
Relativistic Radiation Mediated Shocks

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Collaborators

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Plan of this talk

■ Introduction

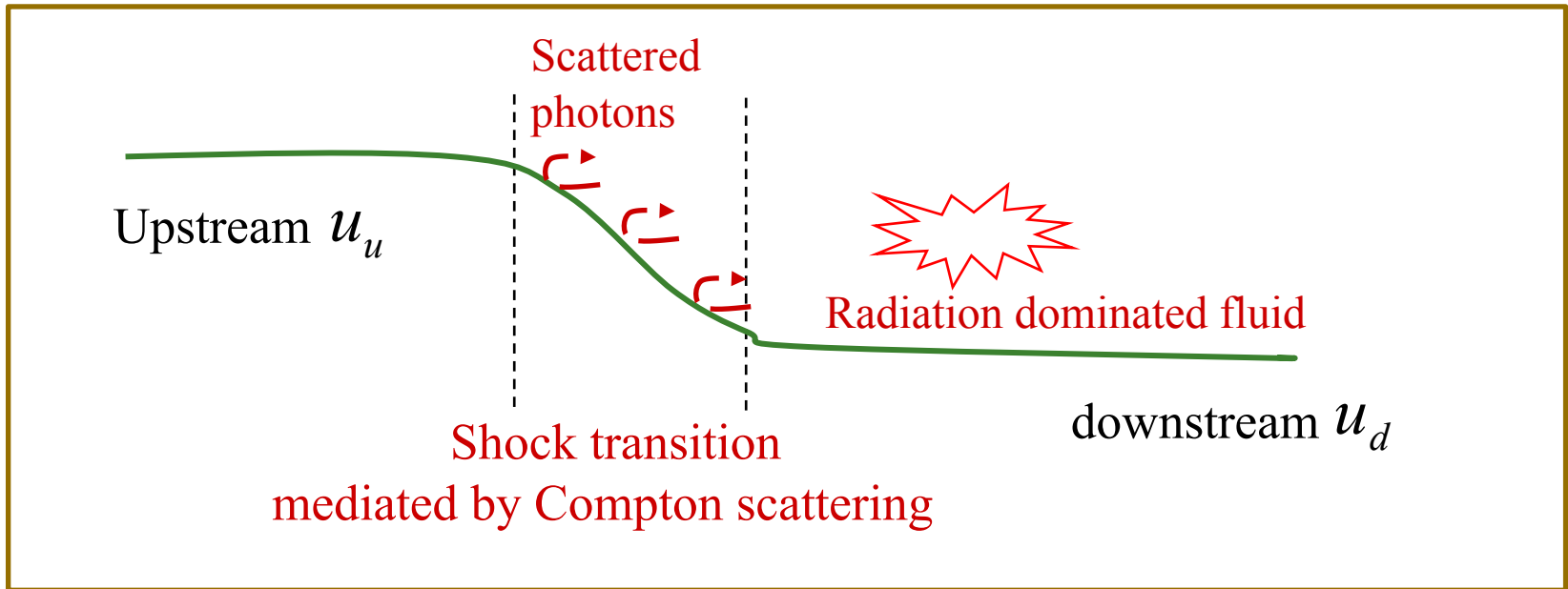
- Brief overview of Radiation Mediated Shocks (RMS)
- Photon rich and photon starved regime
- Non-relativistic and Relativistic RMS (RRMS)
- Motivation

■ Self-consistent calculation of RRMS

- Method for deriving steady solution for RRMS
- Photon rich regime
- Photon starved regime

■ Summary

Radiation Mediated Shocks (RMS)



- downstream energy dominated by radiation
- upstream plasma approaching the shock is decelerated by scattering of counter streaming photons

Under which conditions a RMS forms ?

- Radiation dominance downstream: $aT_d^4 > n_d kT_d$
- Jump conditions : $n_u m_p c^2 \beta_u^2 \approx aT_d^4 / 3$
 $\Rightarrow \beta_u > 10^{-4} \left(\frac{n_u}{10^{15} \text{ cm}^{-3}} \right)^{1/6}$

$$t_{diff} = \tau L / c$$

$$t_{cross} = L / v$$

But requires photon trapping:

$$t_{diff} > t_{cross} \Rightarrow \tau > 1 / \beta_u$$

shock width: $\Delta\tau \sim 1 / \beta_u$ (may be altered by PP and KN)

Why is it interesting?

- The conditions required to form RMS are always satisfied below the photosphere of fast flows
- properties of RMS are vastly different than those of collisionless shocks

Examples: shock breakout in SNe, LLGRB, etc
sub-photospheric shocks in GRBs
NSNS mergers
accretion flows

Shock breakout

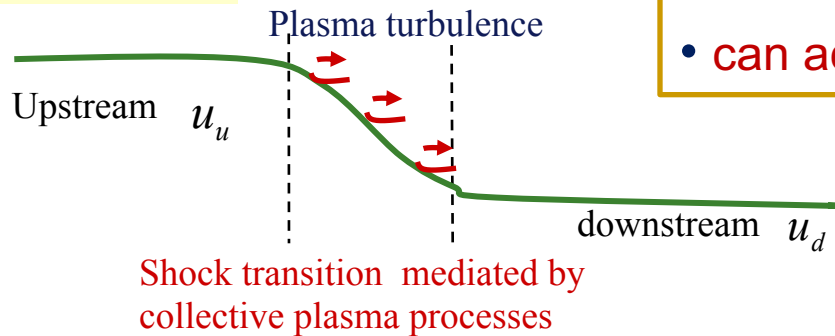
- Transition from RMS to collisionless shock..
- Breakout signal depends on structure of RMS

Breakout when $\tau \sim 1/\beta_u$

- From edge of stellar envelop (SNe).
- From a stellar wind (SNe, LLGRB)
- From a moving ejecta (GRBs, NS mergers)

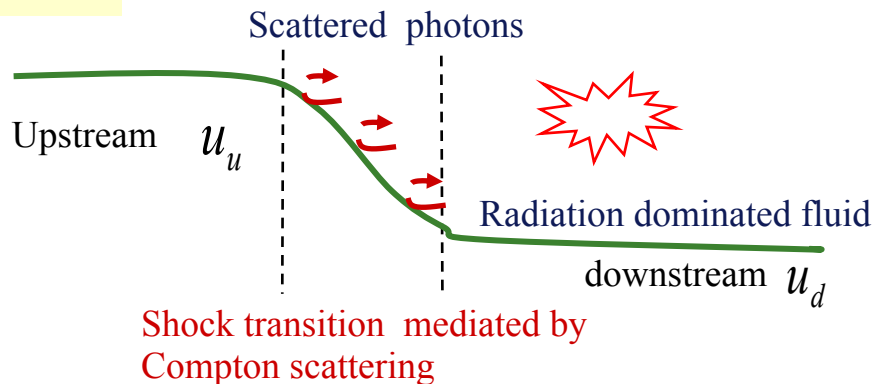
Collisionless shocks .vs. RMS

collisionless



- Scale: $c/\omega_p \sim 1(n_{15})^{-1/2} \text{ cm}$, $c/\omega_B \sim 3\varepsilon(B_6)^{-1} \text{ cm}$
- can accelerate particles to non-thermal energies.

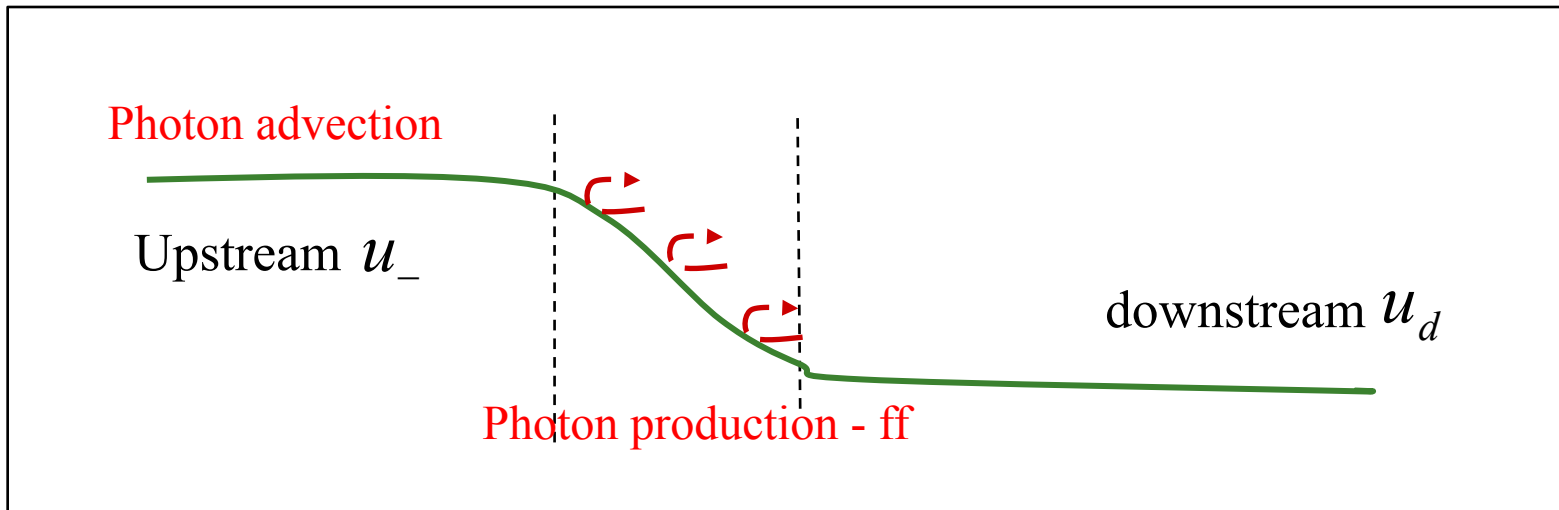
RMS



- scale: $(\sigma_T n \beta_s)^{-1} \sim 10^9 n_{15}^{-1} \text{ cm}$
- microphysics is fully understood
- cannot accelerate particles (important implications for HE neutrino production)

Photon source: two regimes

- **Photon starved shocks:** photon production inside the shock (SNe, LLGRB, NS merger)
- **Photon rich shocks:** photon advection by upstream fluid (GRBs)



Non-relativistic .vs. Relativistic

Non-relativistic RMS

- small energy gain: $\Delta\varepsilon/\varepsilon \ll 1$
- **diffusion approximation holds.**

Zeldovich & Raiser 1967; Weaver 1976; Blandford & Payne 1981;

Relativistic RMS (RRMS)

- **photon distribution is anisotropic**
- energy gain large: $\Delta\varepsilon/\varepsilon > 1$
 - optical depth depends on angle: $\tau \propto (1 - \beta \cos\theta)$
- copious pair production

Levinson & Bromberg 08; Katz et al. 10; Budnik et al. 10; Beloborodov 2017

Self-consistent numerical calculation of RRMS

Photon Rich regime : photons advected from the upstream is dominant

[Levinson & Bromberg \(2008\)](#)

Energy integrated intensity, Klein-Nishina effect, pair production neglected

[Beloborodov \(2017\)](#)

Full radiation transfer, effects of magnetic field considered,
pair production neglected

[Lundman et al. \(2018\)](#)

Full radiation transfer, pair production effect included,
some approximation is given on the temperature calculation

[Ito et al. \(2018\)](#)

Full radiation transfer with pair production, no optimistic approximation
wide range of upstream condition is covered

Photon Starved regime : photons produced in the downstream is dominant

[Budnik et al. \(2010\)](#)

Full radiation transfer with pair production and bremsstrahlung emission
some assumption on cross sections. $6 < \Gamma < 30$

All studies consider Infinite shocks:

Shock Breakout simulation has not been performed

Self-consistent numerical calculation of RRMS

Photon Rich regime : photons advected from the upstream is dominant

[Ito et al. \(2018\)](#) Infinite shock

Full radiation transfer with pair production, no optimistic approximation
wide range of upstream condition is covered

$$2 < \Gamma_u < 10, \quad 0.01 < \xi_u < 10, \quad 10^3 < n < 10^5$$

[Ito et al. in prep I.](#), finite shock (shock breakout)

Simulation with photon escape (shock breakout)

structure, spectra, application to GRBs

Photon Starved regime : photons produced in the downstream is dominant

[Ito et al. in prep II.](#), Infinite shock

Full radiation transfer with pair production,
free-free emission + absorption, no optimistic approximation

