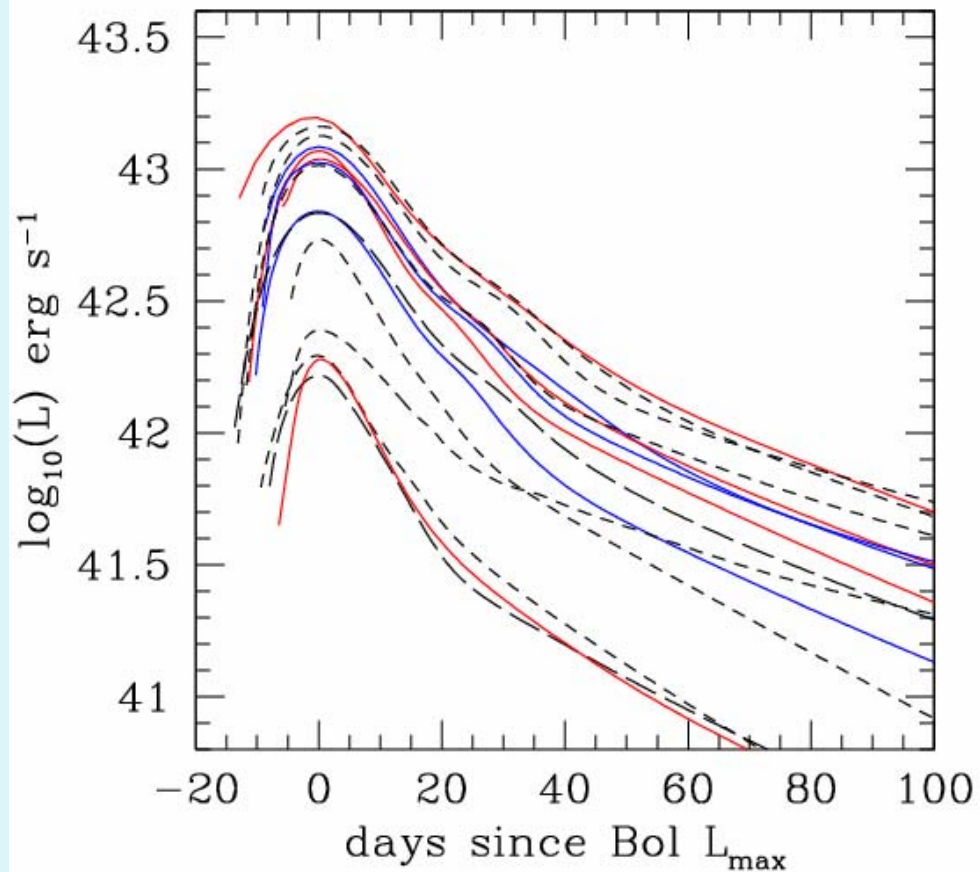
How “different” are SNe Ia?

Example: Early time spectra (court. Stephan Hachinger)



Example: Bolometric LCs and Ni-masses

(mostly RTN/ESC data)



(Court. M. Stritzinger;
also: Stritzinger et al. 2006)

Is evolution a problem?

Or extinction?

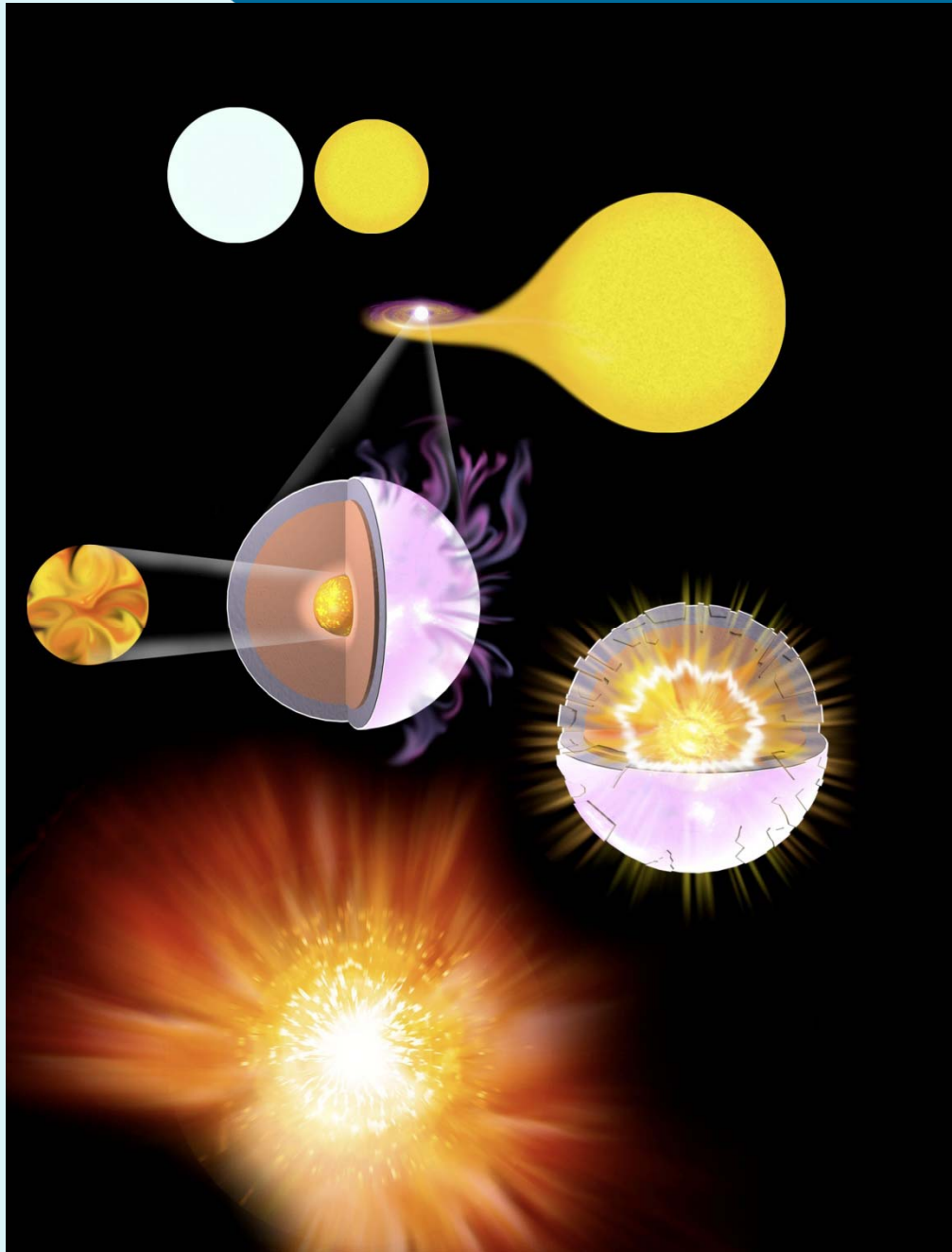
Or ?

Ask theory also!

The “standard” model of type Ia supernovae



The “standard” model of type Ia supernovae

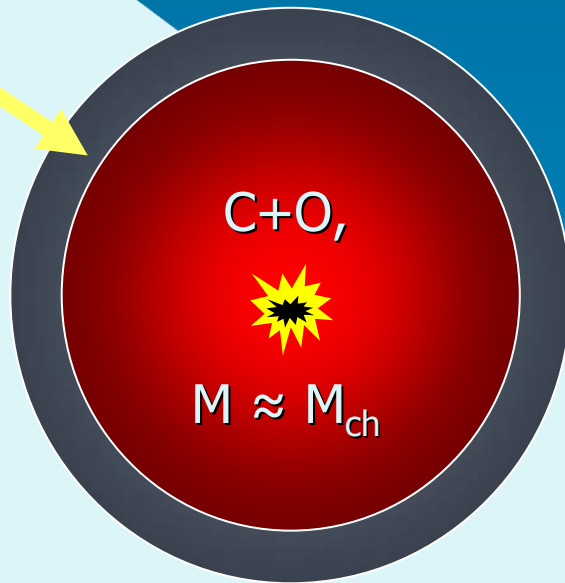


- White dwarf in a binary system
- Growing to M_{Chan} by mass transfer
- Disrupted by a thermonuclear explosion

Here, I will mainly discuss deflagration models!

How does the model work?

He (+H)
from binary
companion



Density $\sim 10^9 - 10^{10}$ g/cm

Temperature: a few 10^9 K

Radii: a few 1000 km

Explosion energy:

*Fusion C+C, C+O,
O+O \rightarrow "Fe"*

Laminar burning
velocity:

$U_L \sim 100$ km/s $\ll U_S$

Too little is burned!

The physics of turbulent combustion

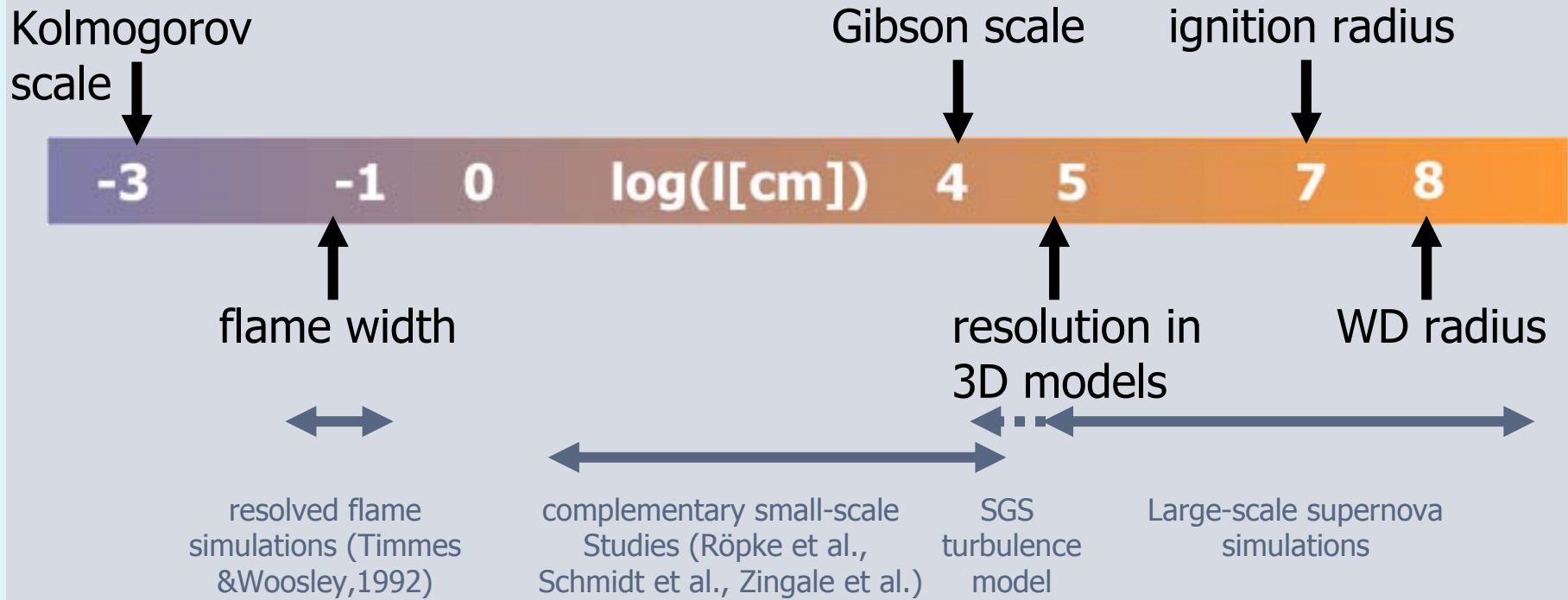
- Everyday experience:
Turbulence increases the burning velocity.
- In a star:
Reynoldsnumber $\sim 10^{14}$!
- In the limit of strong turbulence: $U_B \sim V_T$!
- Physics of thermonuclear burning is very similar to premixed chemical flames.