Self-consistent numerical calculation of RRMS

Photon Rich regime : photons advected from the upstream is dominant

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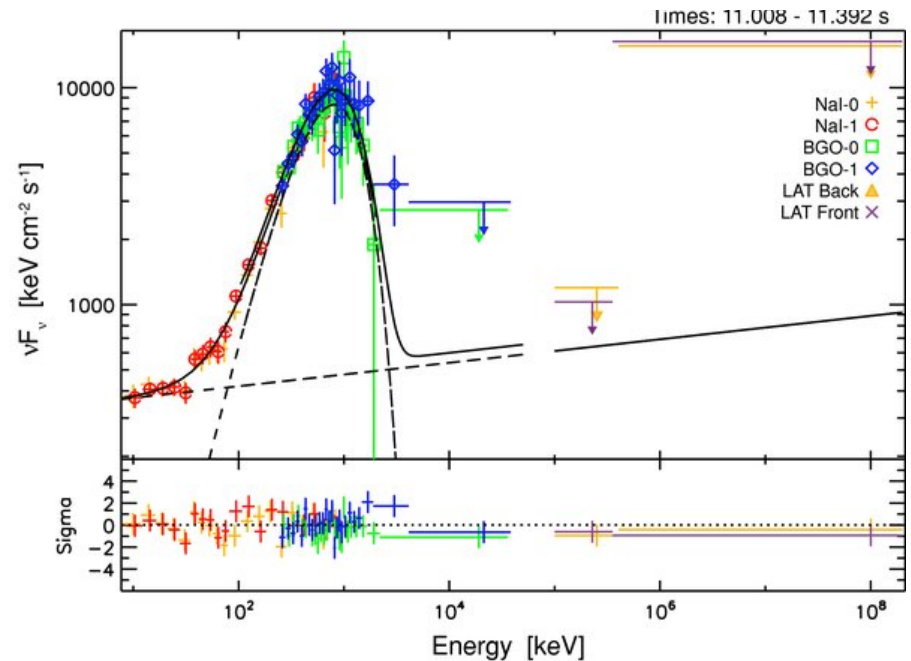
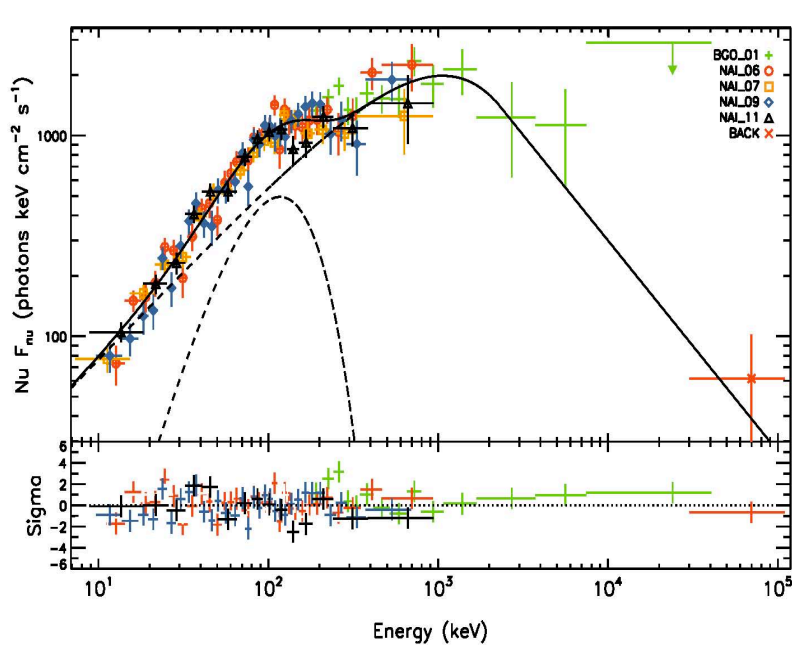
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Full radiation transfer with pair production,
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GRBs: sub-photospheric shocks

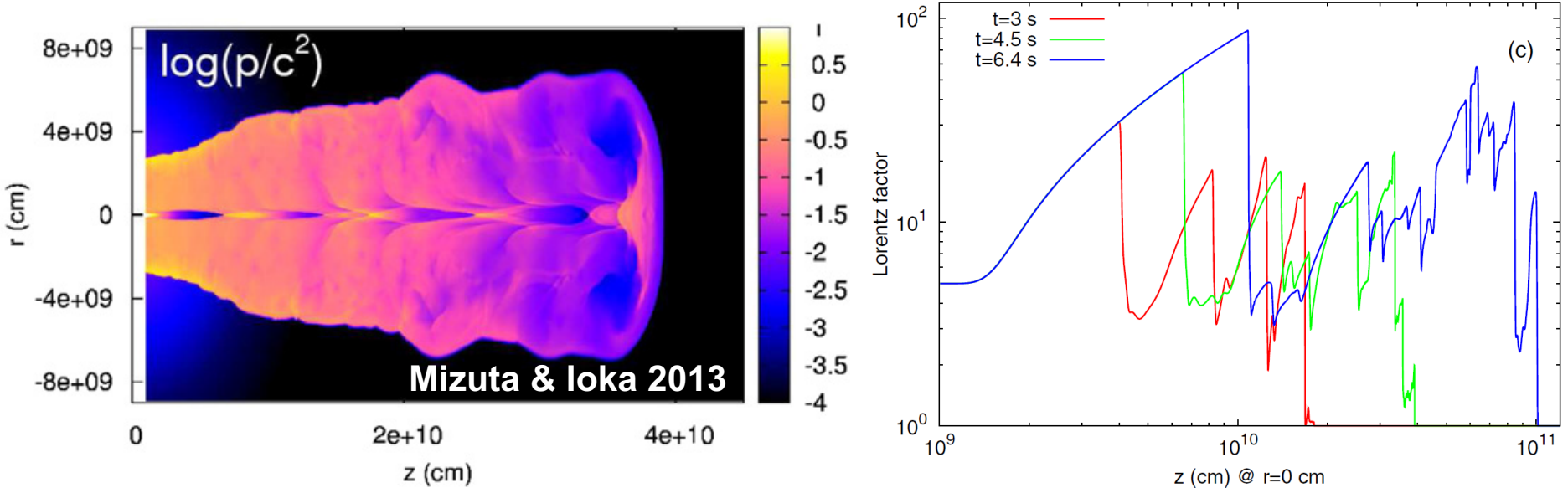
Levinson 12, Levinson & Keren 14, Beloborodov 17, HI+18

Evidence for photospheric emission ? (Peer+Ryde)



Band spectrum from photospheric emission? (Beloborodov 13, Vurm+ 13, Keren+AL 14, HI + 15, Lazzati 16, Parsotan+18)

Application to GRBs



RRMS naturally develops within jet

Condition for RMS to form

- Optically thick ($\tau \gg 1$)
- propagation velocity

$$\beta_s \gg 4 \times 10^{-5} n_{15}^{1/6}$$
$$n = 10^{15} n_{15} \text{ cm}^{-3}$$

Weaver 1976

always satisfied for GRB fireball at
subphotospheric region
(e.g., Bromberg + 2011)

RRMS in GRB fireball

Hot upstream ($n_\gamma/n_p \sim 10^4 - 10^6 \gg 1$)

Thermalization depth

Photon generation: Bremst. + double Compton

$$L_T \sim \beta c \frac{n_{\gamma,eq}}{Q_{\gamma,eff}}$$

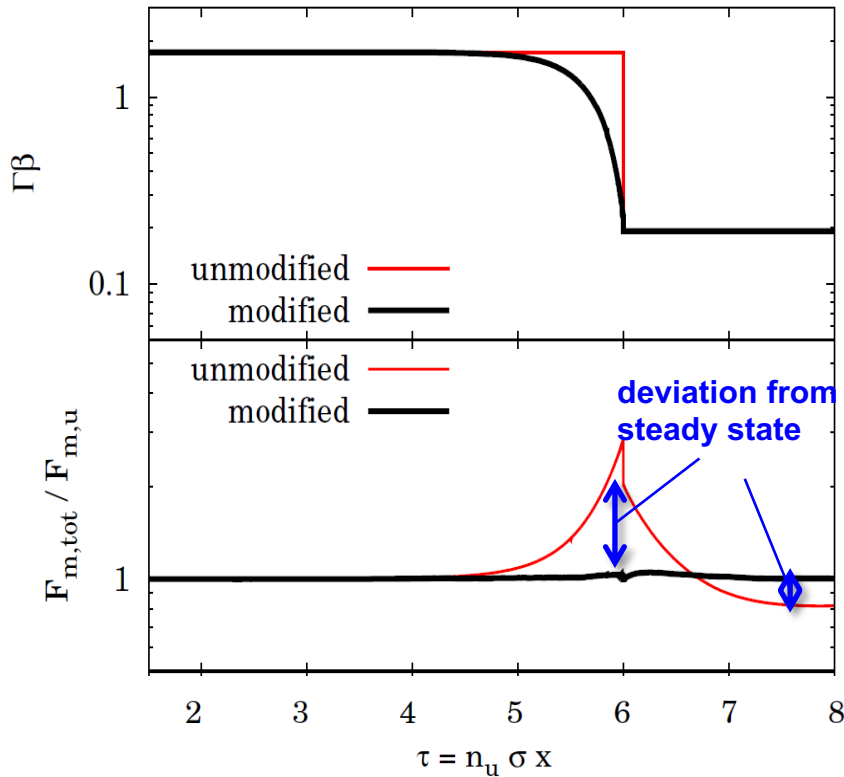
$$\text{Free-free: } \tau'_{ff} = 10^5 \Lambda_{ff}^{-1} (n_{u15})^{-1/8} \gamma_u^{3/4}$$

$$\text{Double Compton: } \tau'_{DC} = 10^6 \Lambda_{DC}^{-1} (n_{u15})^{-1/2} \gamma_u^{-1}$$

Thermalization length \gg shock width ($\tau \sim \text{few}$)

 Photon advection dominant (Photon Rich)
(Photon generation and absorption can be neglected)

Method • Model



Assumption

- advection dominated (emission, absorption neglected, only scattering)
 - large photon to proton ratio ($n_{ph} / n_p = 10^3 - 10^5$)
 - pair production/annihilation included
 - thermal distribution at far up stream
 - electron has Maxwellian distribution
- $\Gamma_u = 2 - 10$

Give plasma profile (n, T, Γ)

↓

Solve radiation transfer using Monte-Carlo Method

↓

Evaluate the deviation from steady profile

Iterate until convergence

feedback

Parameters

Γ_u : Lorentz factor of shock

$\tilde{n} = n_{\text{ph}} / n_p$: photon to baryon number ratio

$\xi_u = 3n_{\text{ph}} k_B T_u / n_p m_p c^2$: photon to baryon inertia ratio

@ far upstream region

Dependences on :

(I) ξ_u

(II) \tilde{n}

(III) Γ_u

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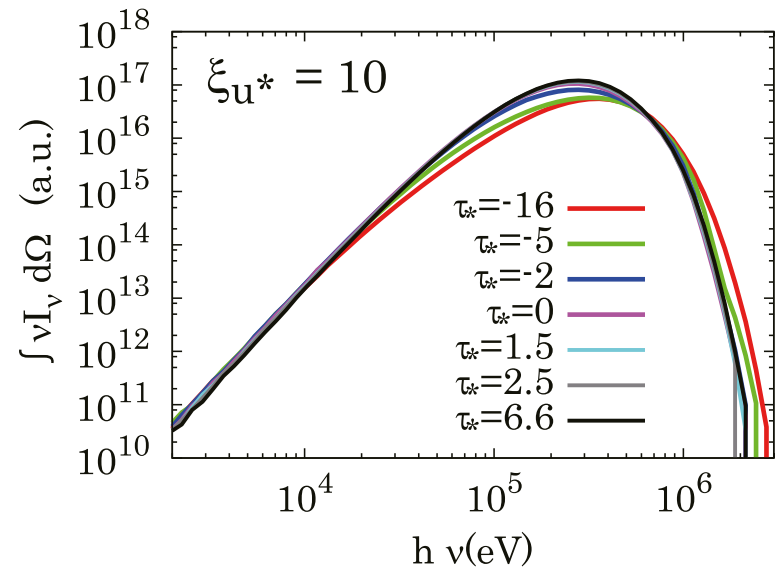
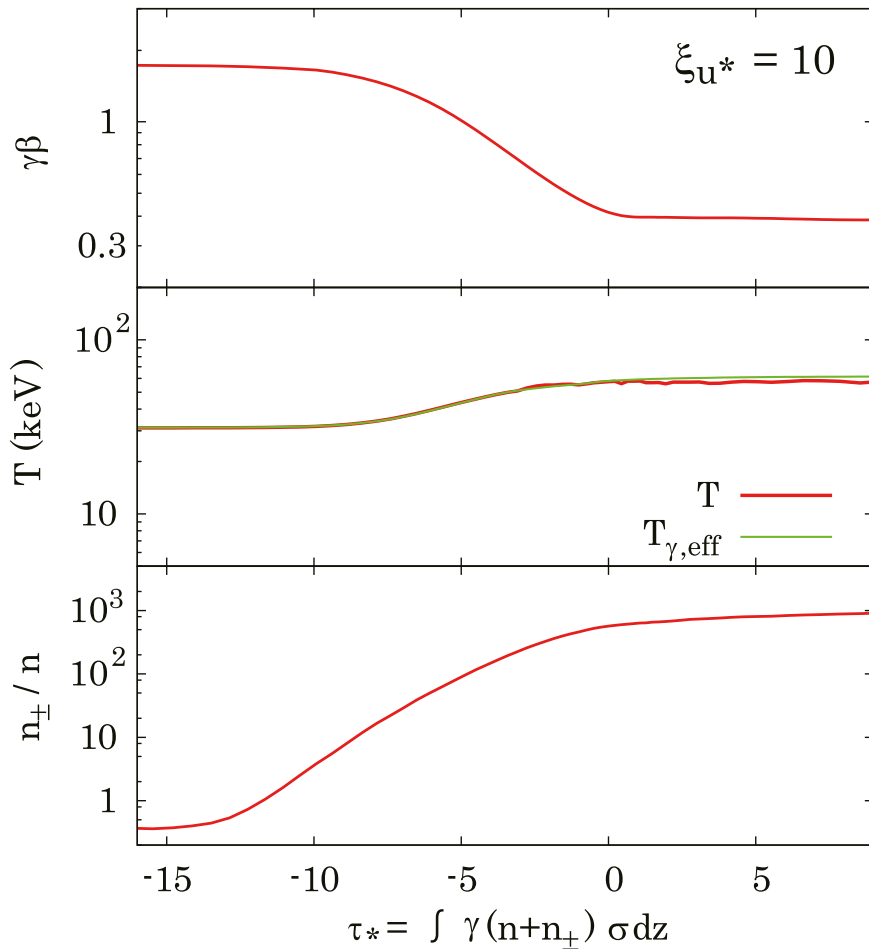
$$\tilde{n} = 10^5 \quad \Gamma_u = 2$$