Relevant length scales in simulations of SN Ia explosions

(Gibson scale $s_l = v'$: below turbulence does not affect flame propagation)

beginning of the explosion: burning in ~~distributed~~ **distributed regime**

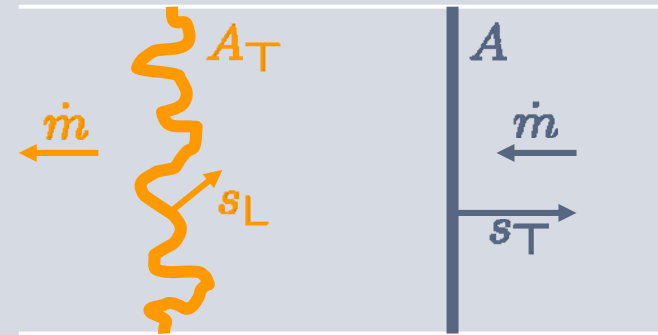


The basic principles of modeling turbulent combustion:

- **During most parts of the SN Ia explosion:** turbulence does not penetrate internal flame structure; **flamelet regime** of turbulent combustion



Burning in the flamelet regime:



$$s_T \propto v'$$

(Damköhler 1940)

In very late stages: turbulence may affect burning microphysics → onset of **distributed burning regime**

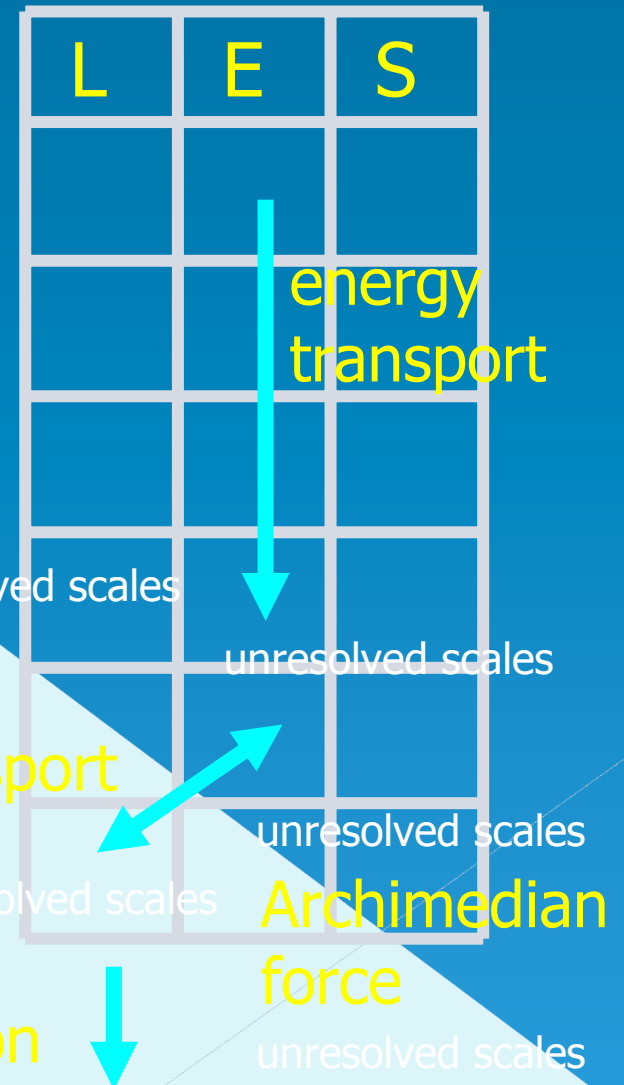
Numerical implementation (I)

- Large Eddy Simulation (LES) approach
- Subgrid-scale turbulence model (Niemeyer & WH, 1995; Schmidt et al., 2005, 2006)

RESOLVED SCA

Balance equation for turbulent kinetic energy on unresolved scales

→ **determines turbulent velocity fluctuations v' (and s_T)**



turbulent transport

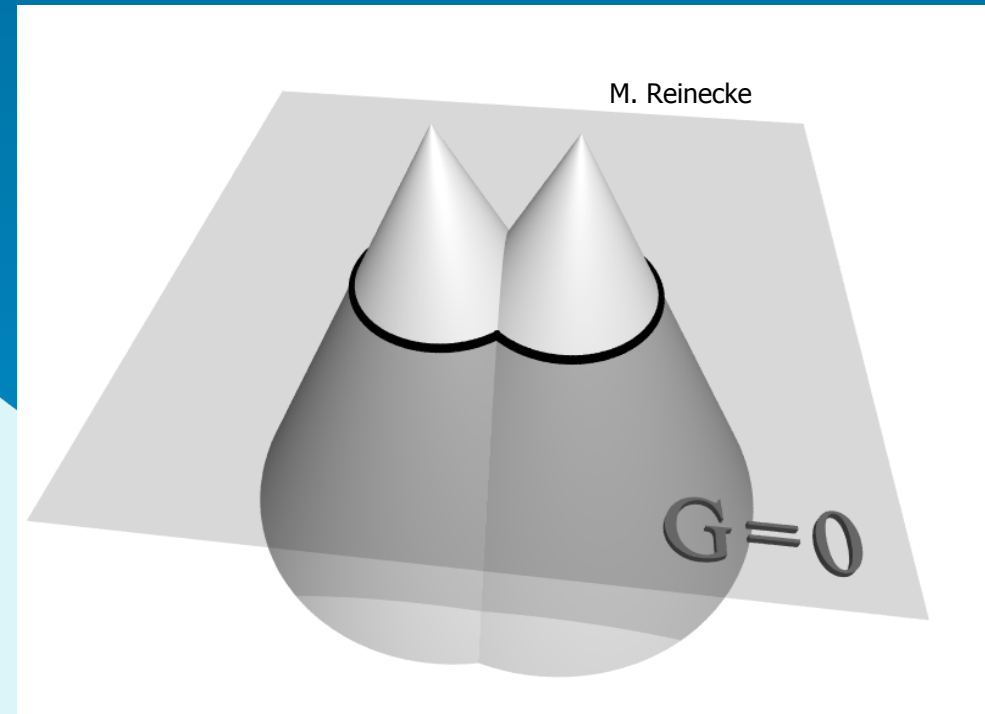
Numerical implementation (II)

- **seen from scales of WD:** flame is a discontinuity between fuel and ash; flame propagation via Level Set Method: associate flame front with

$$\Gamma = \{\vec{r} \mid G(\vec{r}, t) = 0\}$$

- **distance function G,** $G < 0$ in fuel, $G > 0$ in ashes, **equation of motion:**

$$\frac{\partial G}{\partial t} = (\mathbf{v}_u \mathbf{n} + s_T) |\nabla G|$$



- **simplified description of burning:** everything behind $G=0$ isosurface is nuclear ash; depending on fuel density at burning: intermediate mass elements (“Mg”) or NSE (mixture of “Ni” and ^4He)

Note:

➤ *This has become the preferred method in many recent technical applications involving premixed turbulent chemical flames!*

(e.g., Smiljanowski et al. 1997, Peters 2000, Angelberger et al. 2002, Kraus 2007,)

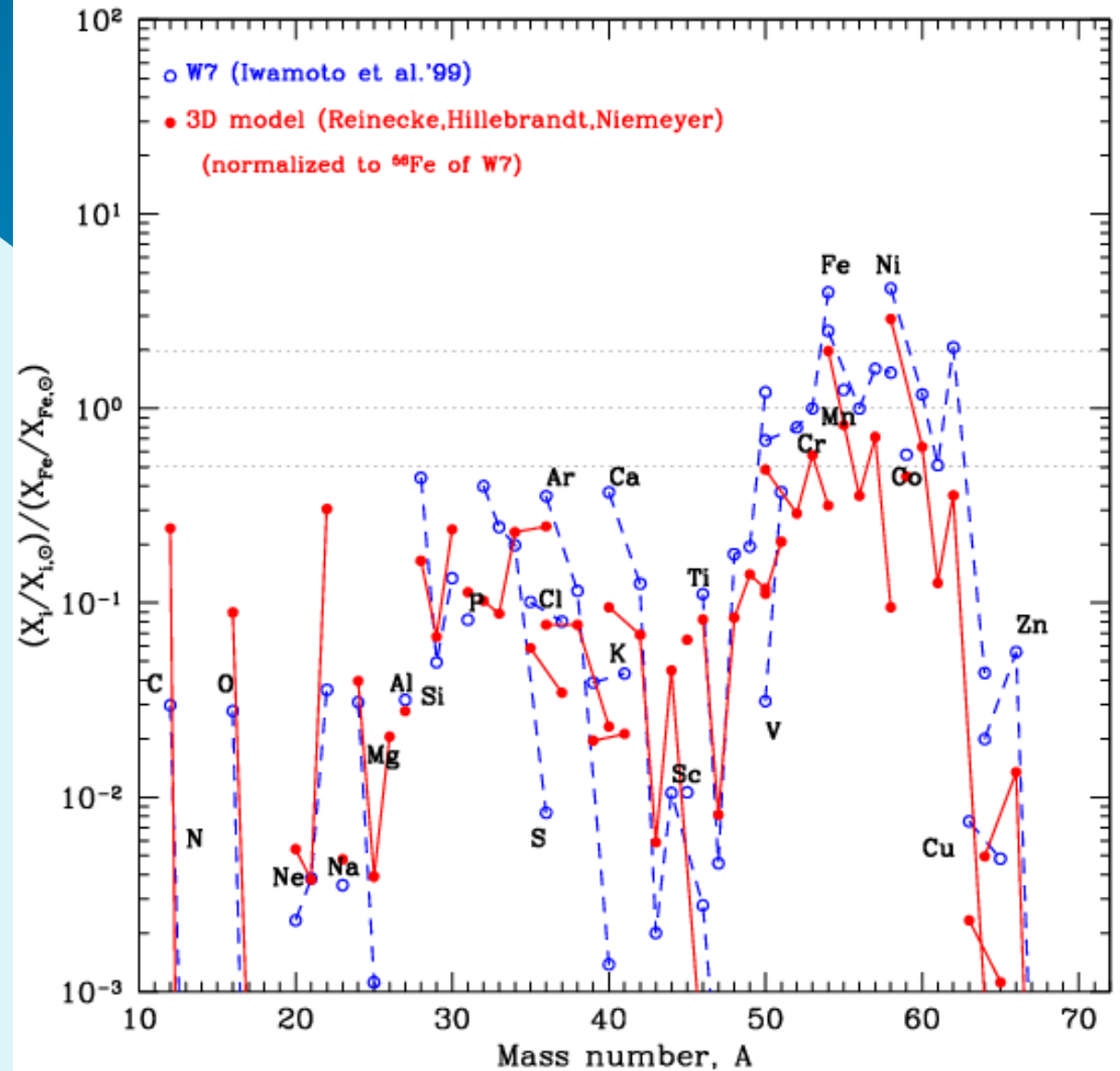
➤ *It is free of adjustable parameters once the subgrid-scale model has been fixed!*

A few 'generic' results

('low-resolution' 3D parameter study)

Nuclear Abundances

(Travaglio et al. 2004,
also Röpke et al. 2006)

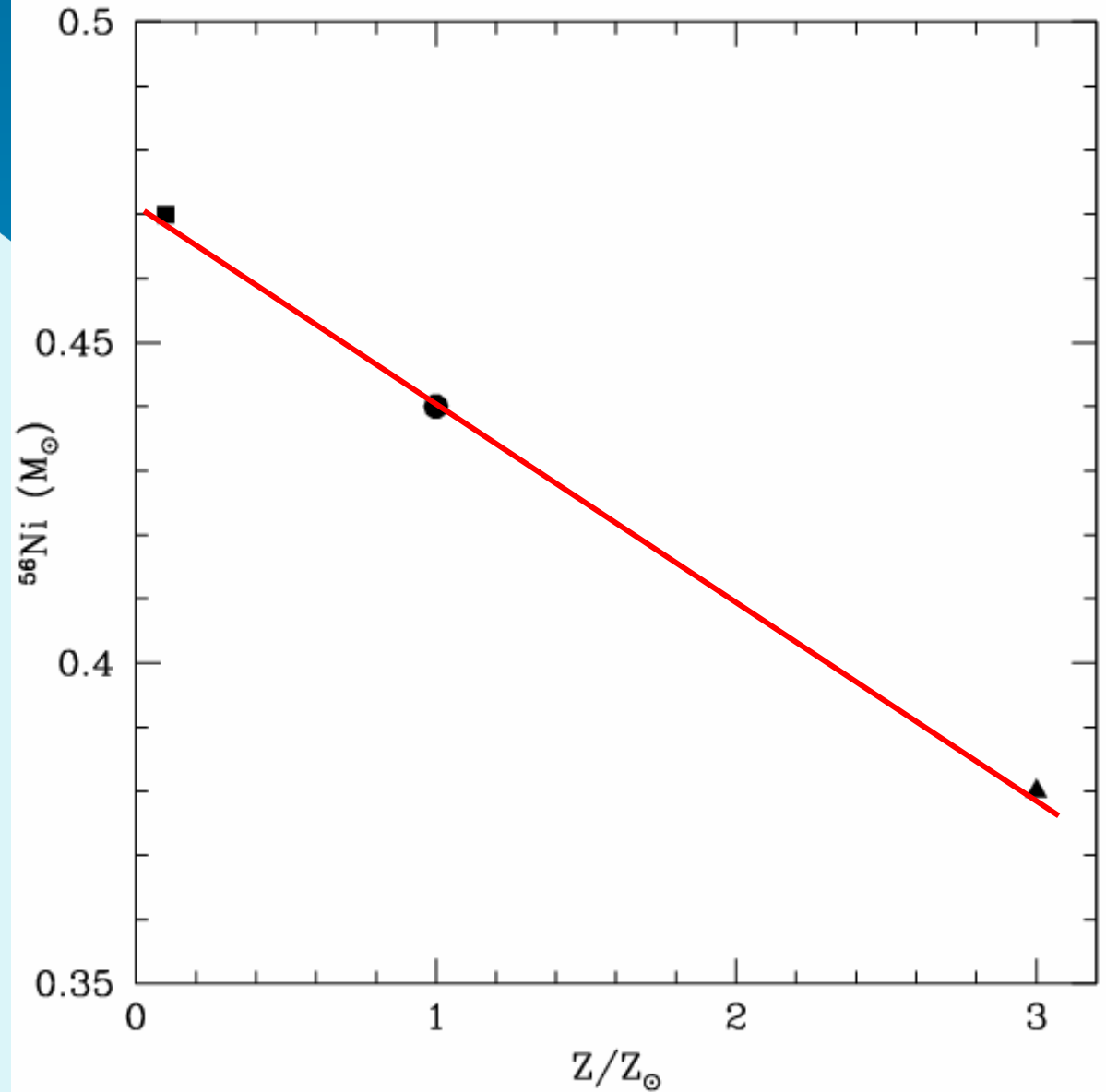


Effects of metallicity

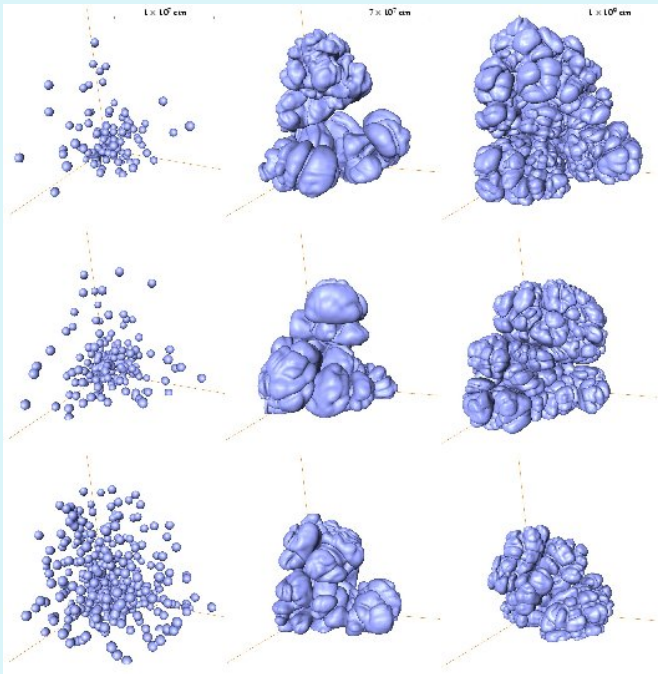
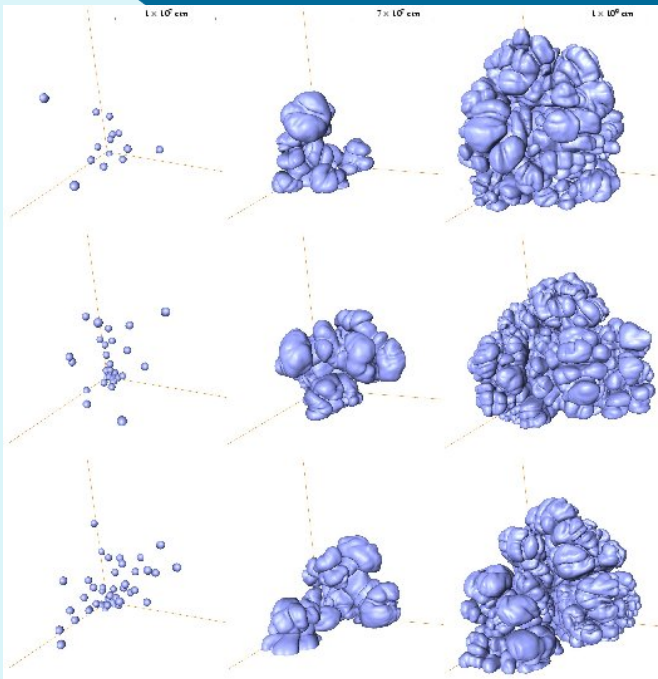
(Travaglio et al. 2005,

Röpke et al. 2006)

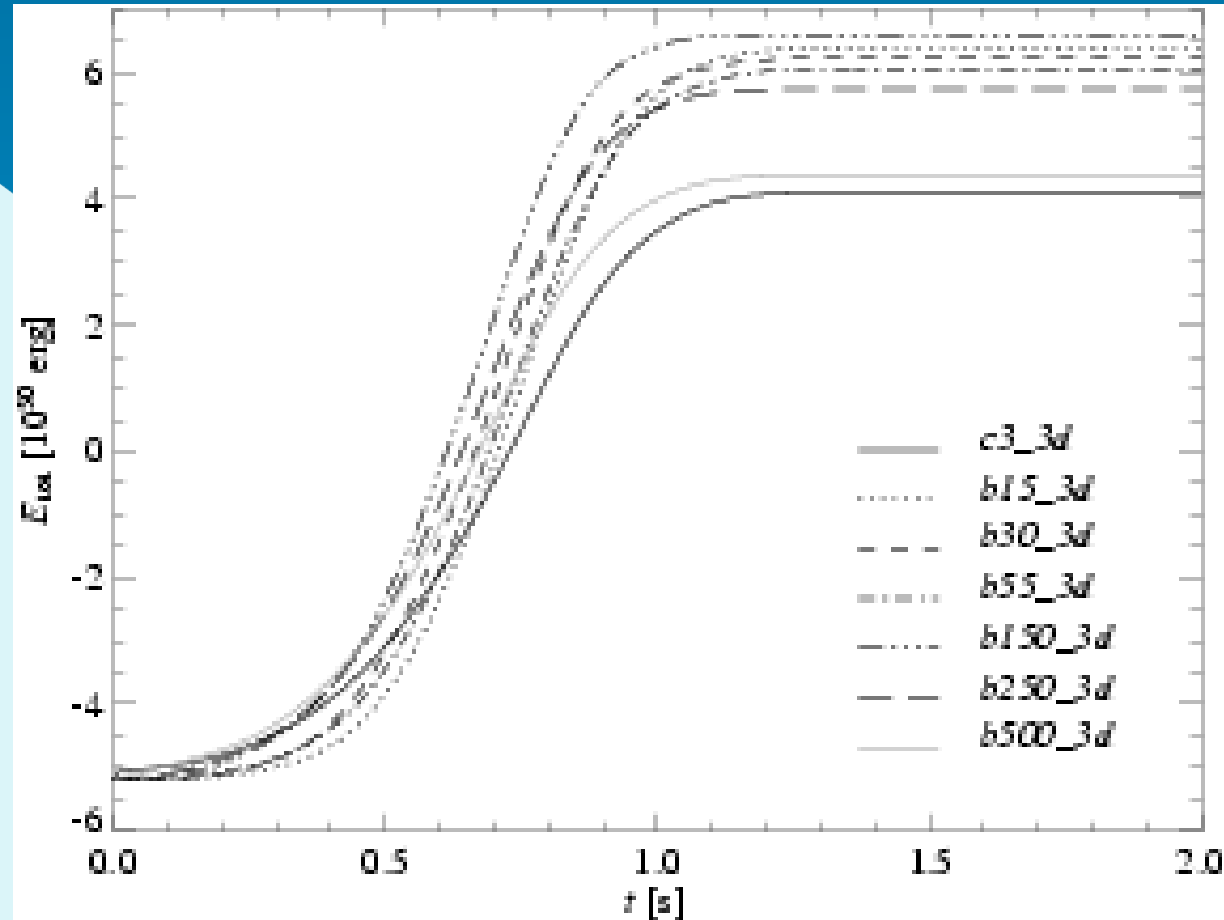
(also Timmes et al.
2003)



Ignition conditions: a reason for diversity?



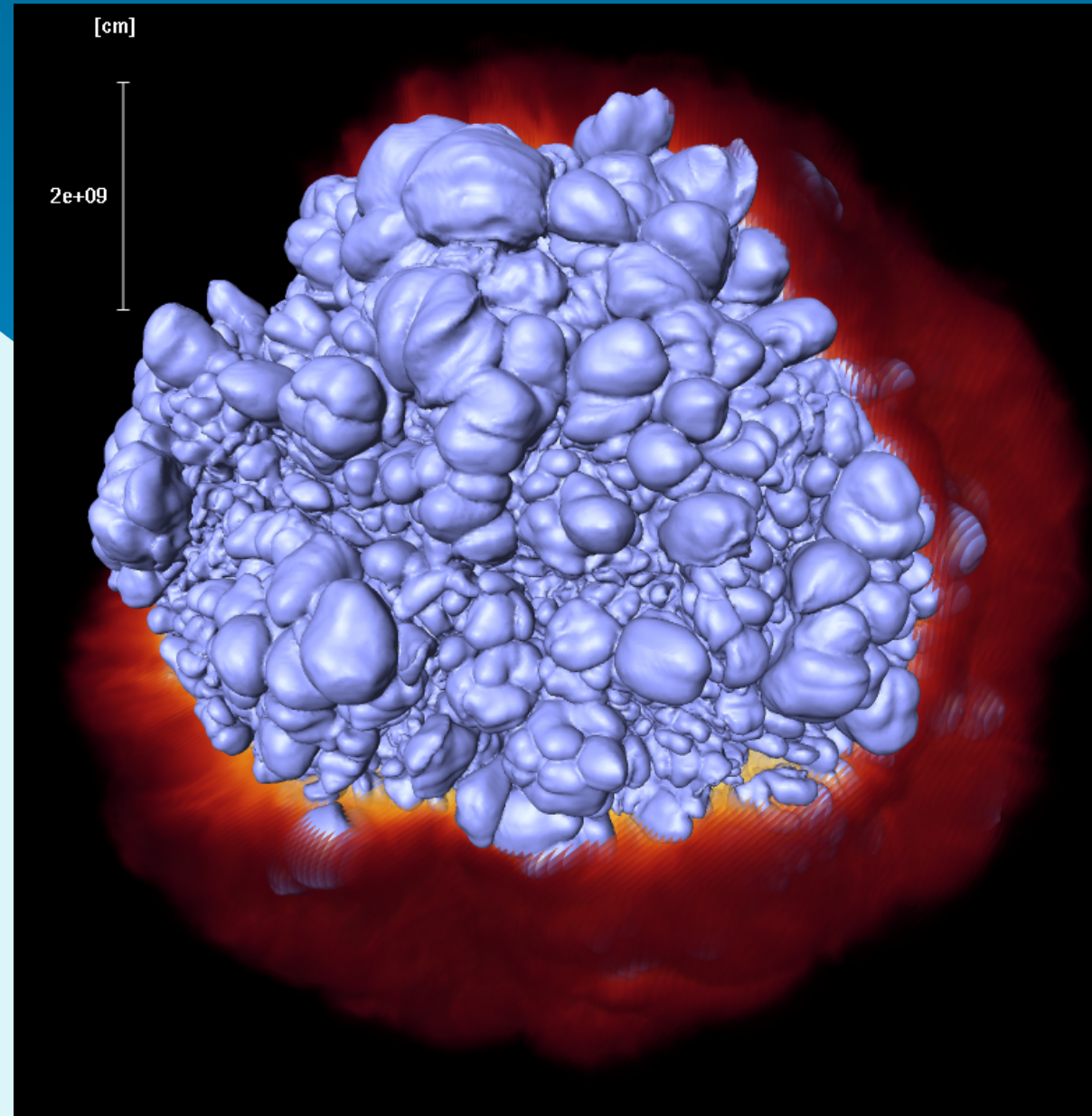
"Multi-spot"



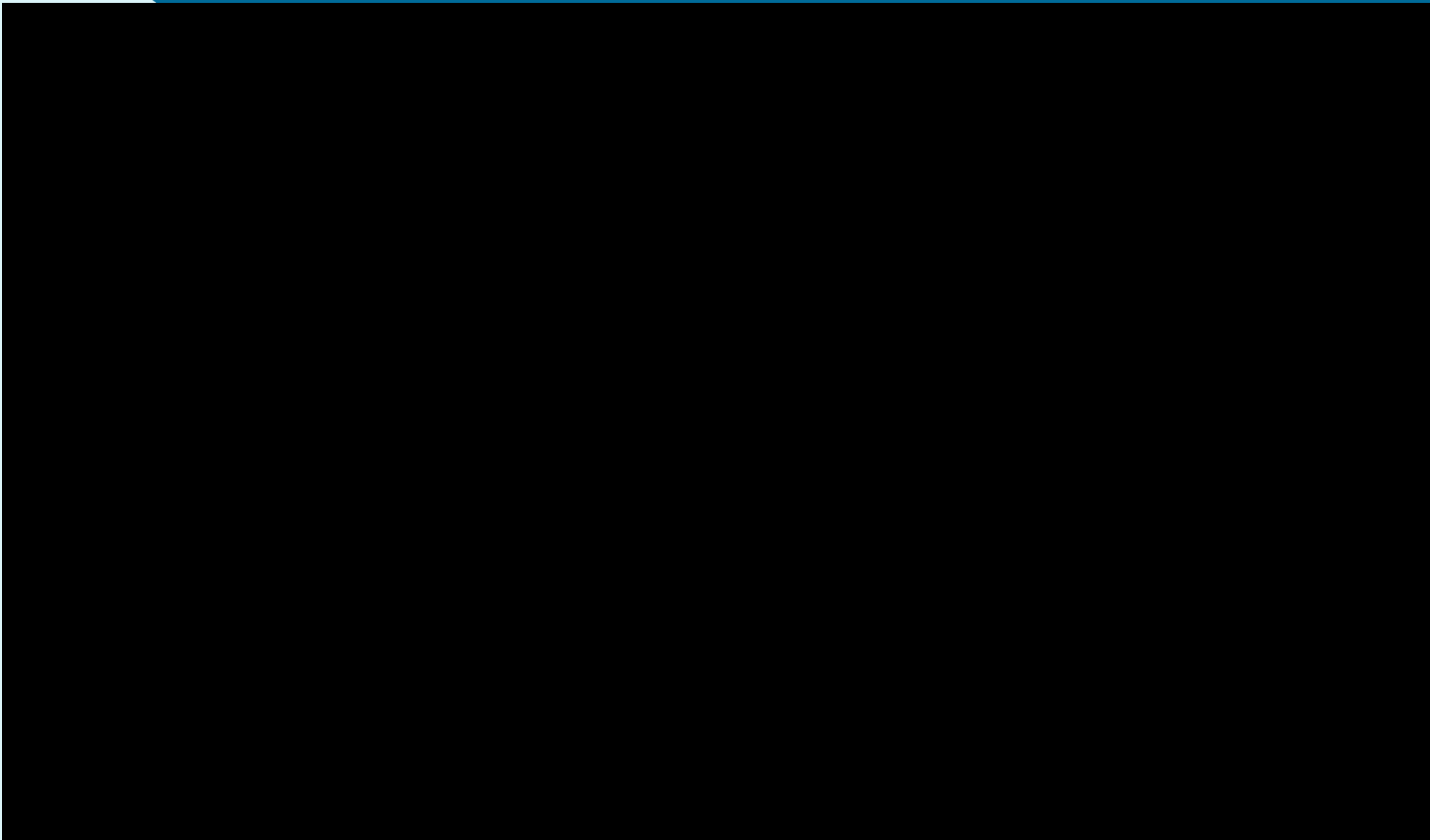
Röpke et al. (2005)