(II) \tilde{n}

(III) Γ_u

$$\xi_u = 3n_{\text{ph}} k_B T_u / n_p m_p c^2 = 10$$

$$\Gamma_u = 2 \quad \tilde{n} = 10^5$$



Radiation dominant US

"force-free" flow profile

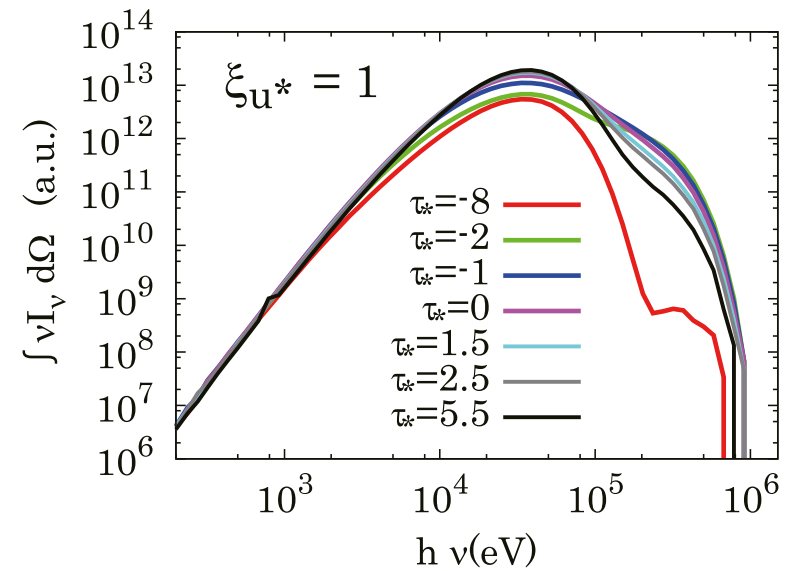
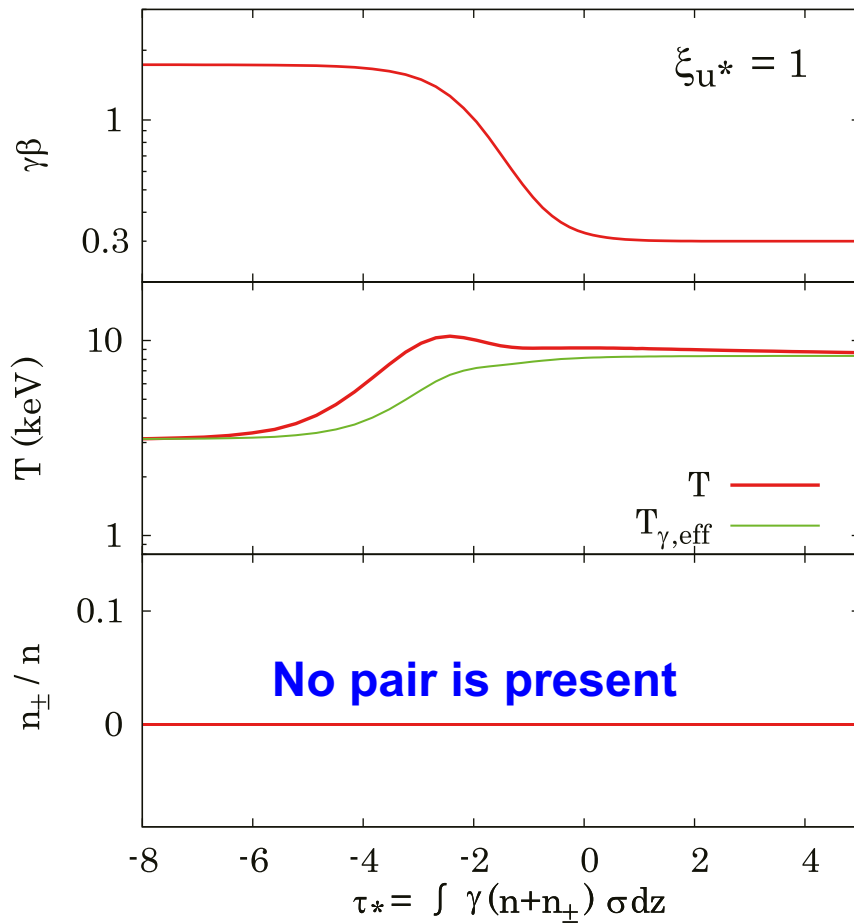
no strong anisotropy appears

Beloborodov 2017

Spectra is mostly thermal

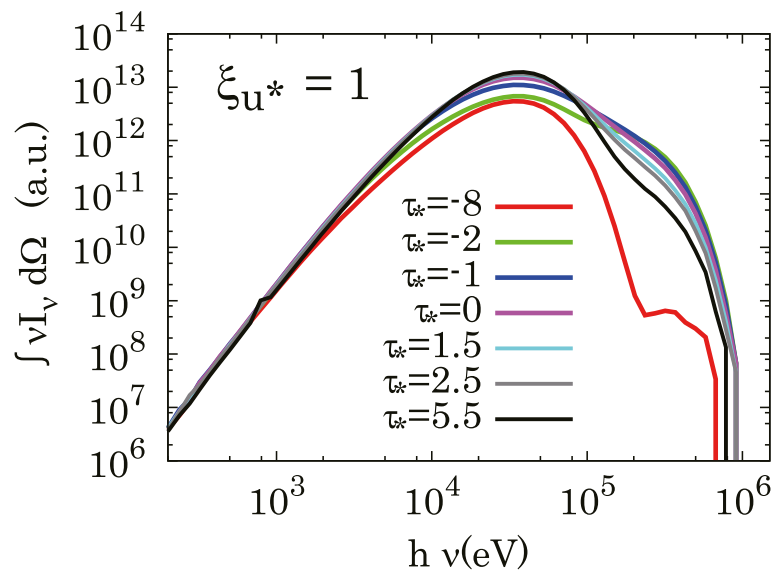
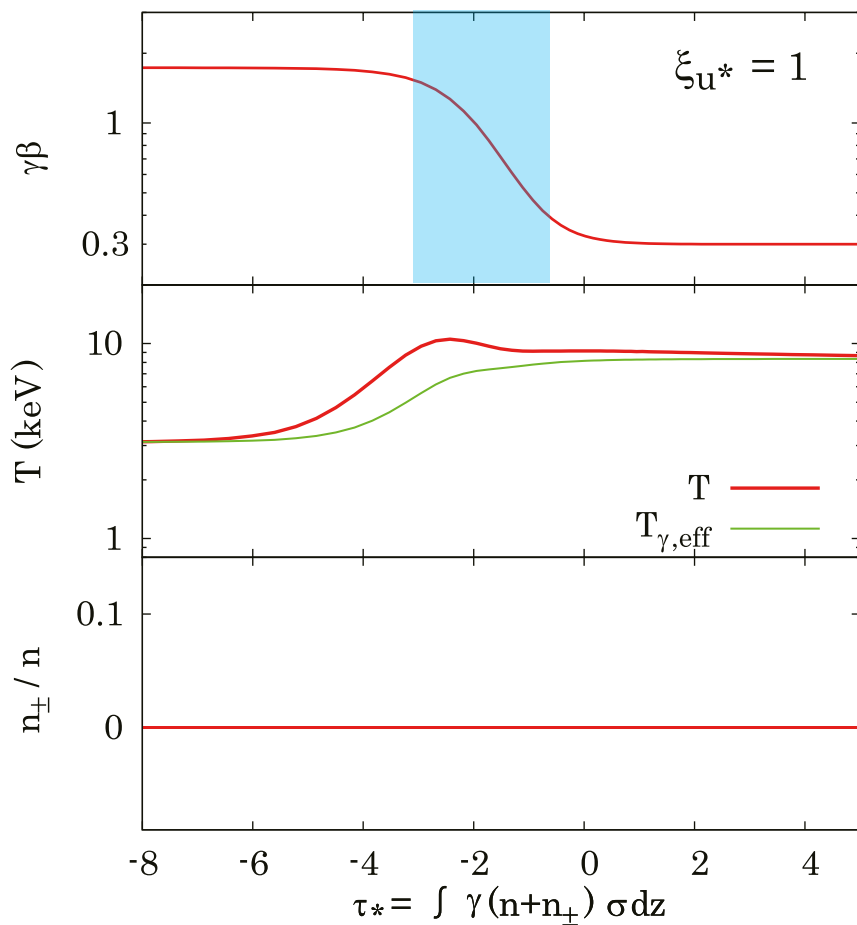
$$\xi_u = 3n_{\text{ph}} k_B T_u / n_p m_p c^2 = 1$$

$$\Gamma_u = 2 \quad \tilde{n} = 10^5$$



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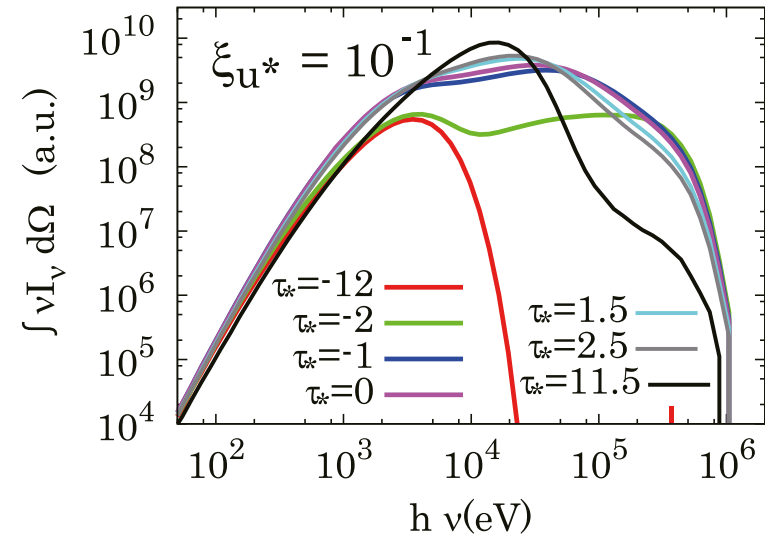
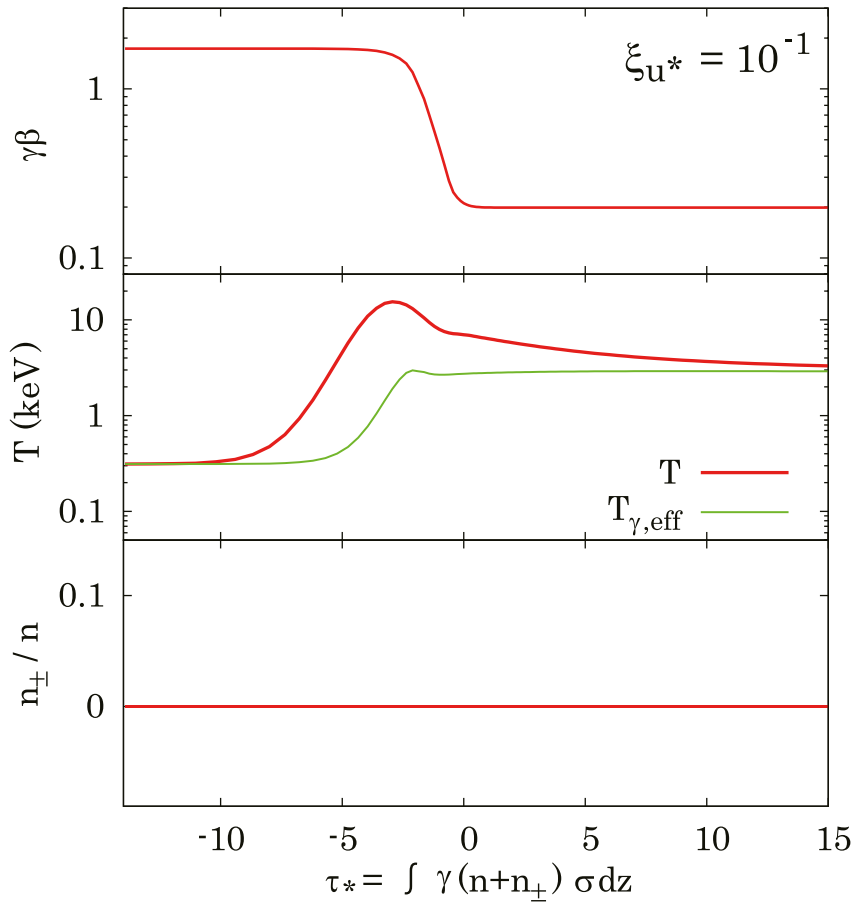