A high-resolution model ('the SNOB run')

- “ 4π ”
- 1024^3 grid
- initial resolution near the center $\approx 800\text{m}$
- moving grid
- Local & dynamical sgs-model
- $\sim 1,000$ h on 512 processors, IBM/Power4, at RZG



(Röpke et al., 2007)

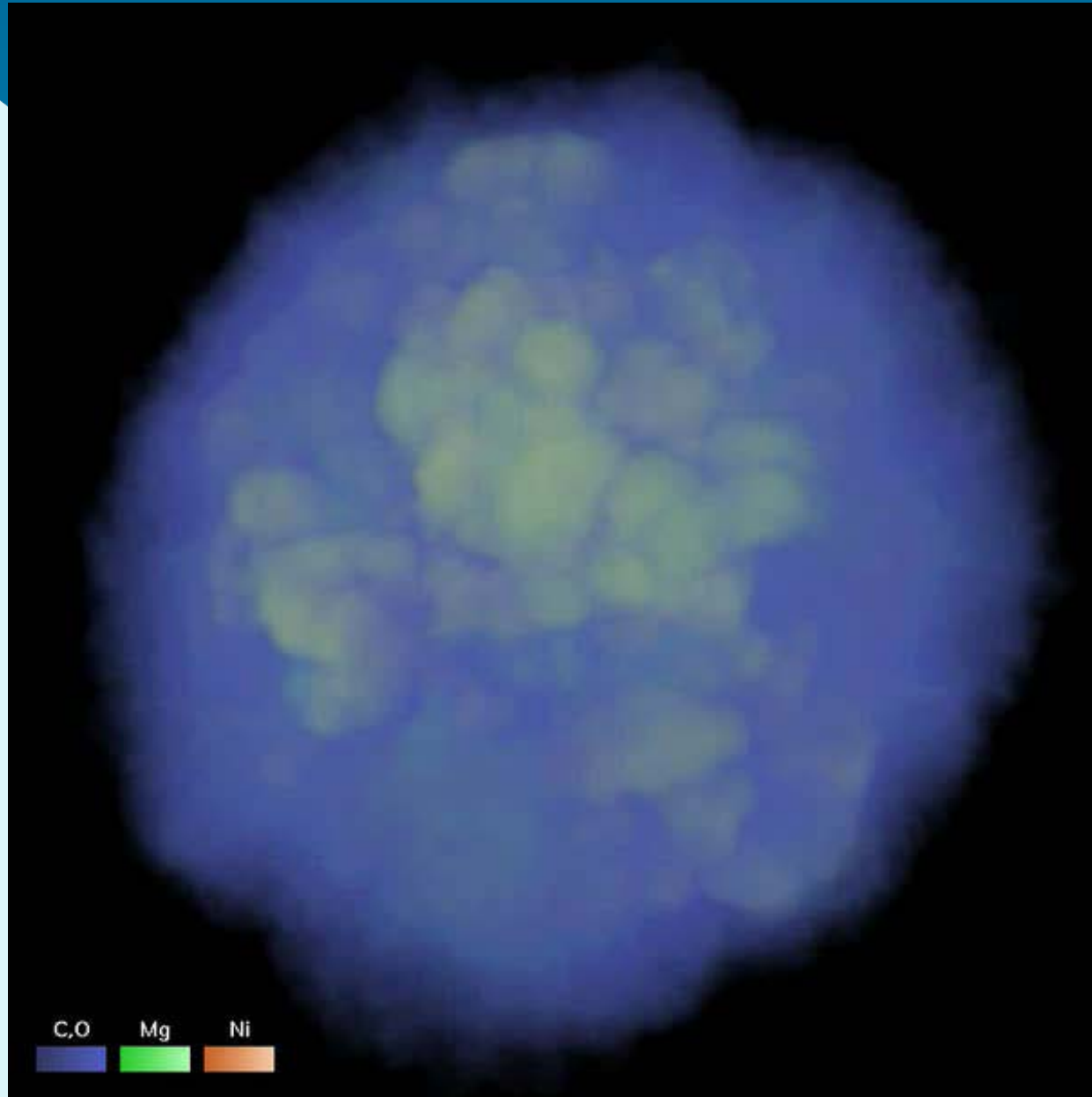


Some important results

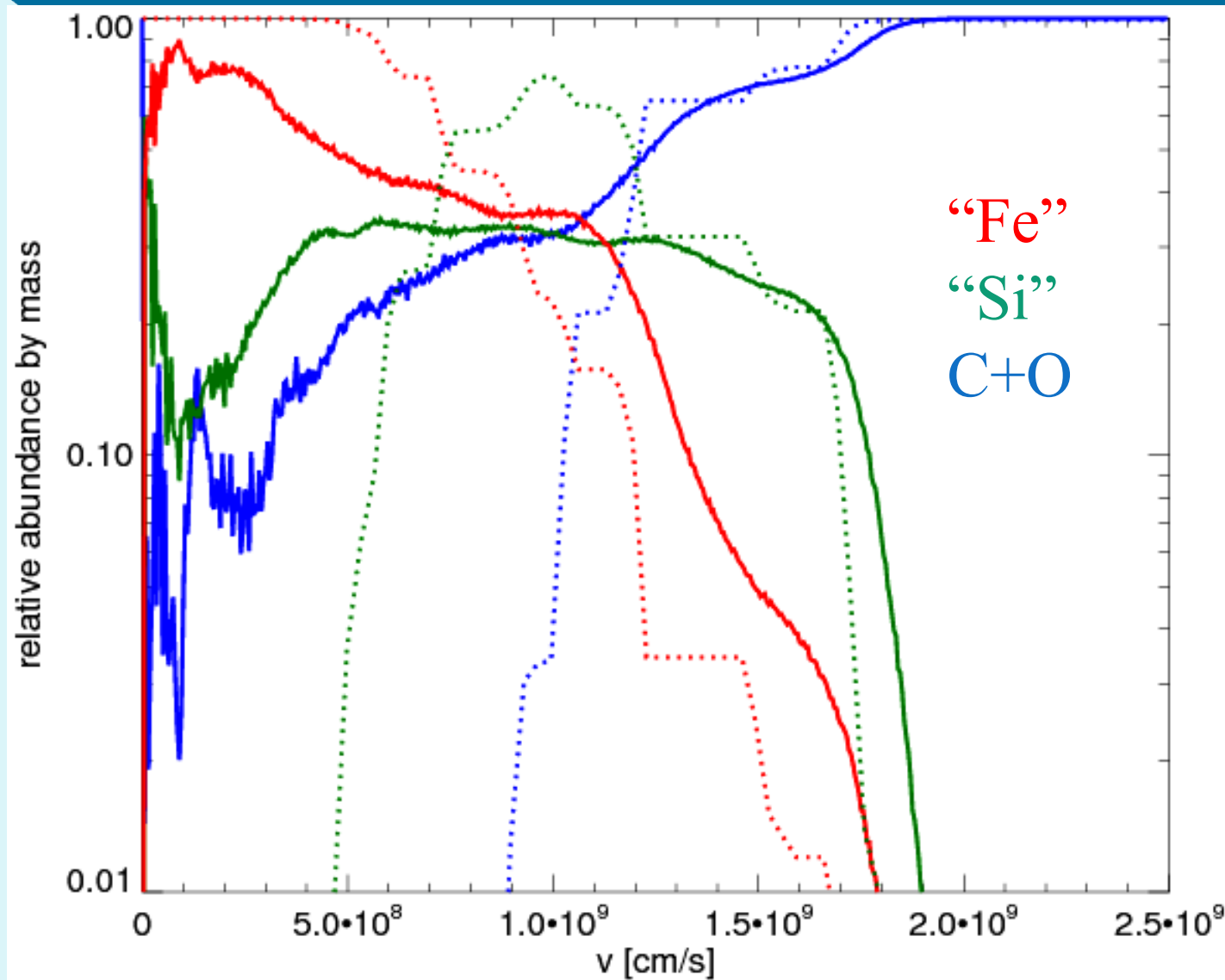
- $E_{\text{kin}} = 8.1 \cdot 10^{50}$ erg (= 0.81 B)
- Iron-group nuclei: $0.61 M_{\text{sun}}$ ($\sim 0.33 M_{\text{sun}} {}^{56}\text{Ni}$)
- Intermediate-mass nuclei: $0.43 M_{\text{sun}}$ (from hydro)
- Unburnt C+O: $0.37 M_{\text{sun}}$ (from hydro)
(less than $0.08 M_{\text{sun}}$ at $v < 8000$ km/s)
- $V_{\text{max}} \approx 17,000$ km/s

Good agreement with observations of some
“normal” SNe Ia!

Example 1: Abundances



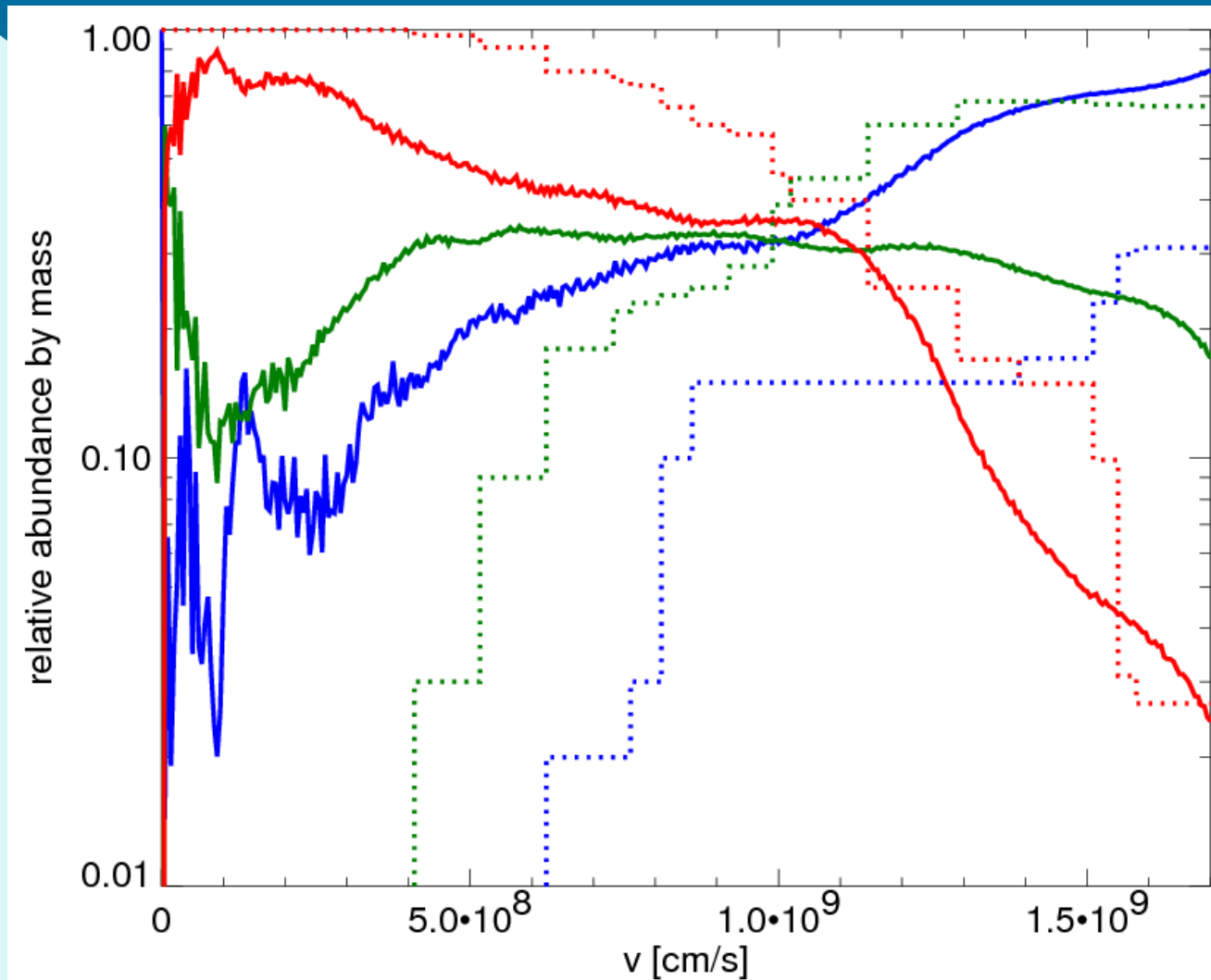
..... and “abundance tomography”



SN 2004eo

(Mazzali et al., 2008)

..... and “abundance tomography”

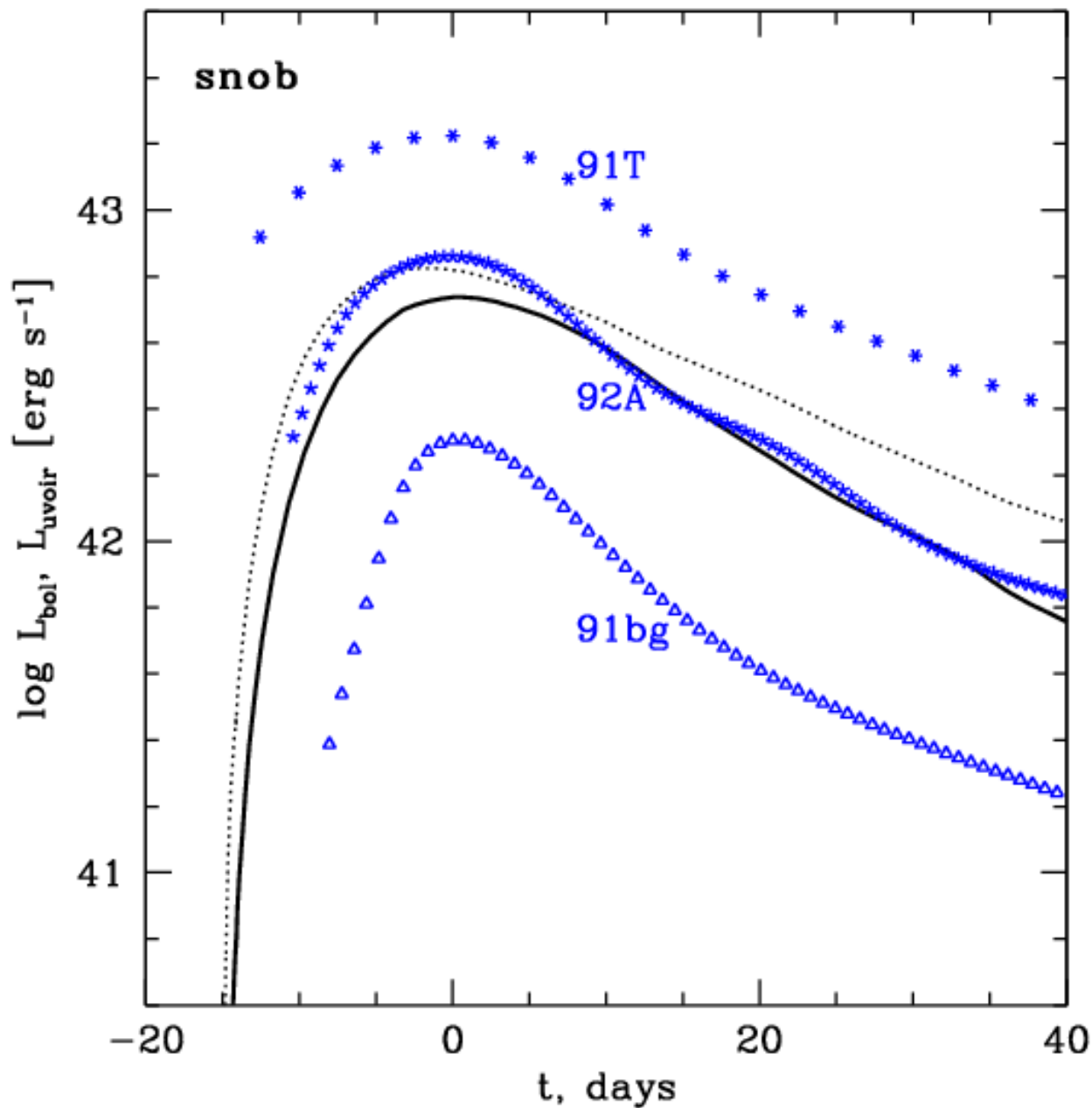


SN 2002bo

vs.

SNOB

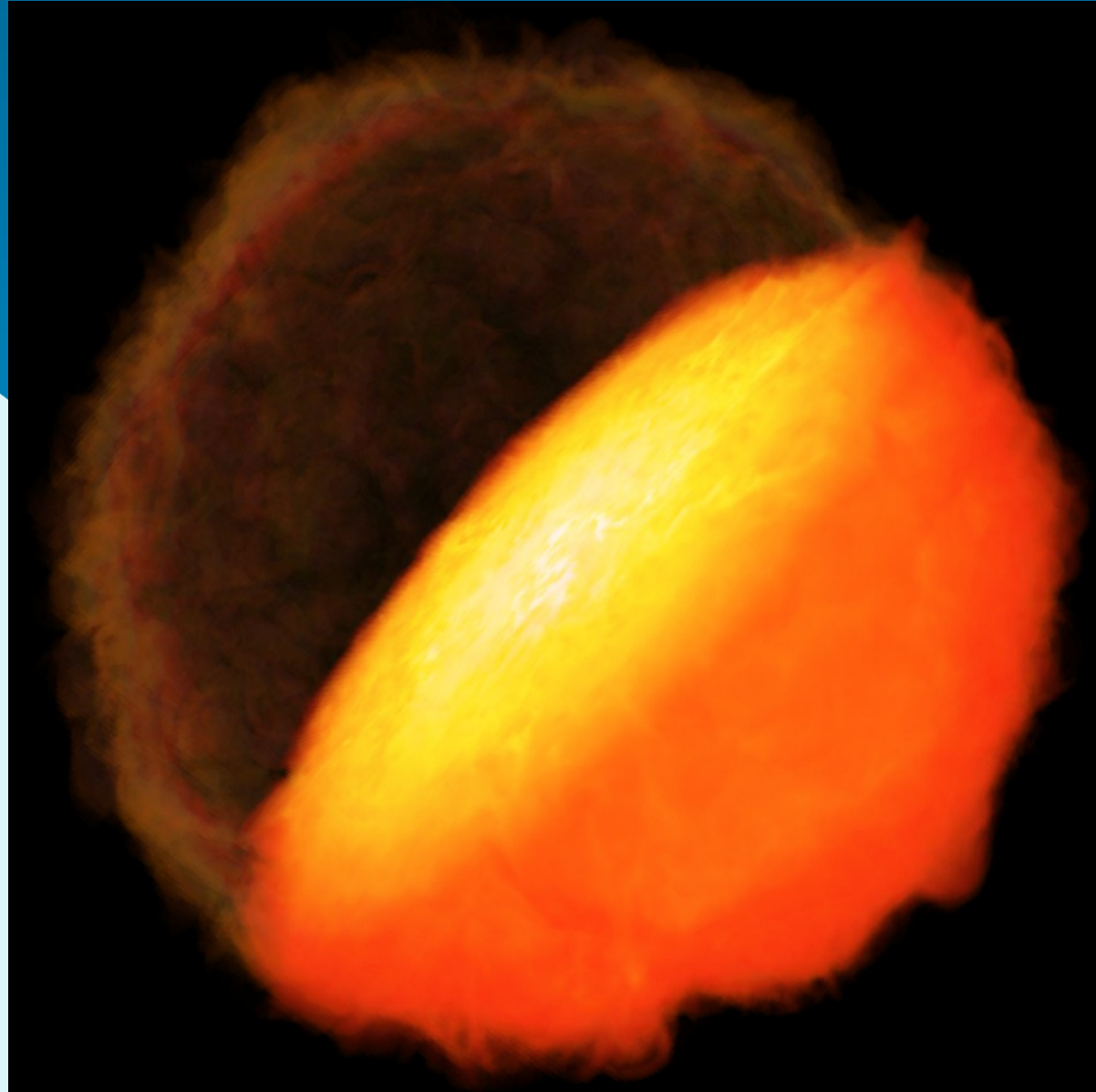
Example 2: Bolometric light curve



Note:
These are
predictions,
not fits!

Changing physical parameters: ignition density

- “ 4π ”
- 640^3 grid
- initial resolution near the center $\approx 1000\text{m}$
- moving grid
- Local & dynamical sgs-model
- $\sim 200,000$ CPUh on IBM/Power5, at EPCC



Röpke et al. (in preparation)

Preliminary results:

- $E_{\text{kin}} = 7.7 \cdot 10^{50}$ erg (= 0.77 B)
- Iron-group nuclei: $0.55 M_{\text{sun}}$ (mostly ^{56}Ni !)
- Intermediate-mass nuclei: $0.47 M_{\text{sun}}$
- Unburnt C+O: $0.38 M_{\text{sun}}$
- $V_{\text{max}} \approx 16,000$ km/s

nova less

Observations?

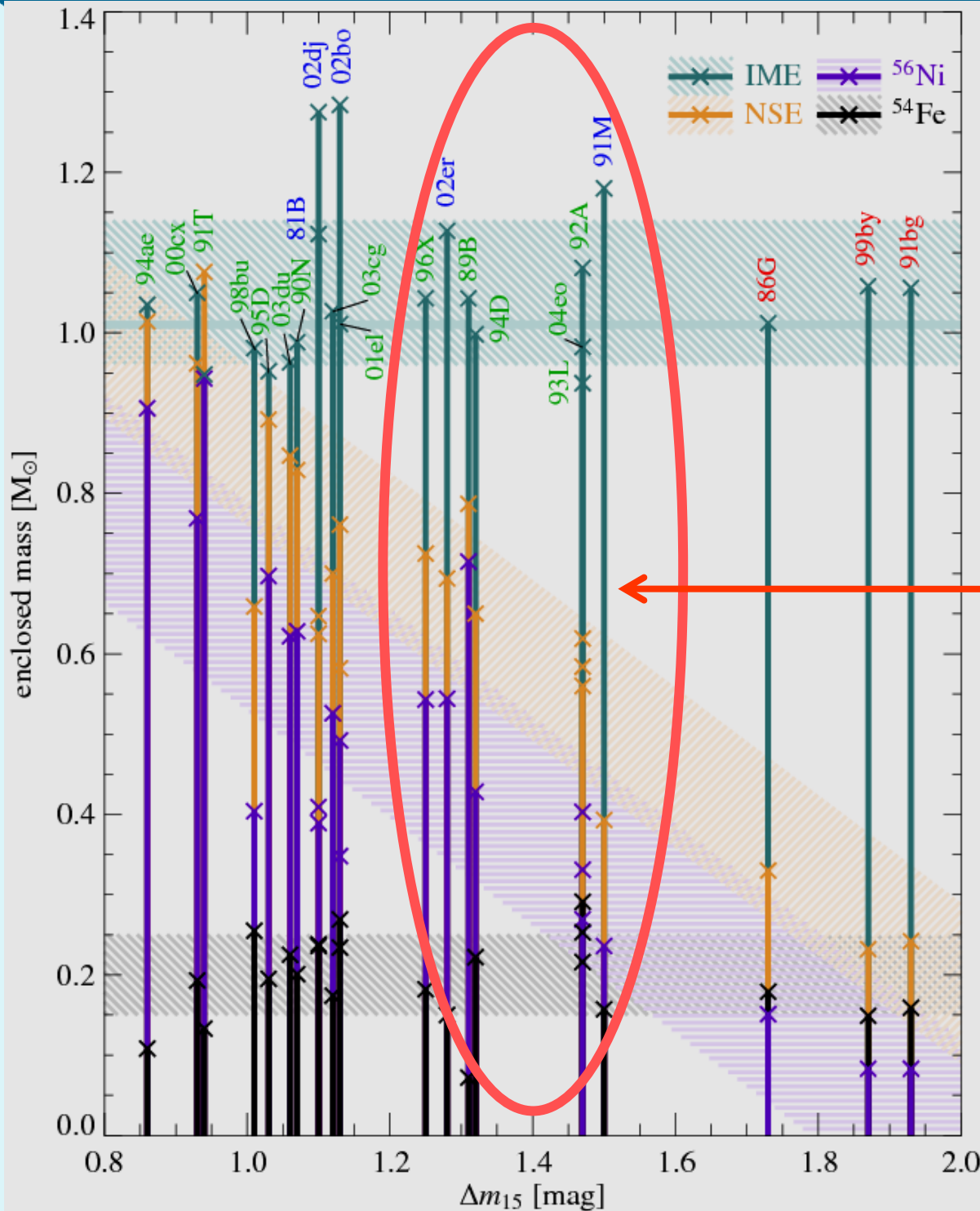
Röpke et al. (in preparation)

Summary and conclusions

- "Parameter-free" thermonuclear models of SNe Ia, based on (Chandrasekhar-mass) white dwarfs explode with about the right energy.
- They allow to predict light curves and spectra, depending on physical parameters!
- The diversity may be due to:
 - Ignition conditions (or other physical parameters).
 - Or deflagration-to-detonation transitions?

(Gamezo et al. 2004, 2005; Röpke & Niemeyer 2006, Woosley 2007, Röpke 2007)

The 'Zorro' diagramme



Pure deflagrations!

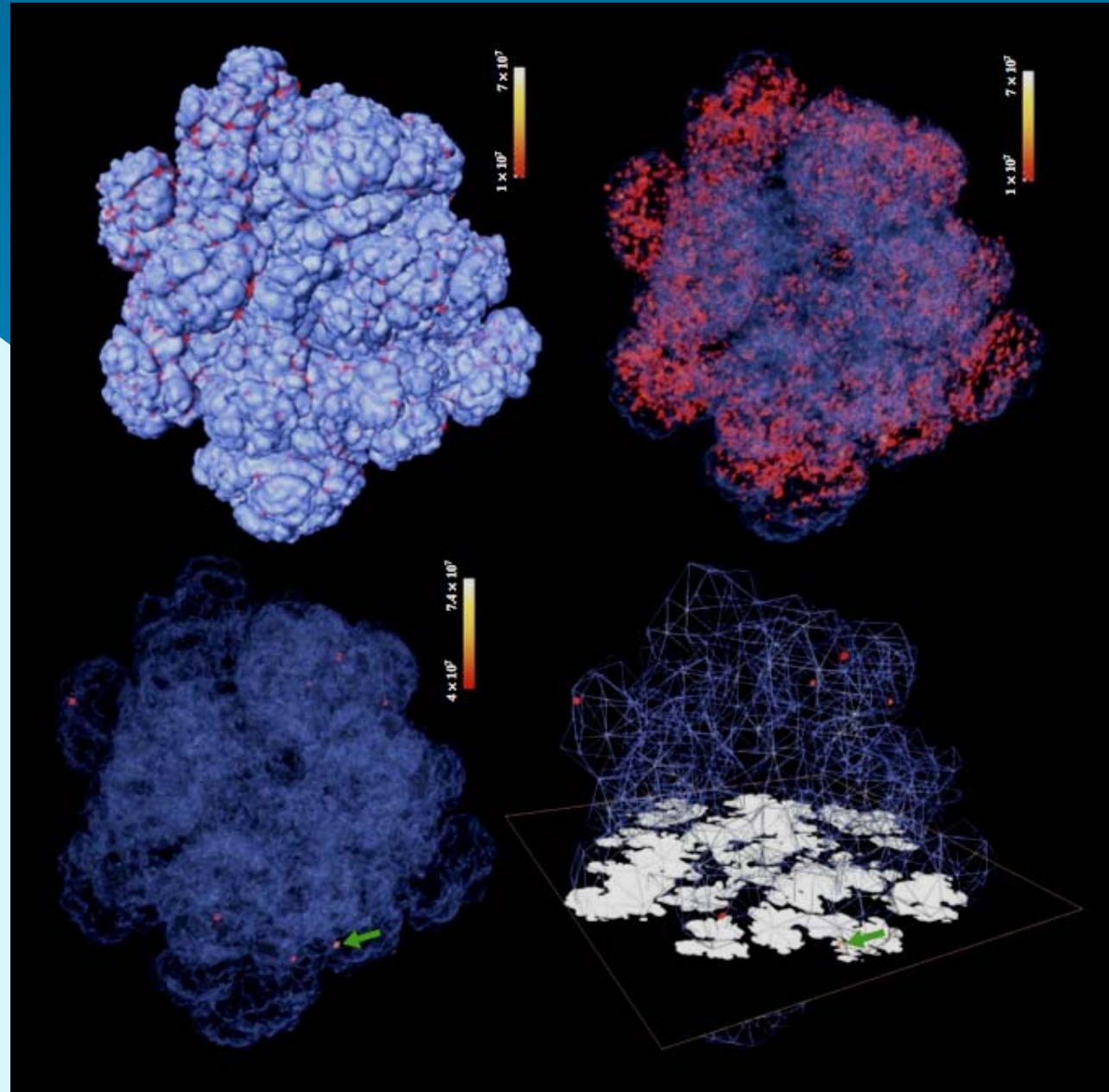
Mazzali et al. (2007)

Deflagration-to-detonation transitions?