Deceleration in $\Delta\tau \sim 1$

**Anisotropy and
Non-thermal spectra appears**

$$\xi_u = 3n_{\text{ph}} k_B T_u / n_p m_p c^2 = 0.1$$

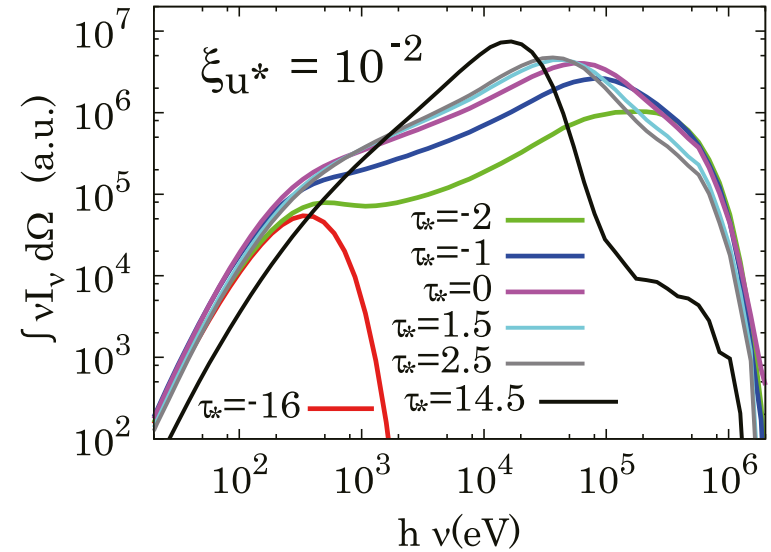
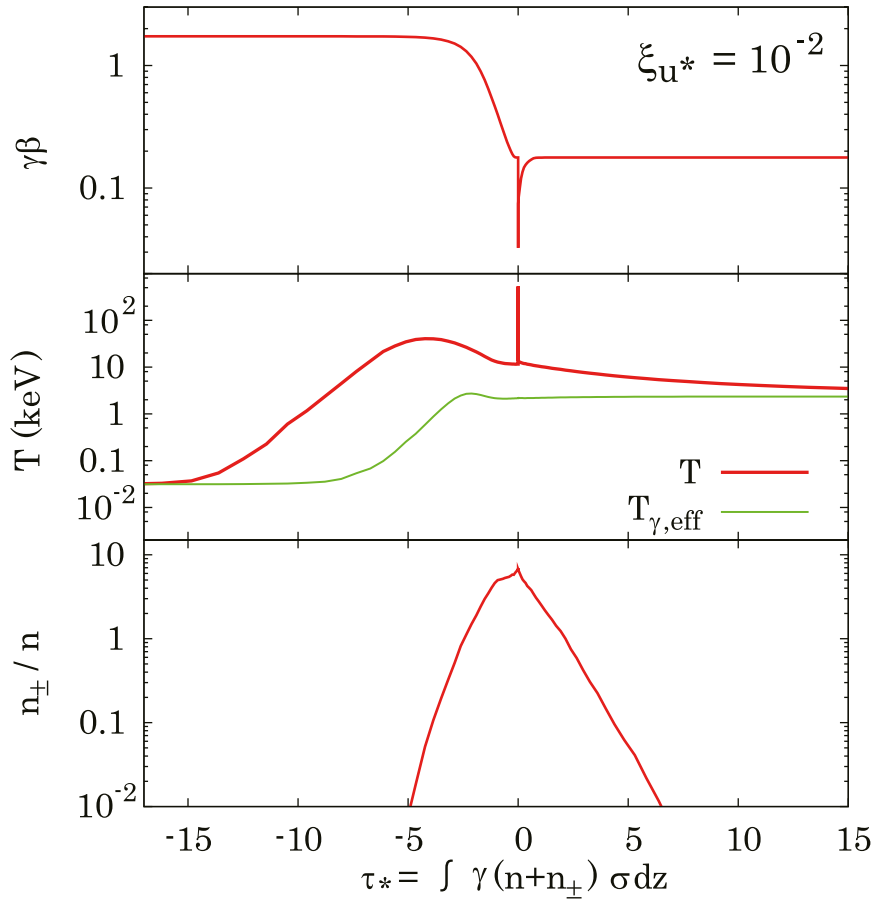
$$\Gamma_u = 2 \quad \tilde{n} = 10^5$$



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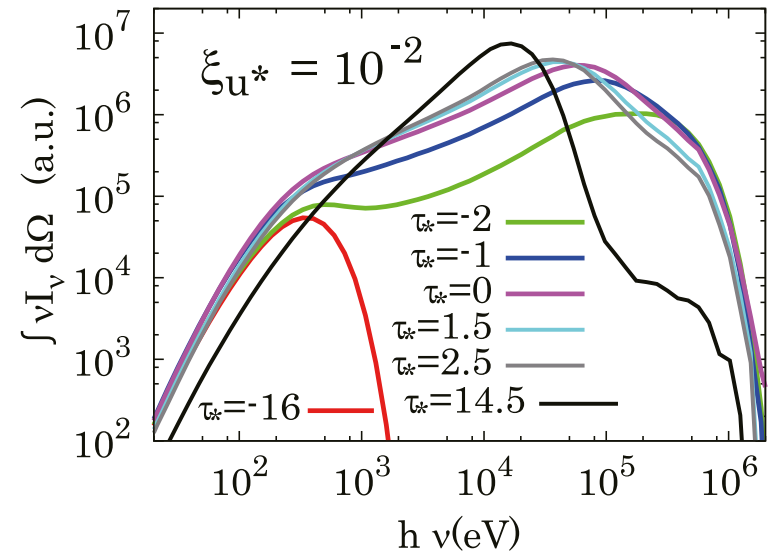
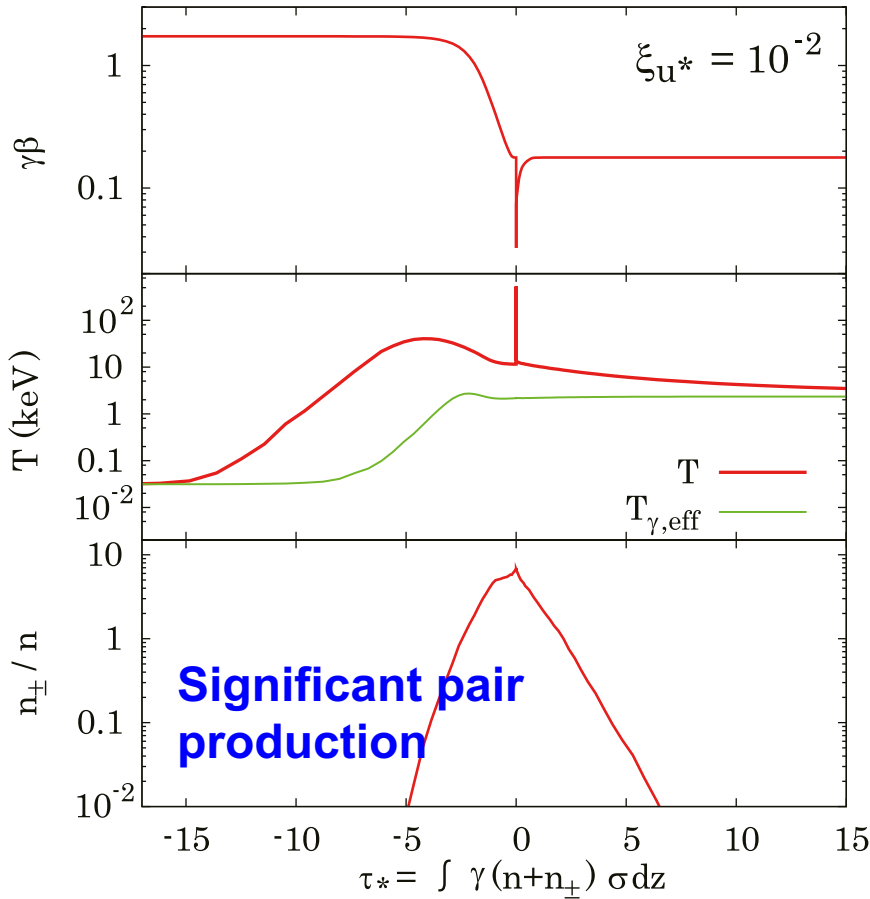
$$\xi_u = 3n_{\text{ph}} k_B T_u / n_p m_p c^2 = 0.01 \quad \Gamma_u = 2 \quad \tilde{n} = 10^5$$



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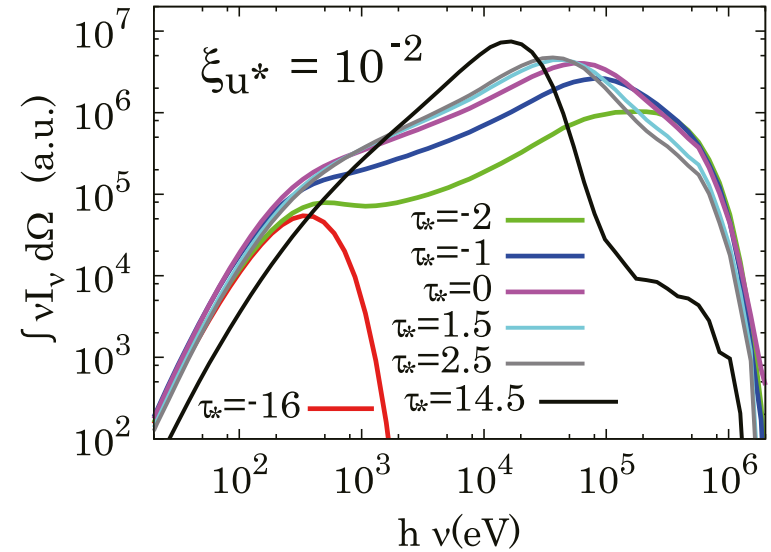
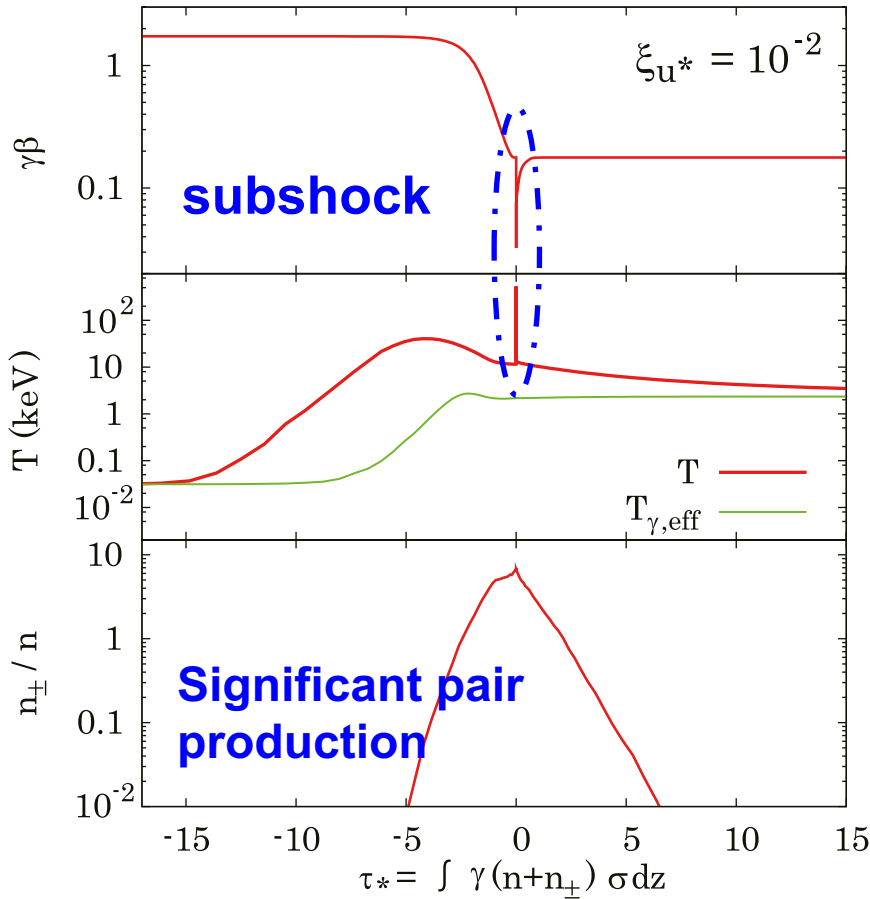
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Deceleration in $\Delta\tau \sim 1$

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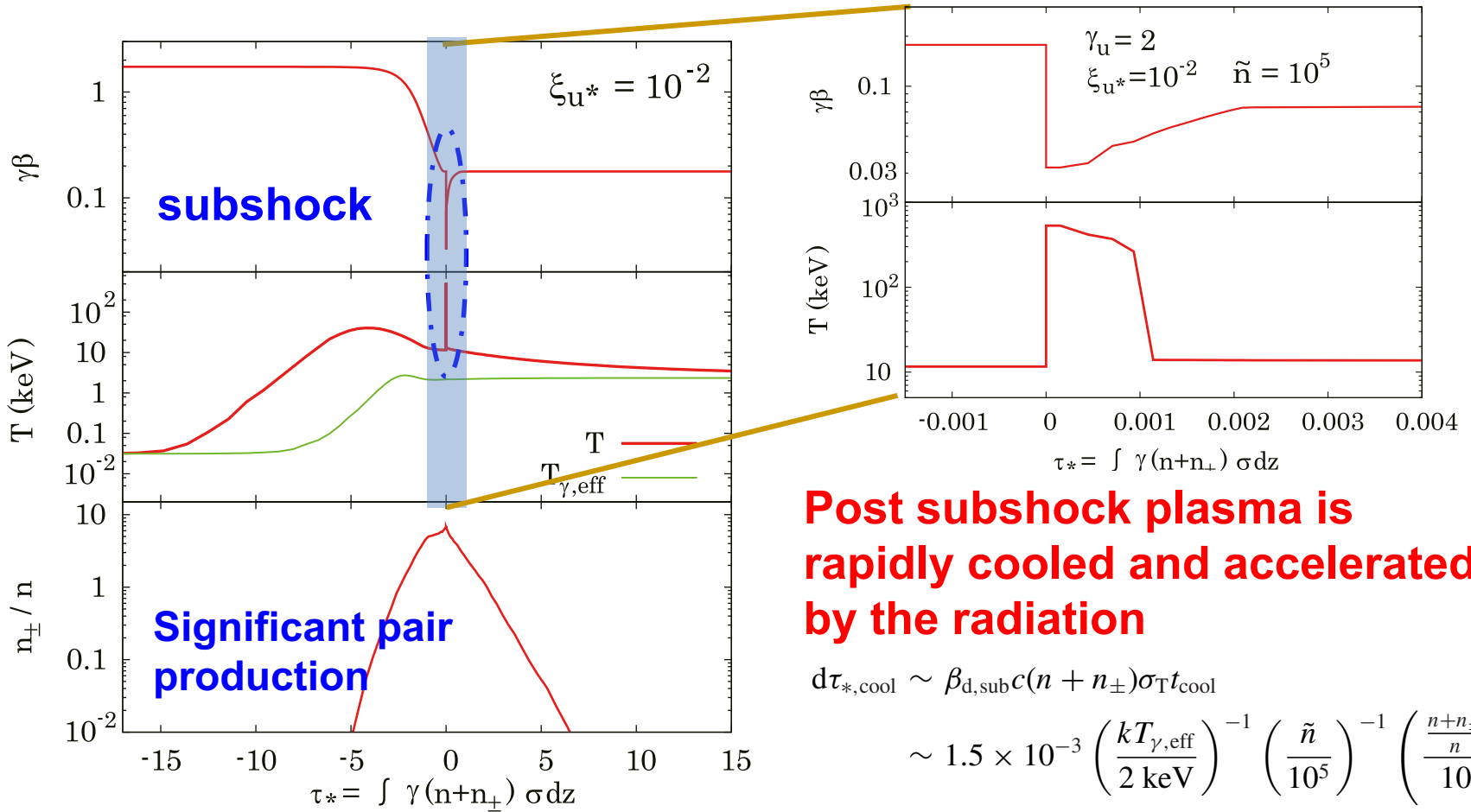
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$$\xi_u = 3n_{\text{ph}} k_B T_u / n_p m_p c^2 = 0.01 \quad \Gamma_u = 2 \quad \tilde{n} = 10^5$$