Analysis of turbulent velocity fluctuations

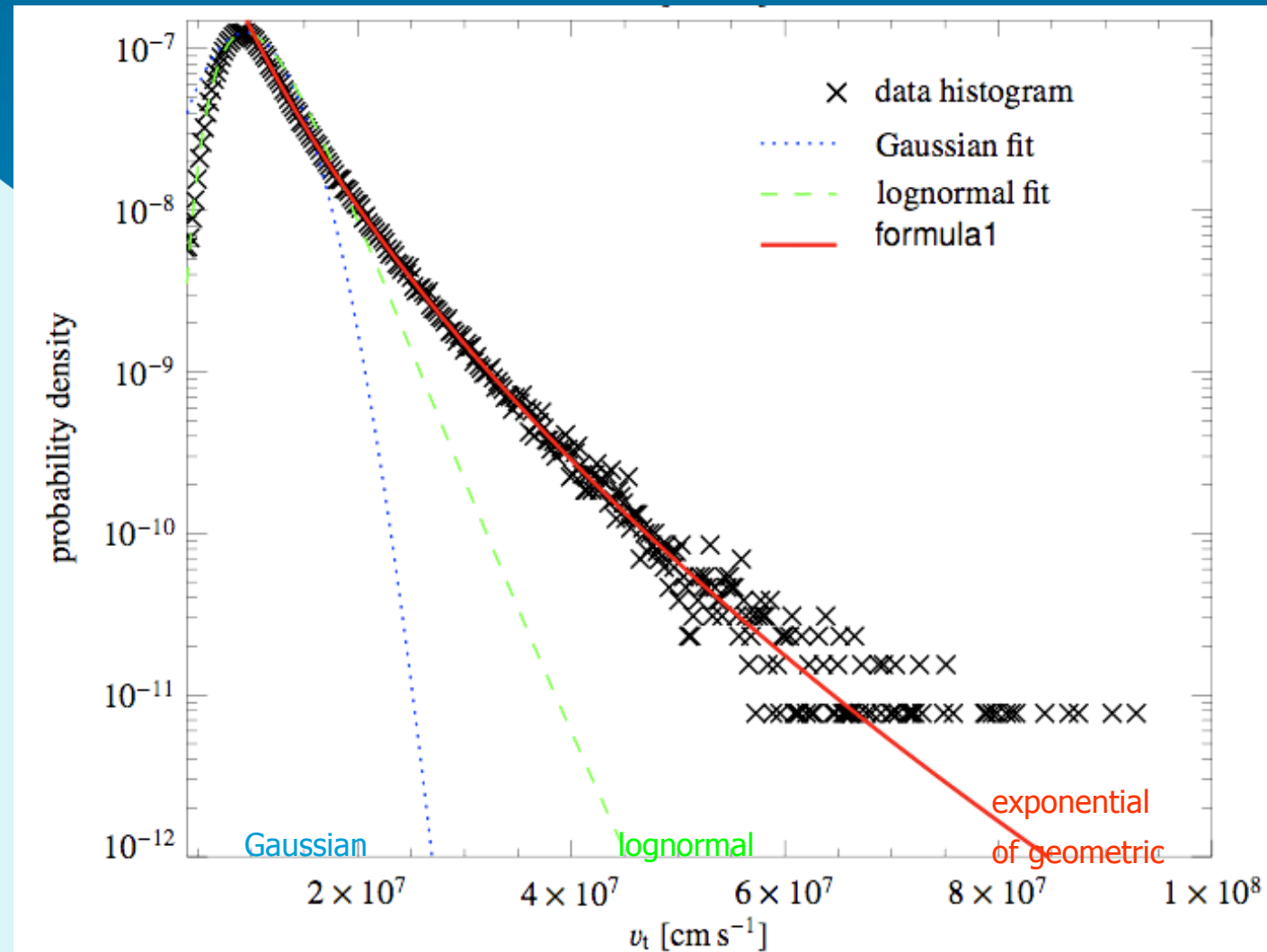
(as predicted by
sub-grid scale model
at the flame front
for densities
 $1 \dots 3 \cdot 10^7 \text{ g cm}^{-3}$)

(Röpke 2007)



Deflagration-to-detonation transitions?

High-amplitude
turbulent velocity
fluctuations
($\sim 10^8 \text{ cm s}^{-1}$)
occur at the onset
of distributed
burning regime
on sufficiently
large area of
flame ($\sim 10^{12} \text{ cm}^2$)



(Röpke 2007)

More questions and challenges

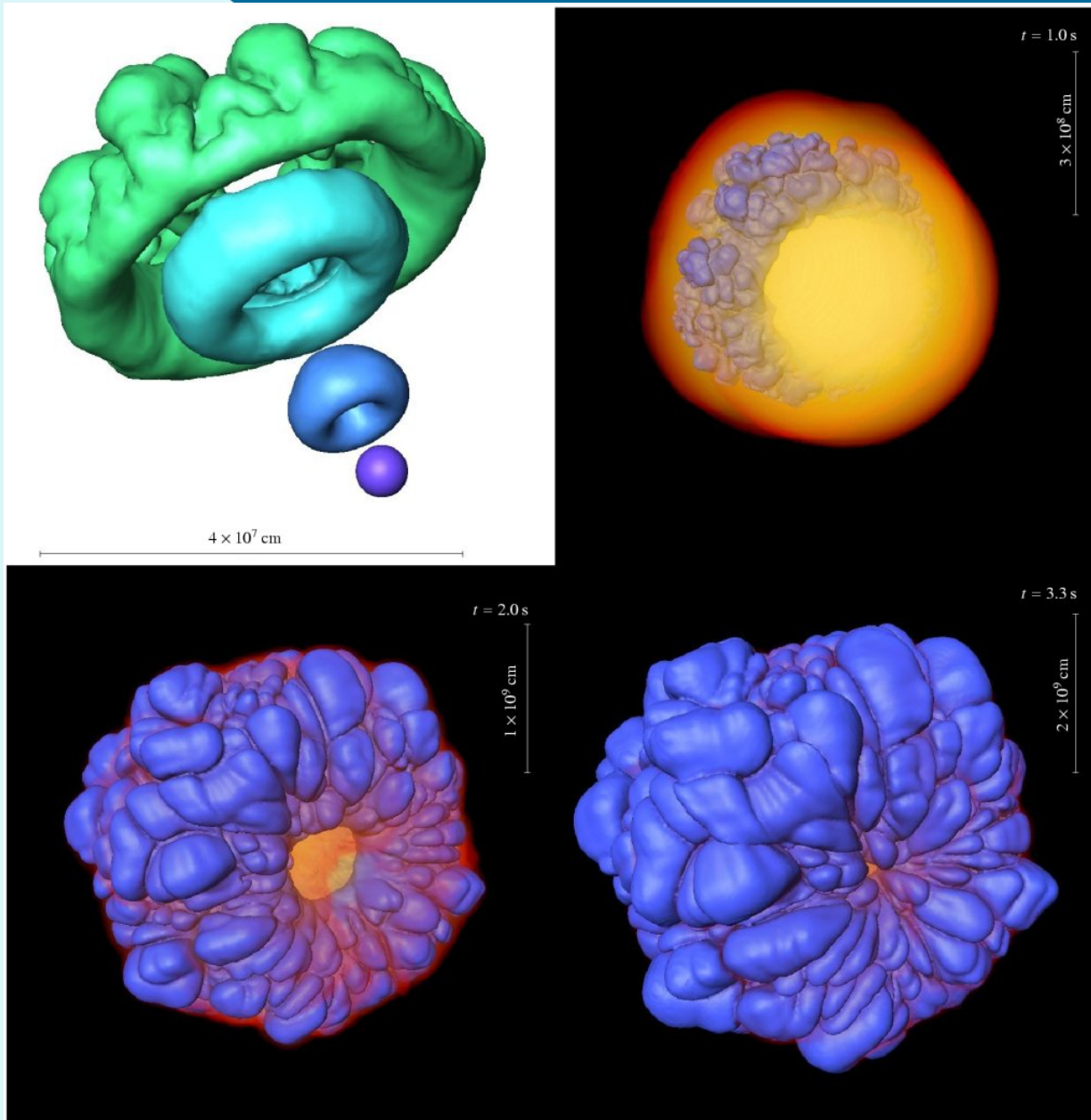
➤ Ignition conditions:

How do WDs reach the critical mass?

Center/off-center ignition?

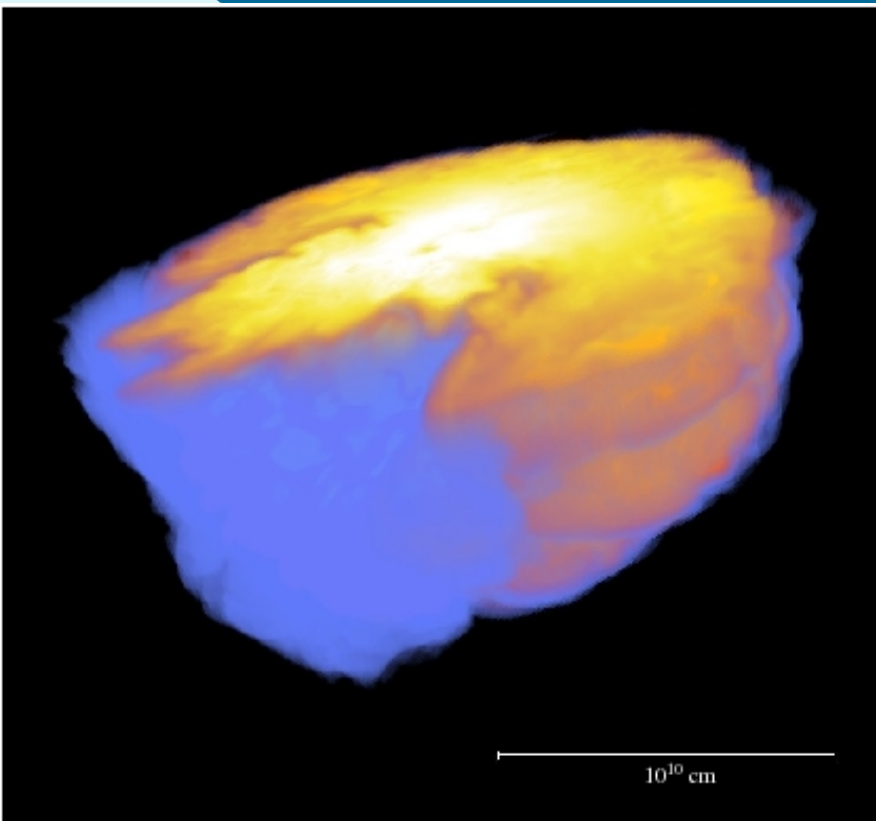
One/multiple 'points'?

Off-center explosions



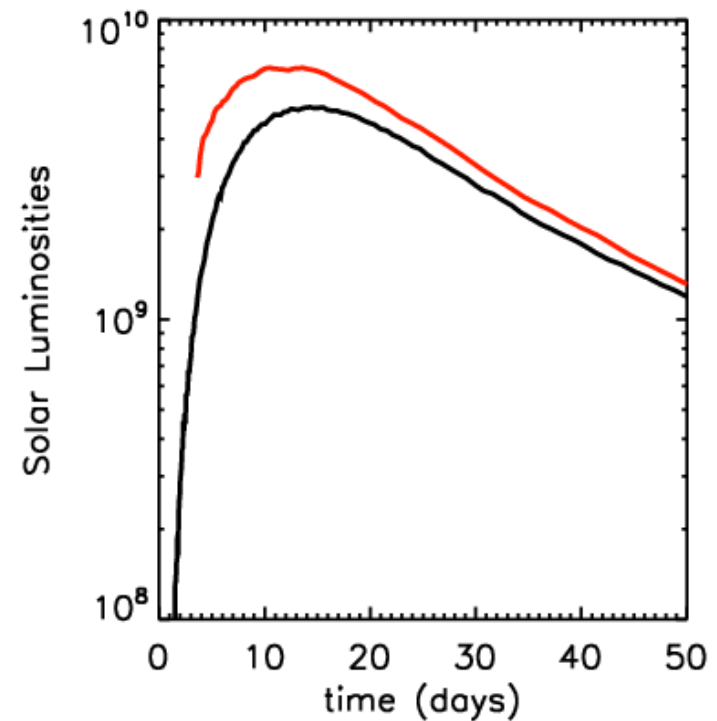
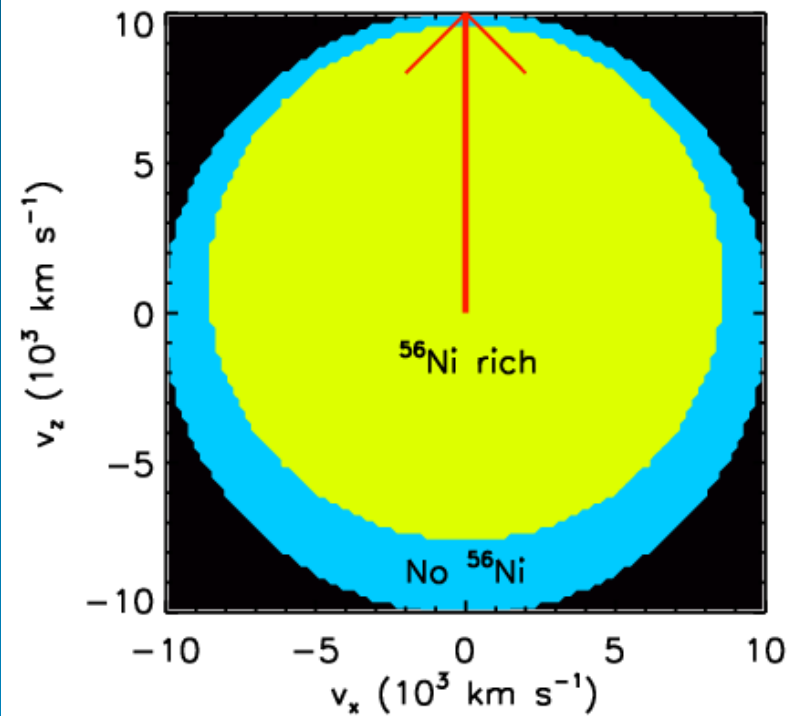
Röpke et al. (2006)
(also Jordan et al., 2008;
Meakin et al., 2008;
Townesley et al., 2007; ...)

.... and their predictions



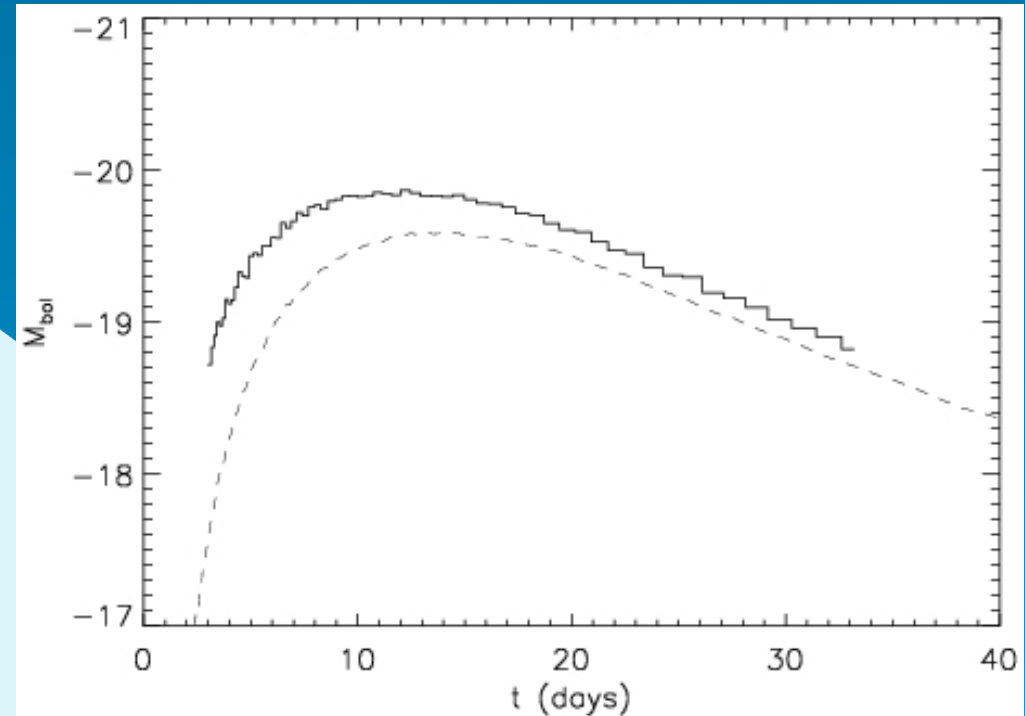
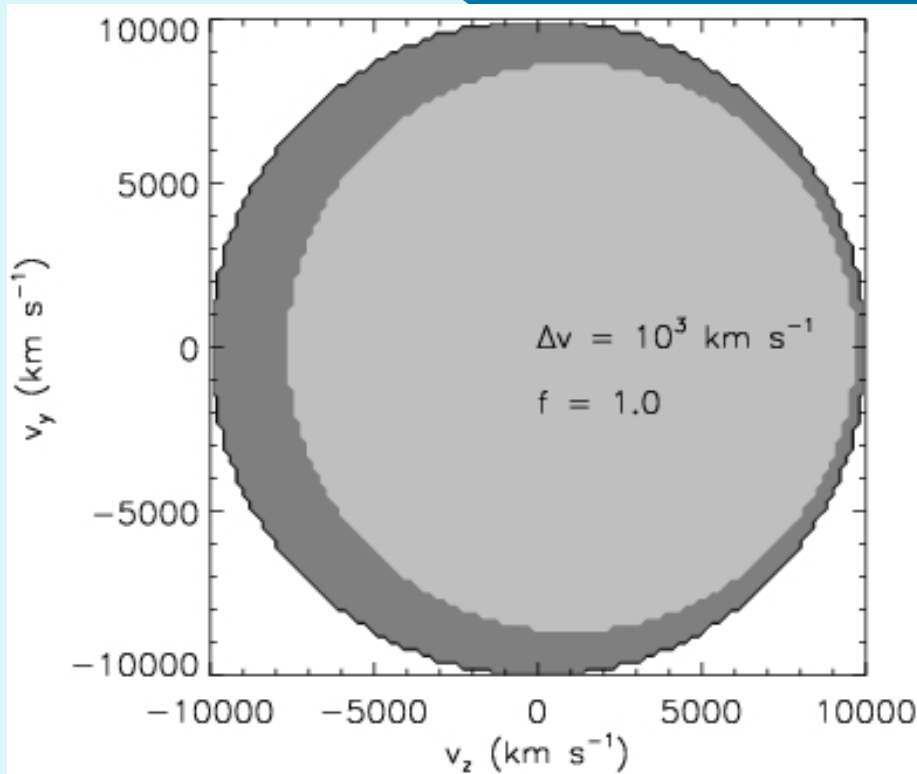
Note: This is a model that has $\sim 0.4 M_{sun}$ of Ni only!

Sim et al. (2007)



How far up can we go in luminosity?

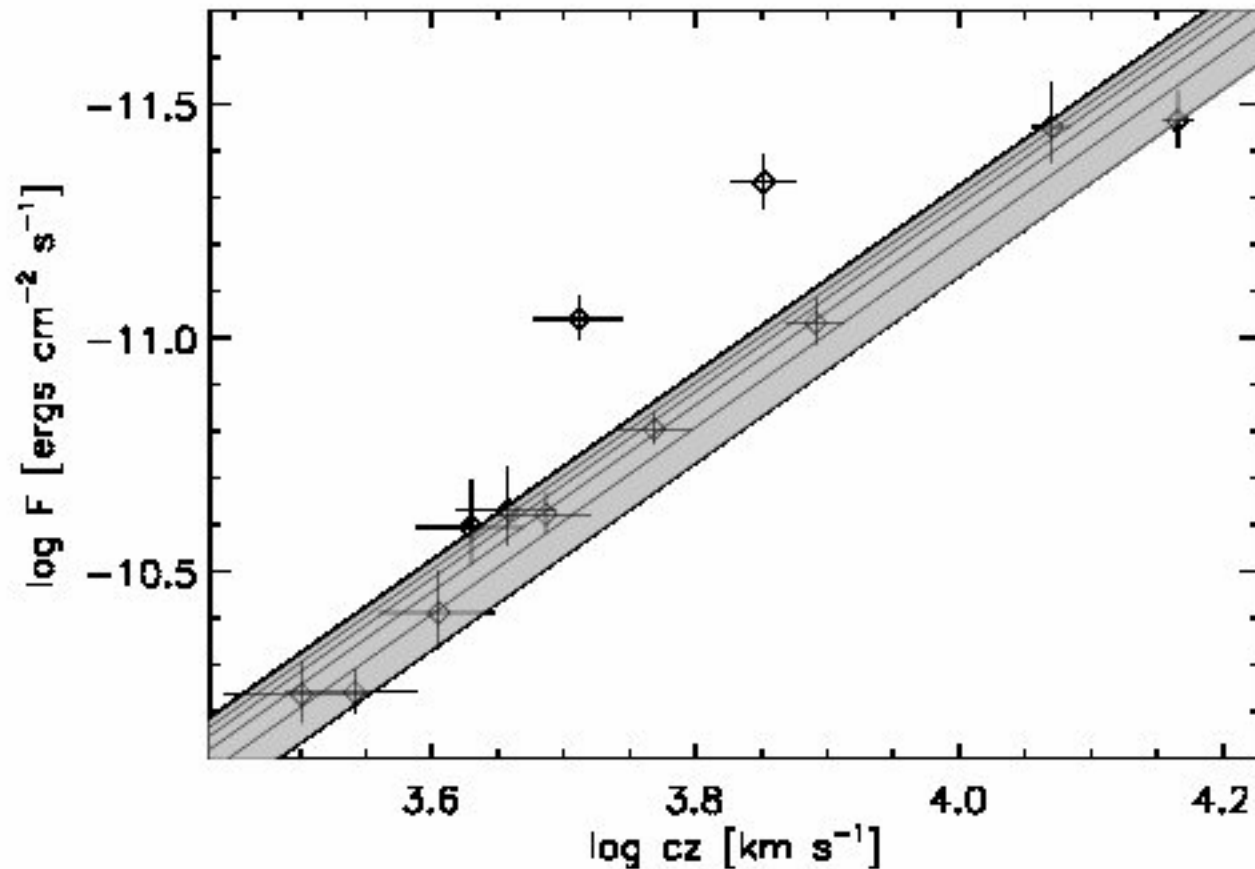
Hillebrandt et al. (2007)



$M_{\text{bol}} \approx -20$ is possible with $\sim 0.9 M_{\text{sun}}$ of Ni!

And what does this mean for cosmology?

Sim et al. (2007)

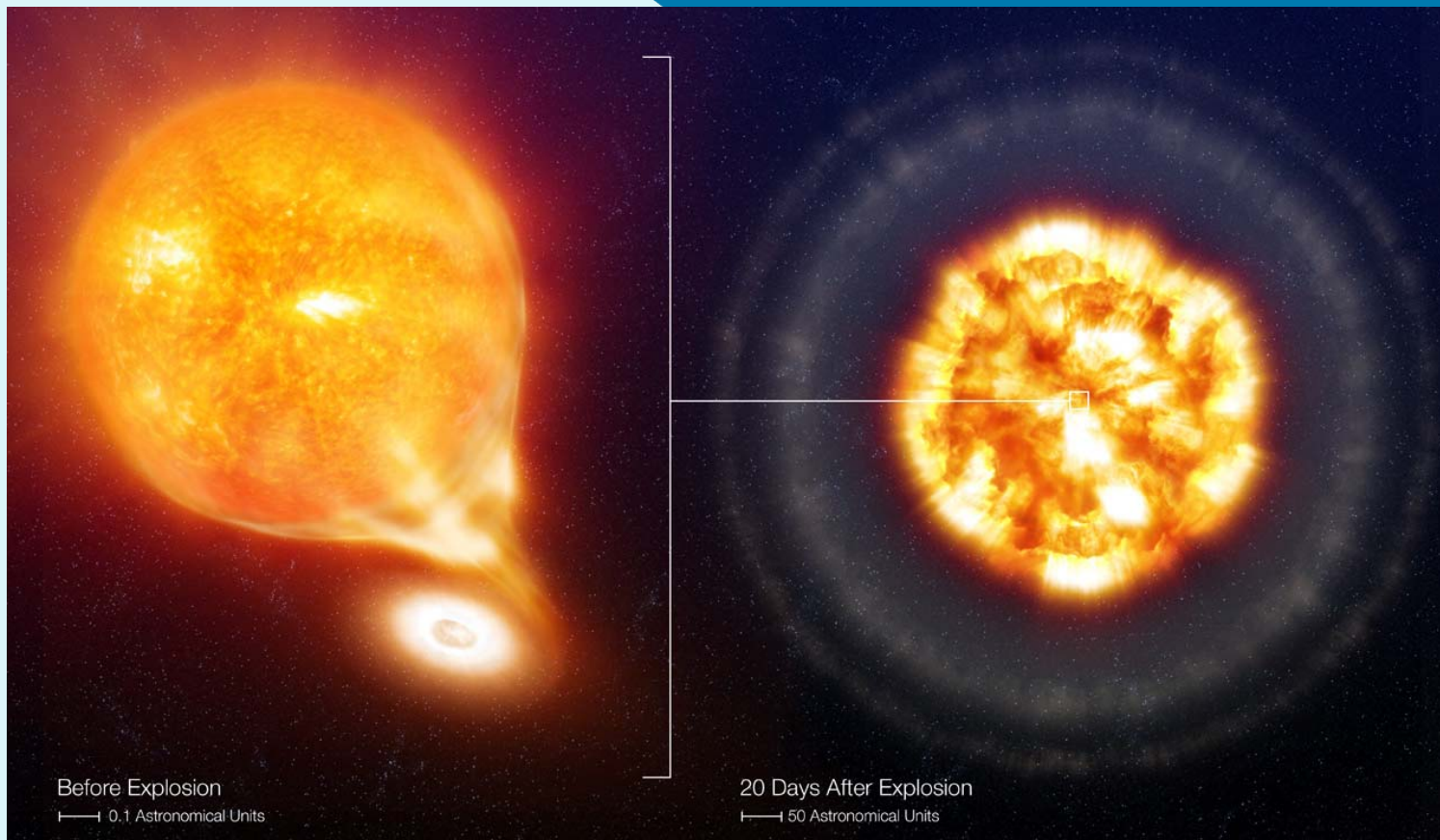


Viewing-angle effects can (in principle) explain the observed scatter in the SN Ia Hubble diagram!