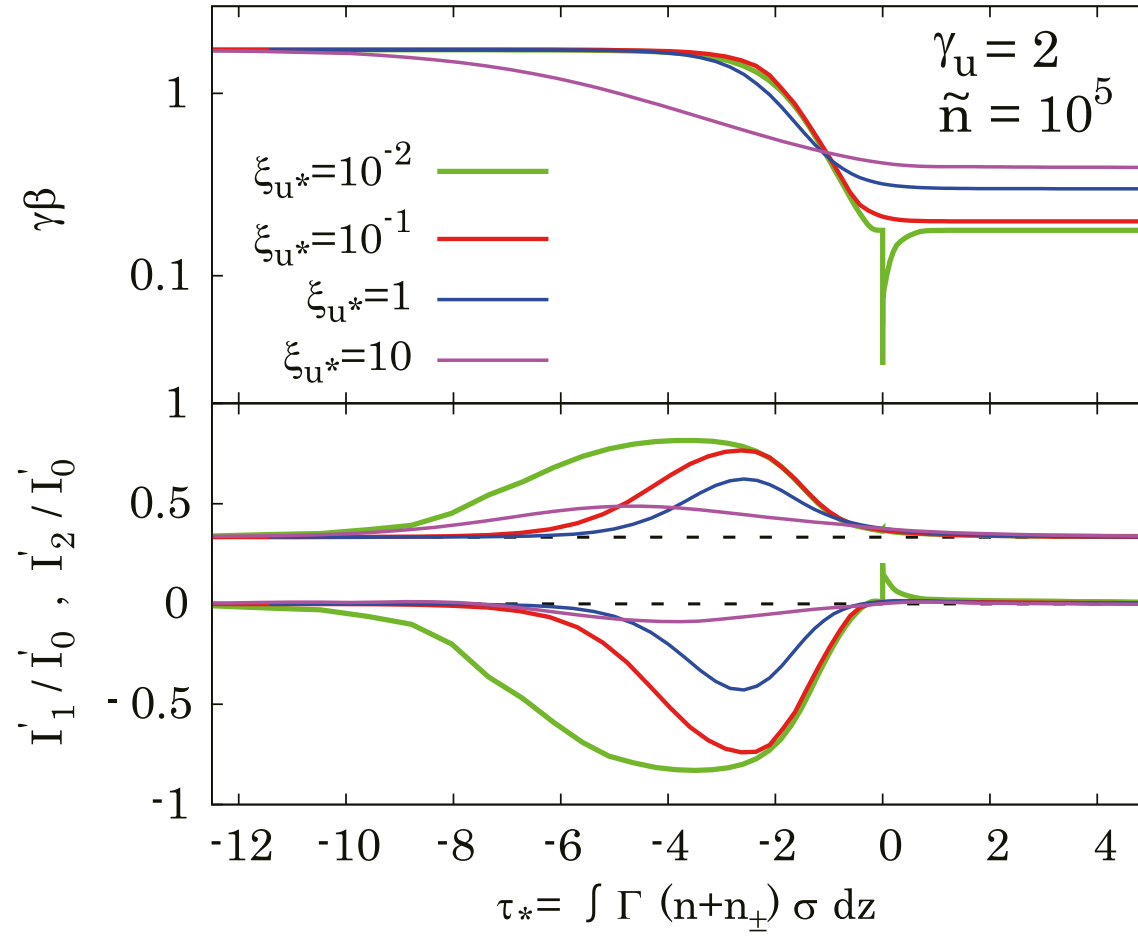


Post subshock plasma is rapidly cooled and accelerated by the radiation

$$\begin{aligned} d\tau_{*, \text{cool}} &\sim \beta_{\text{d,sub}} c (n + n_{\perp}) \sigma T t_{\text{cool}} \\ &\sim 1.5 \times 10^{-3} \left(\frac{kT_{\gamma, \text{eff}}}{2 \text{ keV}} \right)^{-1} \left(\frac{\tilde{n}}{10^5} \right)^{-1} \left(\frac{n+n_{\perp}}{10} \right) \\ &\quad \times \left(\frac{\beta_{\text{u,sub}}}{\beta_{\text{d,sub}}} \right) \left(\frac{\beta_{\text{d,sub}}}{0.03} \right). \end{aligned}$$

* negligible fraction of energy is dissipated in the weak subshock

Dependence on ξ_u



Parameters

Γ_u : Lorentz factor of shock

$\tilde{n} = n_{\text{ph}} / n_p$: photon to baryon number ratio

$\xi_u = 3n_{\text{ph}} k_B T_u / n_p m_p c^2$: photon to baryon inertia ratio

@ far upstream region

Dependences on :

(I) ξ_u

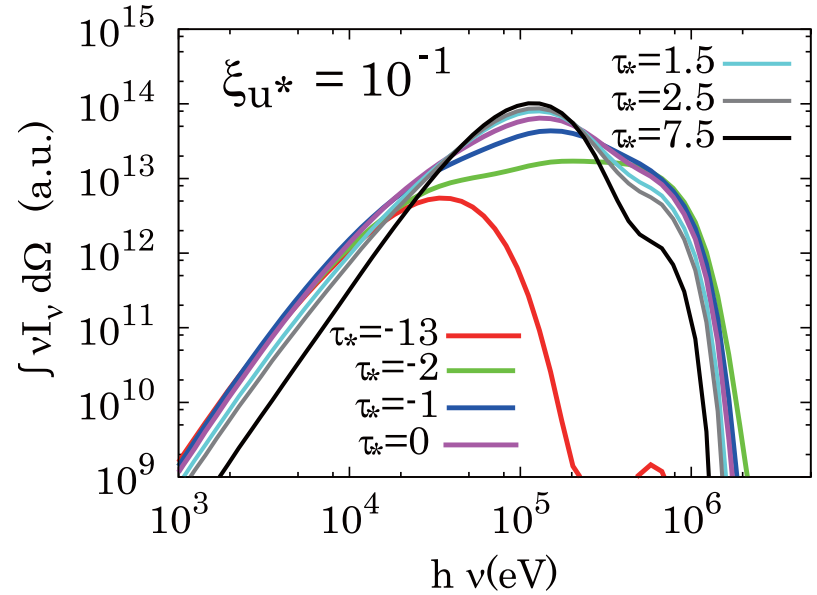
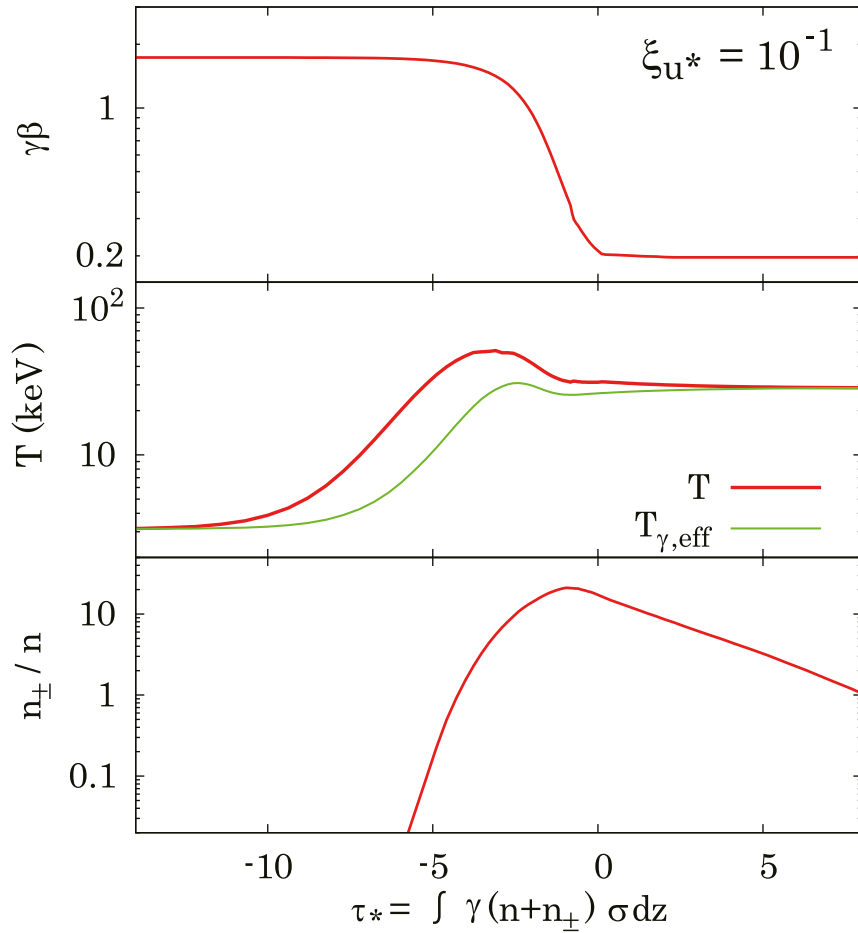
(II) \tilde{n}

$$\xi_u = 0.1 \quad \Gamma_u = 2$$

(III) Γ_u

$$\tilde{n} = n_{\text{ph}} / n_p = 10^4$$

$$\xi_u = 0.1 \quad \Gamma_u = 2$$

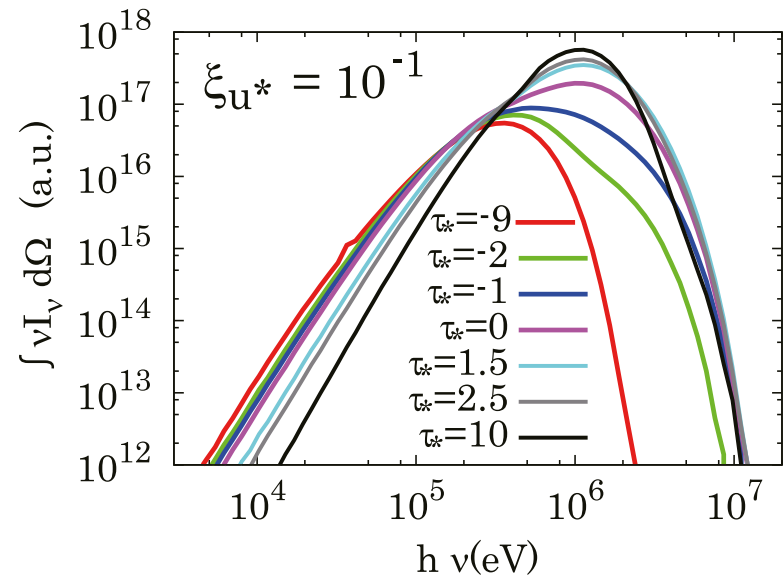
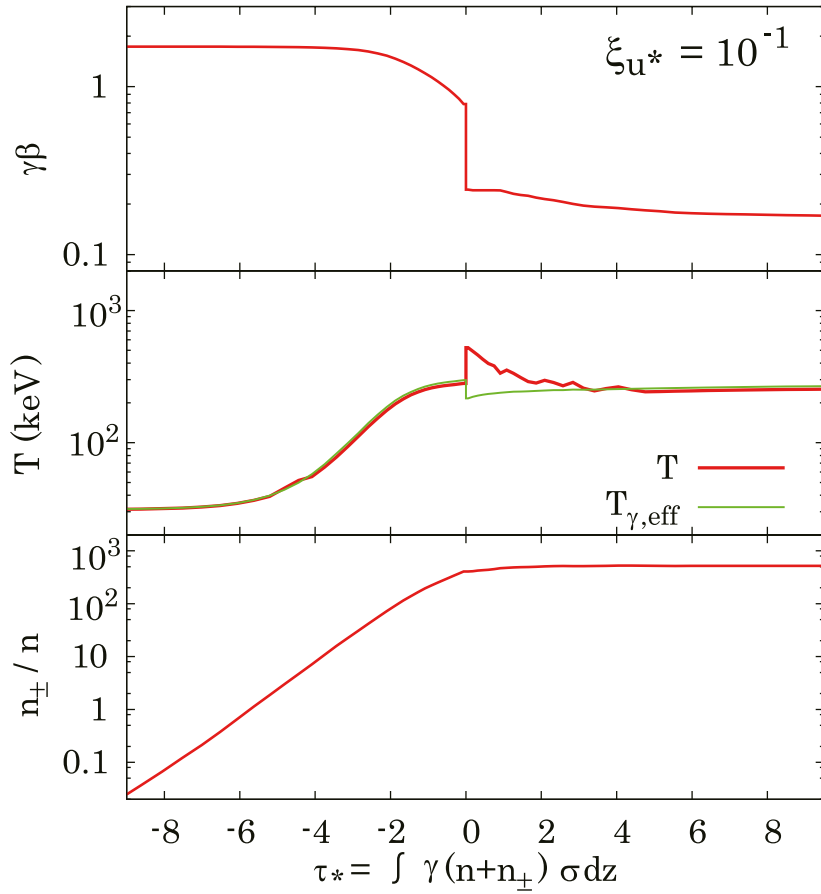