More questions and challenges (cont.)

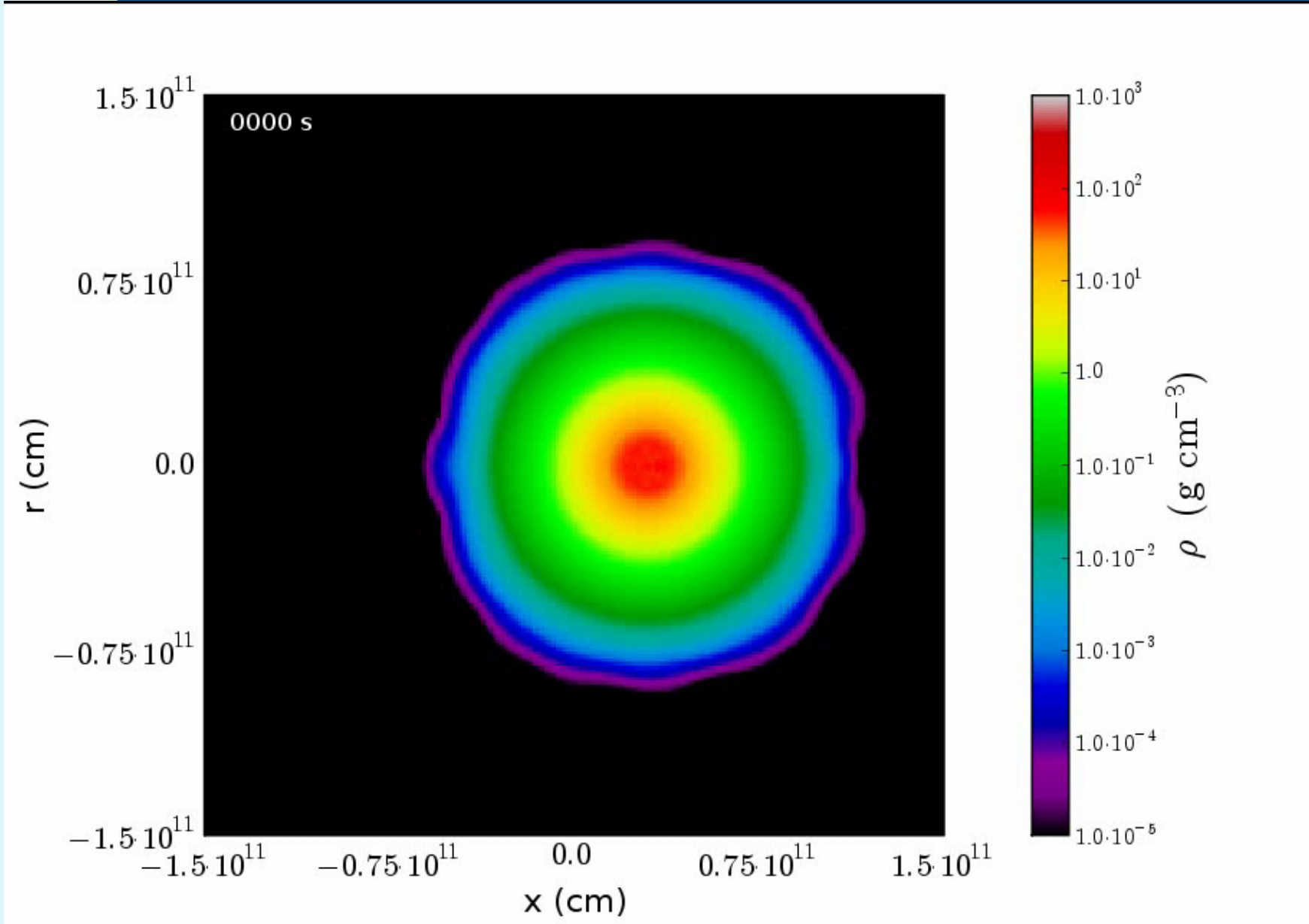
➤ The progenitor question:

Single degenerates? Double degenerates? Sub- M_{ch} explosions?



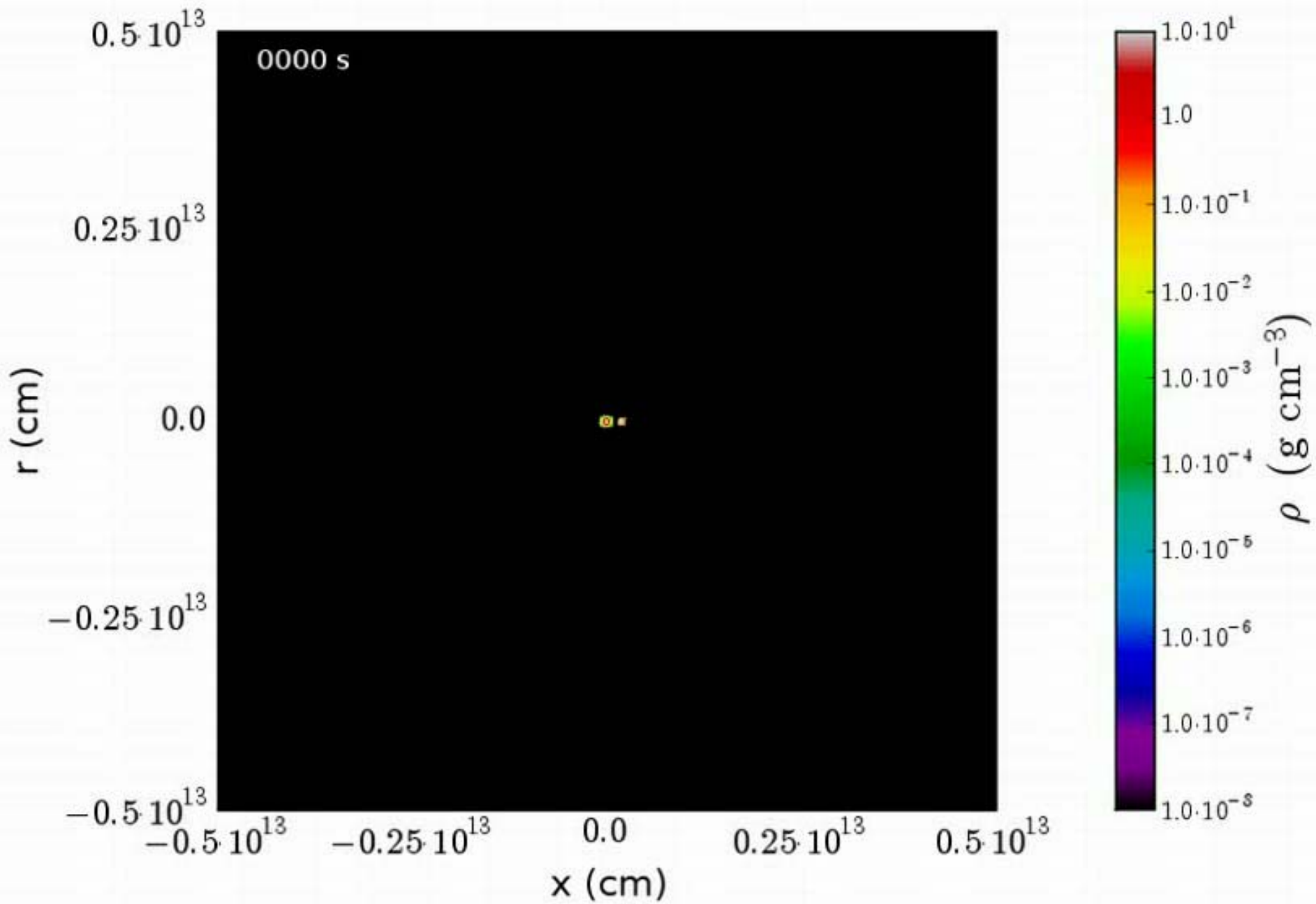
SN 2006X
(Patat et al. 2007)

➤ Should one see the hydrogen?

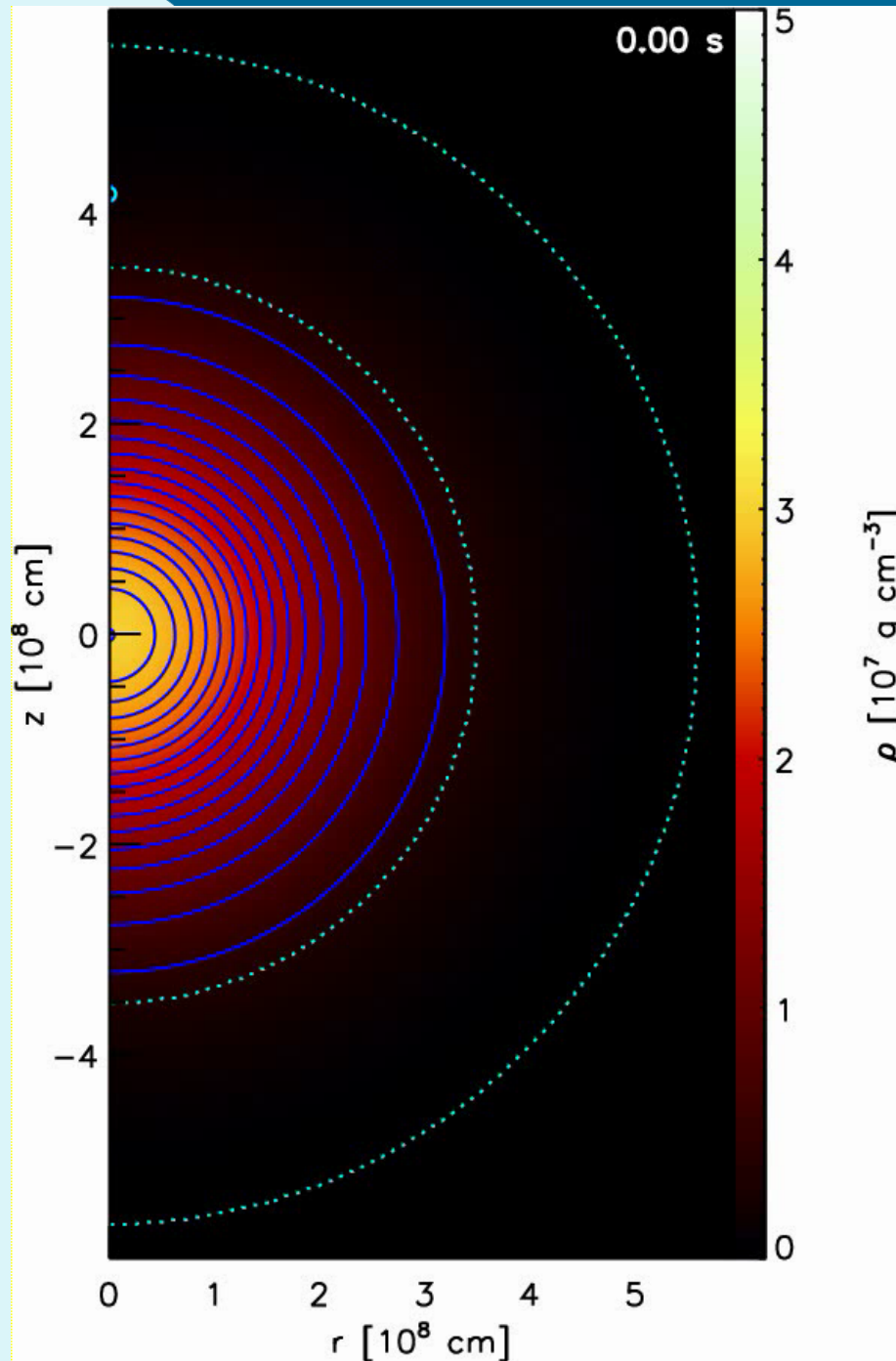


No, not necessarily!

(Pakmor et al., 2008)



A few remarks on sub-Chandra double detonations



(Fink et al., 2007)

- *The He-triggered double detonation is a robust explosion mechanism, provided one can accumulate $\sim 0.1 M_{sun}$ of He.*
- *These explosions would be bright ($\geq 0.4 M_{sun}$ of Ni), but the velocity too high: they would **not** look like any of the observed SNe Ia.*

More questions and challenges (cont.)

➤ New generation of 'full-star' models:

Light curves?

Spectra?

Luminosity calibration?

Key question for supernova cosmology:

There are potential sources of systematic errors.

But: they can be controlled by better models.

Hope has left Pandora's box!