$$T_d \sim 30 (\Gamma_u / 2) (\tilde{n} / 10^4)^{-1} \text{ keV}$$

Pair enrichment is enhanced due to high temperature

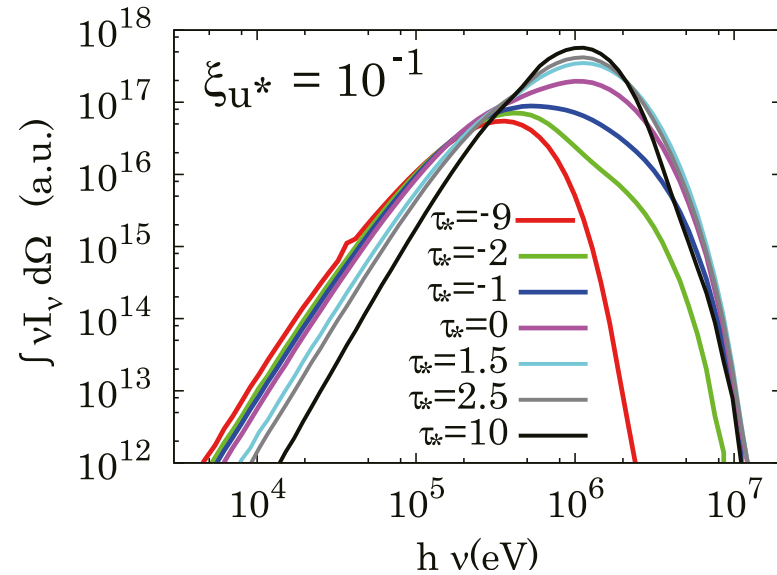
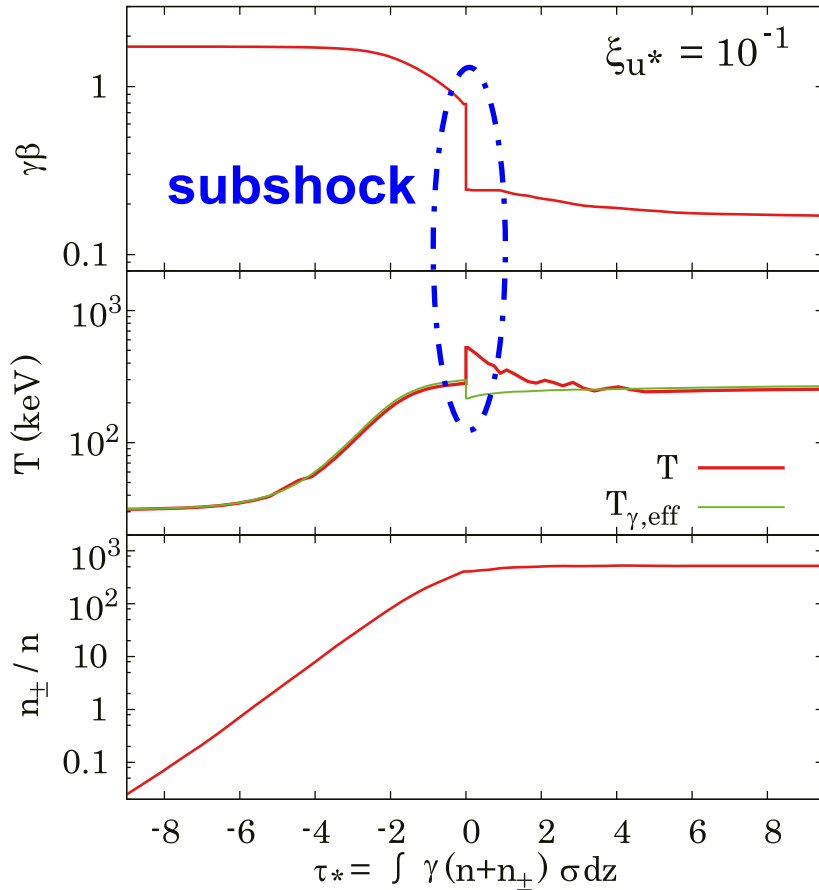
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Strong subshock plasma is appears
for $n_{\text{ph}} / n_p < m_p / m_e$

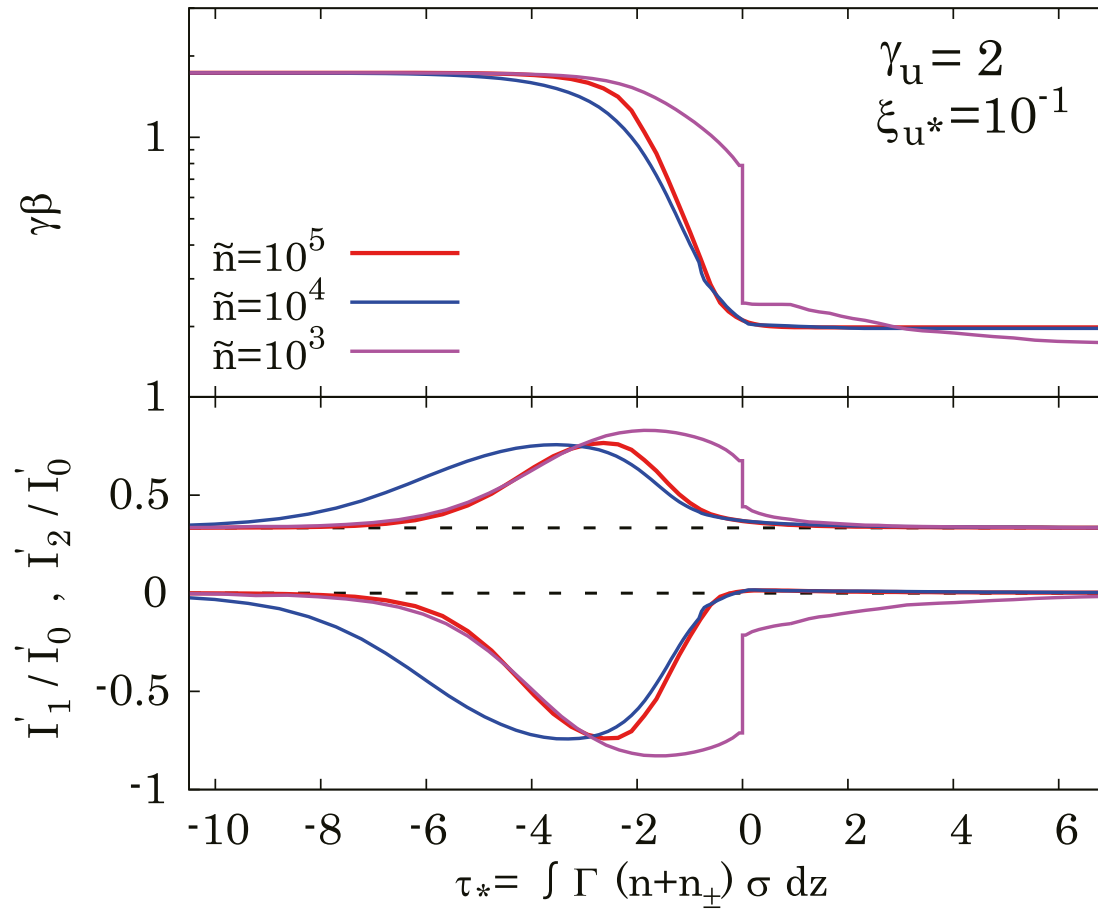
$$E_{\text{ph,max}} = \Gamma_u m_e c^2$$

**➡ Necessary condition for conversion
 from kinetic energy to radiation**

$$\Gamma_u n_p m_p c^2 < n_{\text{ph}} \Gamma_u m_e c^2$$

* Reasonable range of parameter, photon generation cannot be neglected
 => subshock may disappear or be significantly weaker

Dependence on \tilde{n}



Parameters

Γ_u : Lorentz factor of shock

$\tilde{n} = n_{\text{ph}} / n_p$: photon to baryon number ratio

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@ far upstream region

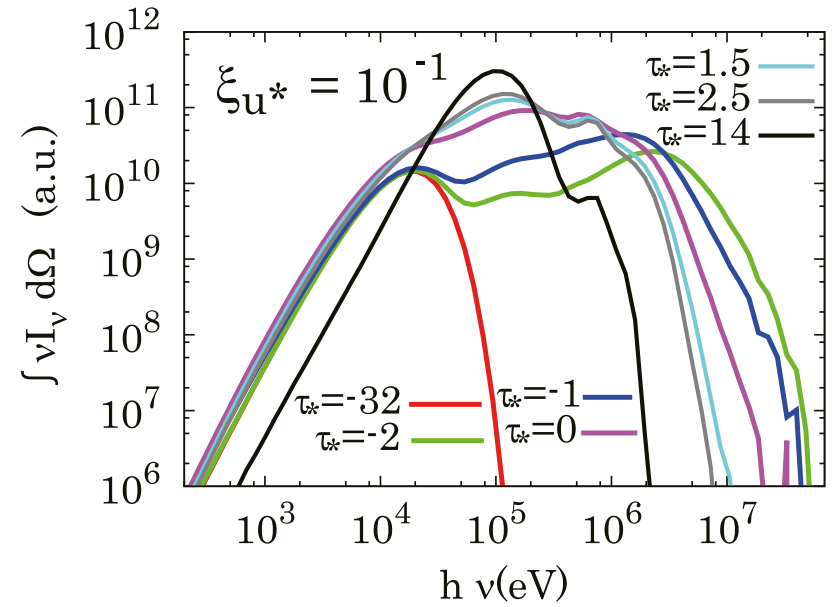
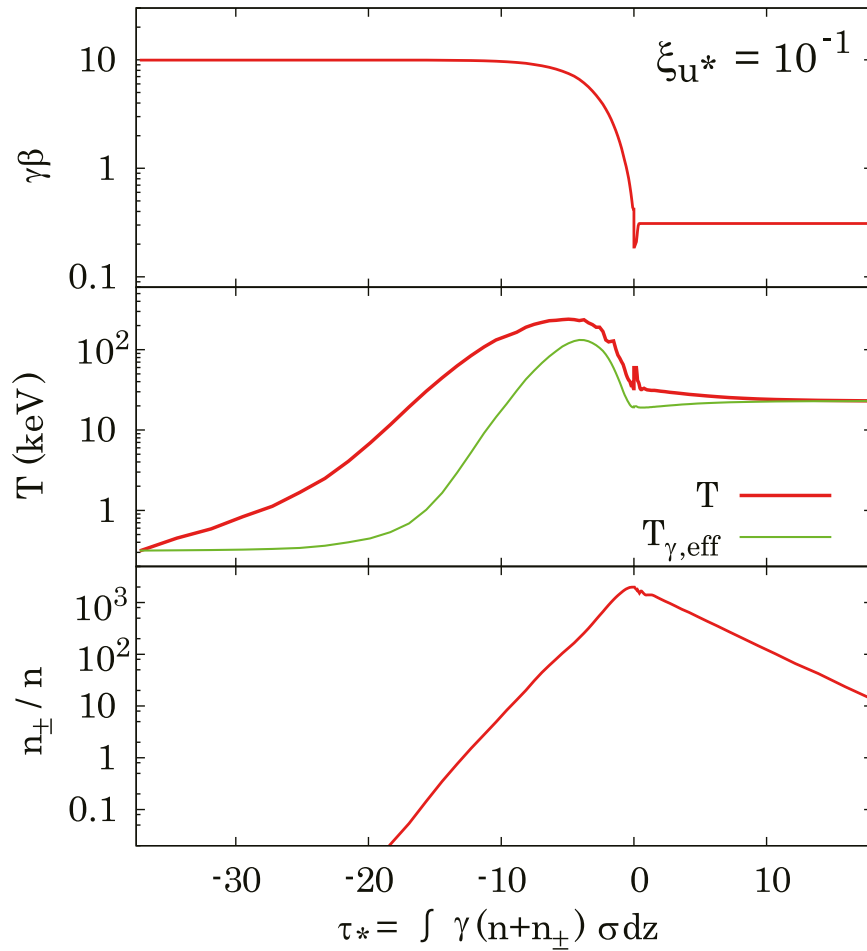
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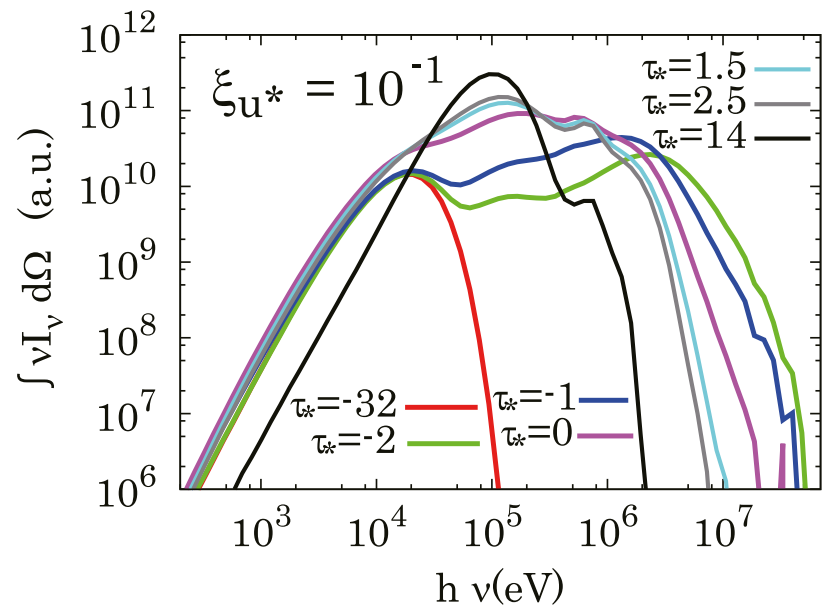
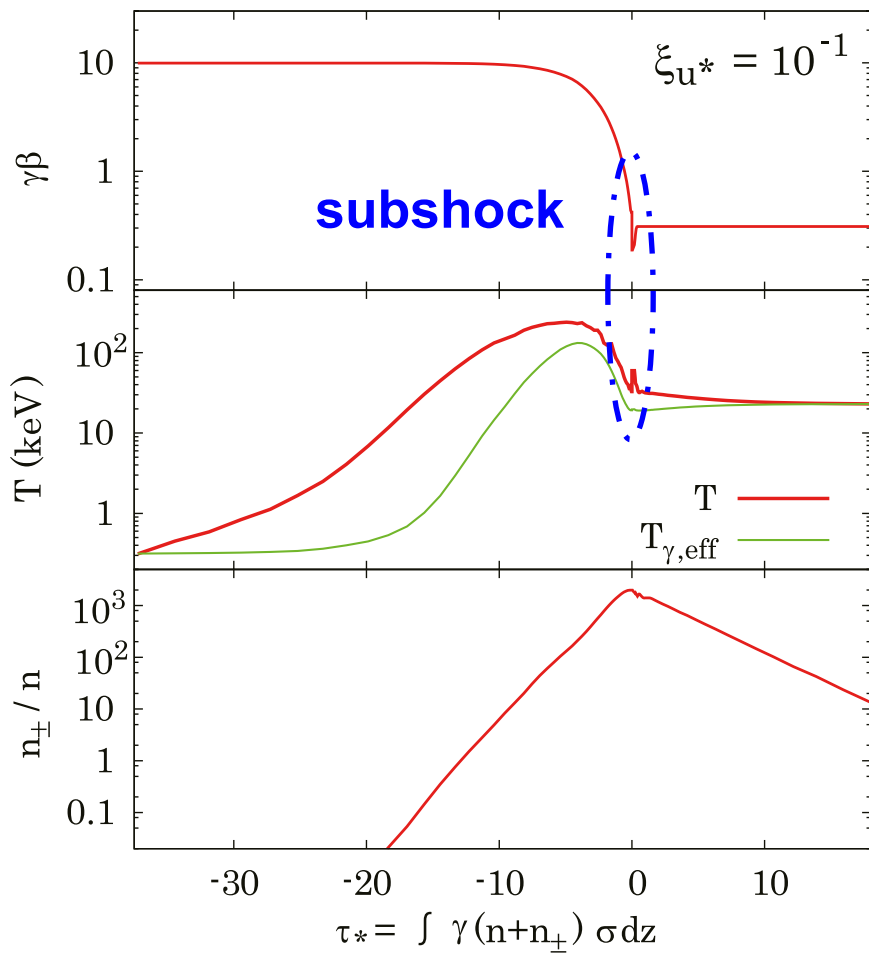
(I) ξ_u

(II) \tilde{n}

(III) Γ_u

$$\xi_u = 0.1 \quad \tilde{n} = 10^5$$

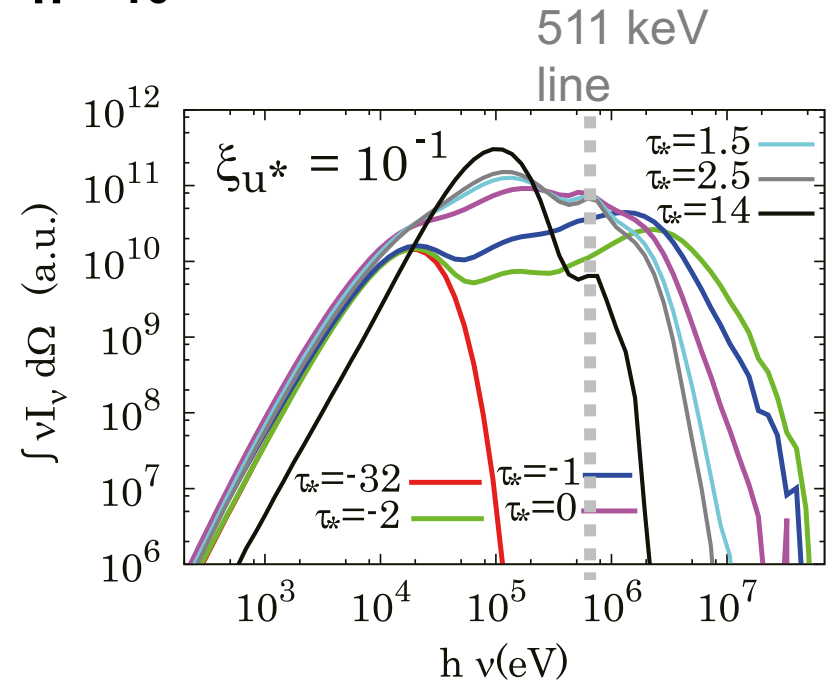
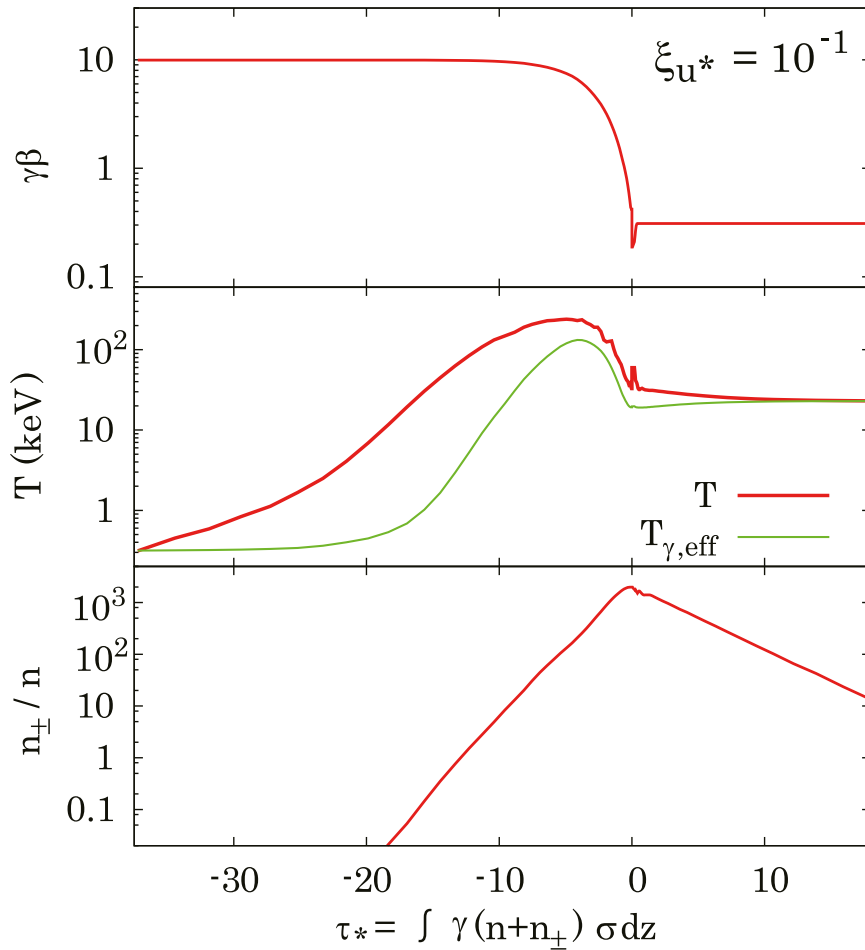
$\Gamma_u = 10$ $\xi_u = 0.1$ $n = 10^5$ 

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$$\Gamma_u = 10$$

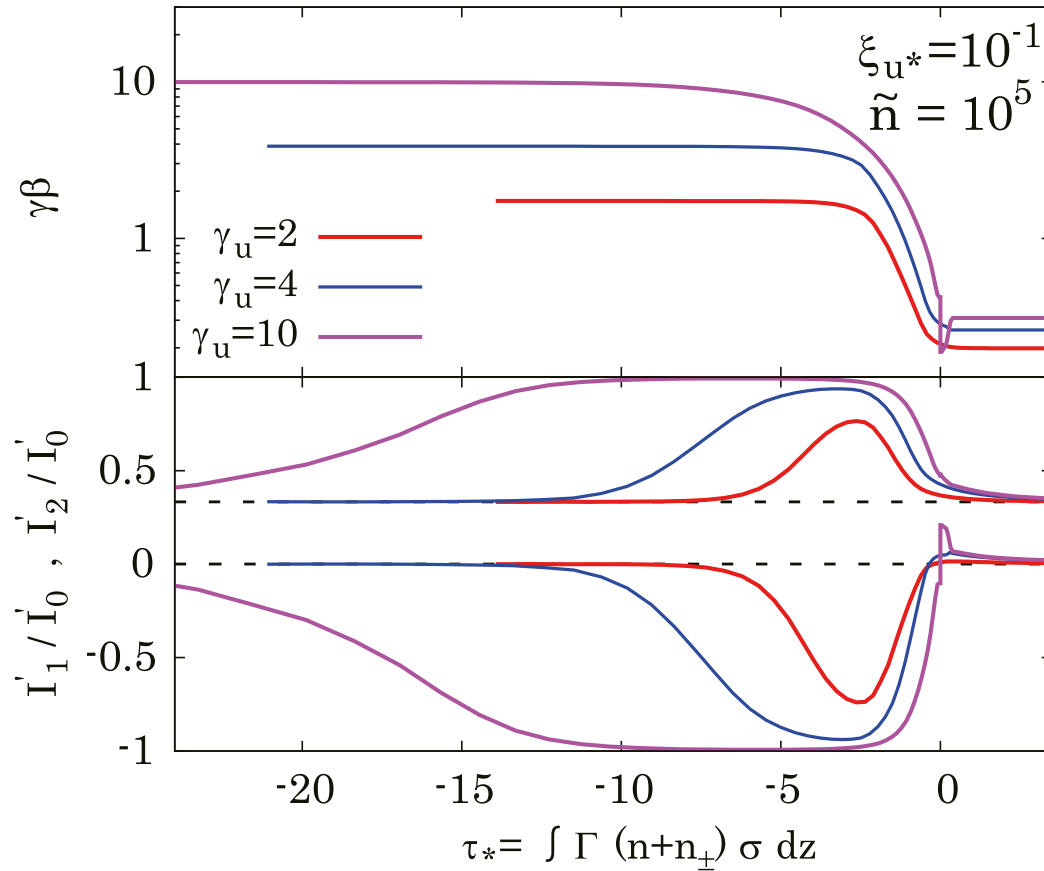
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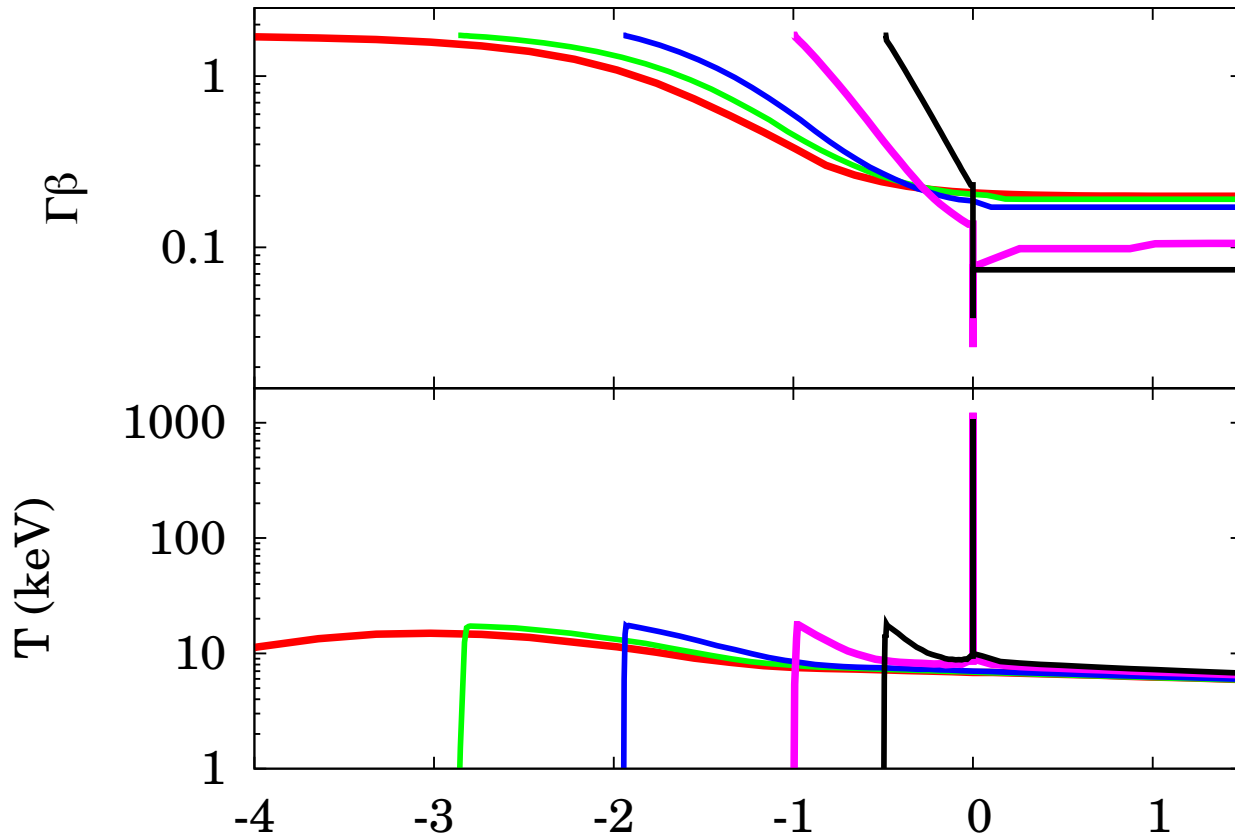
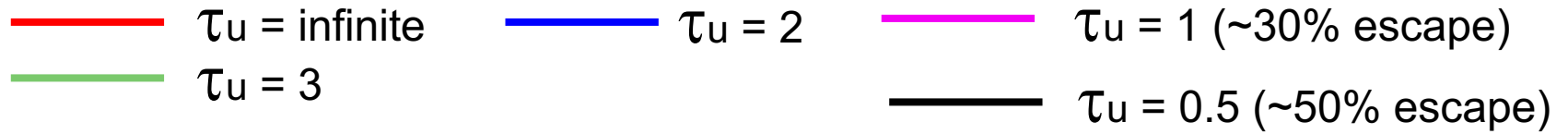


Pair enrichment is enhanced due to strong bulk Comptonization

Dependence on Γ_u



Simulation with escape



As Escape fraction increases

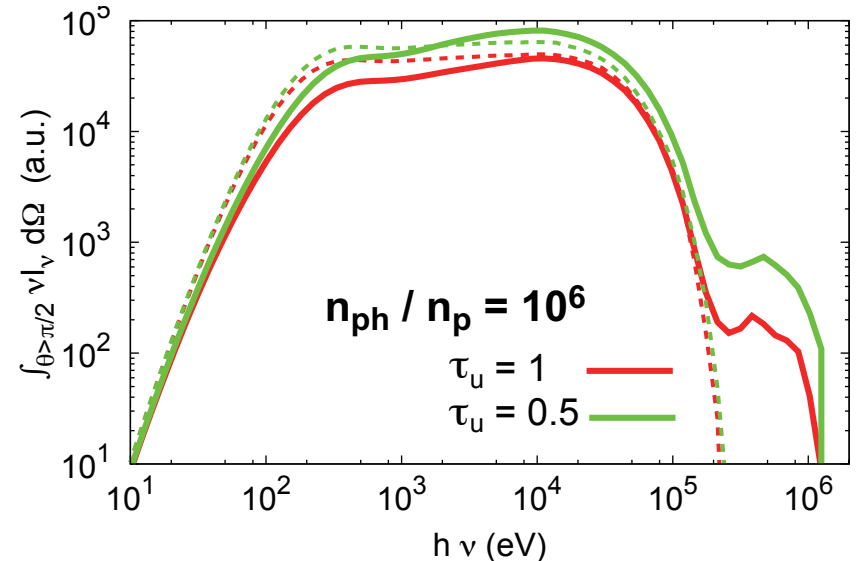
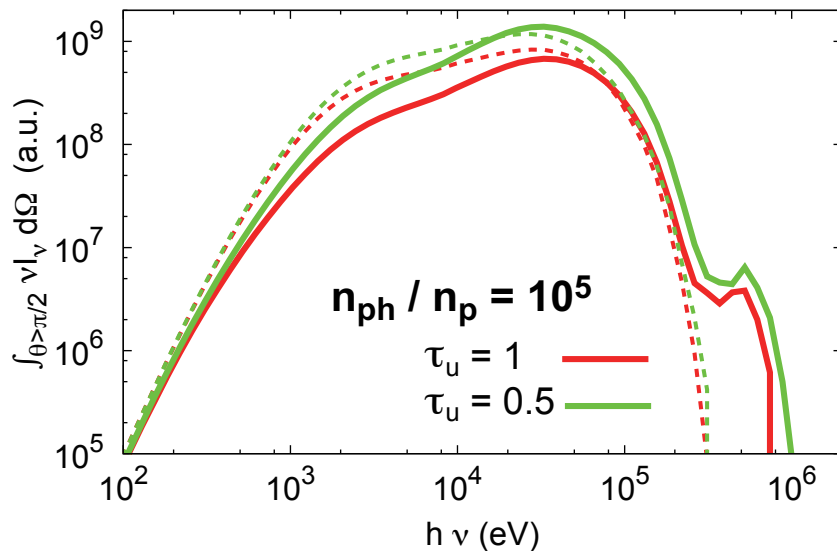
Compression ratio increases

Subshock appears

Escaped Spectrum

— $\tau_u = 1$ (~30% escape)
— $\tau_u = 0.5$ (~50% escape)

- - - Infinite shock @ $\tau = 1$
- - - Infinite shock @ $\tau = 0.5$



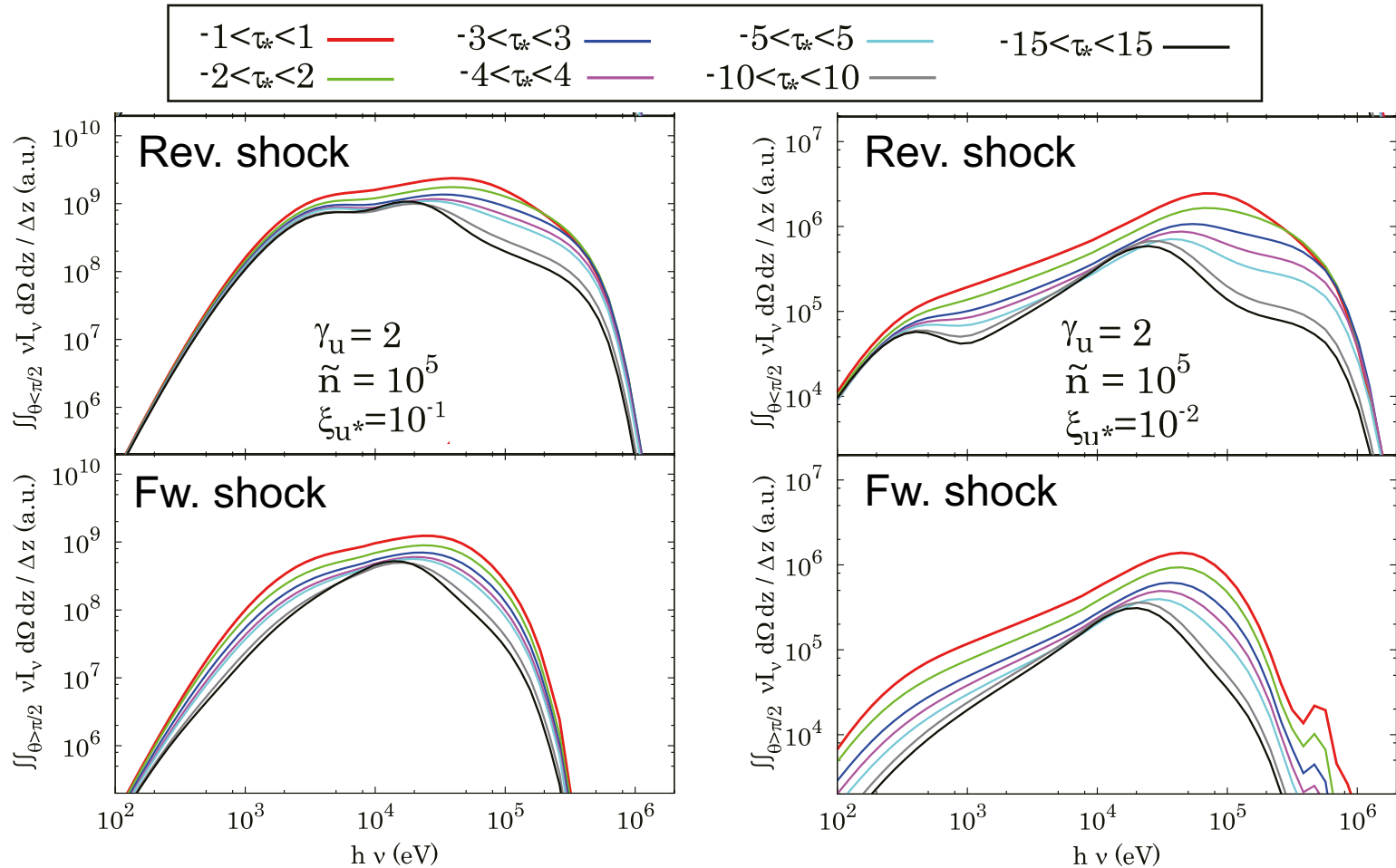
Broad non-thermal spectrum appears

Small difference from the infinite shock at same position



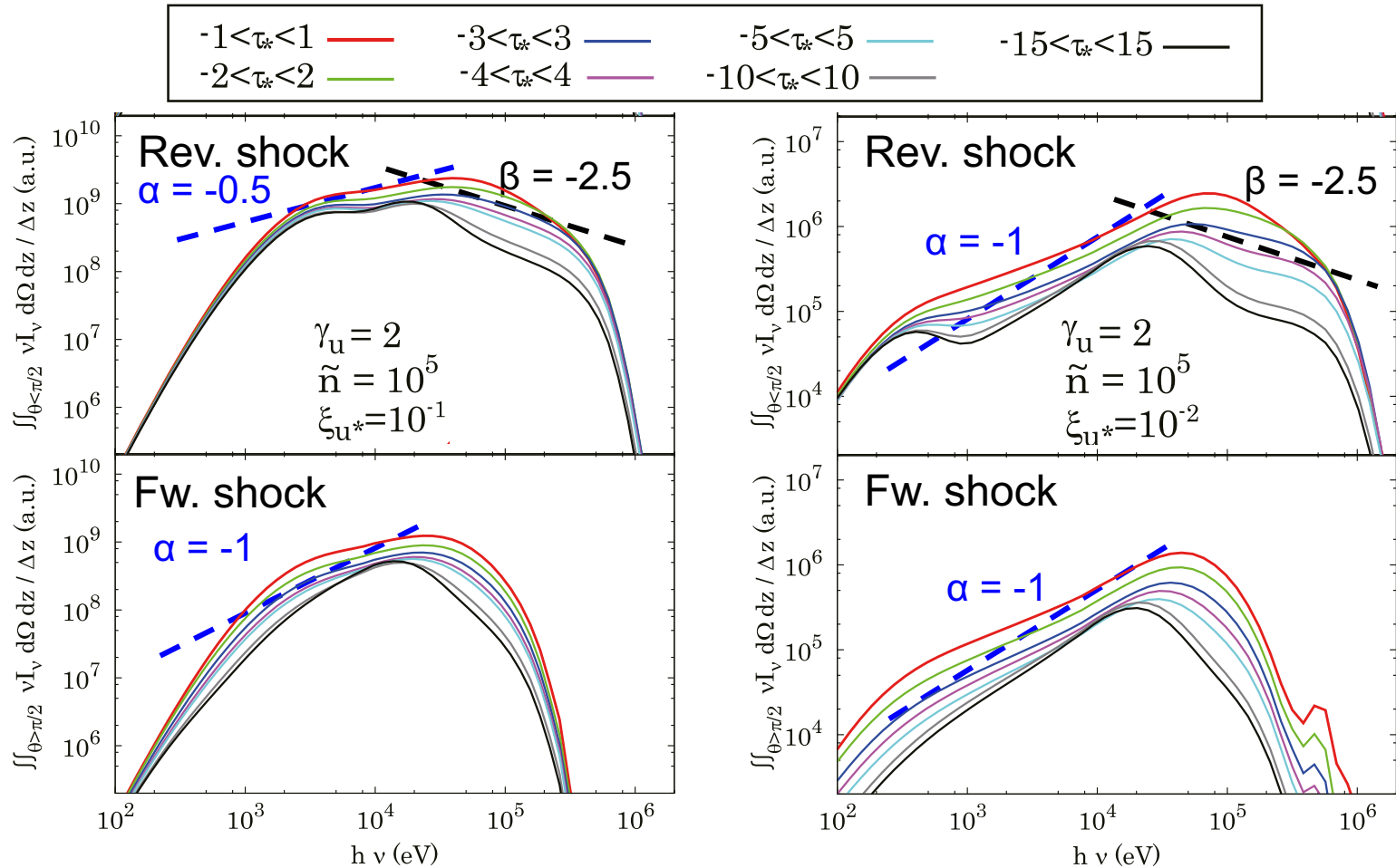
Infinite shock is a good approximation for the breakout emission

Spacially averaged spectra



Highly non-thermal spectra appears near the shock

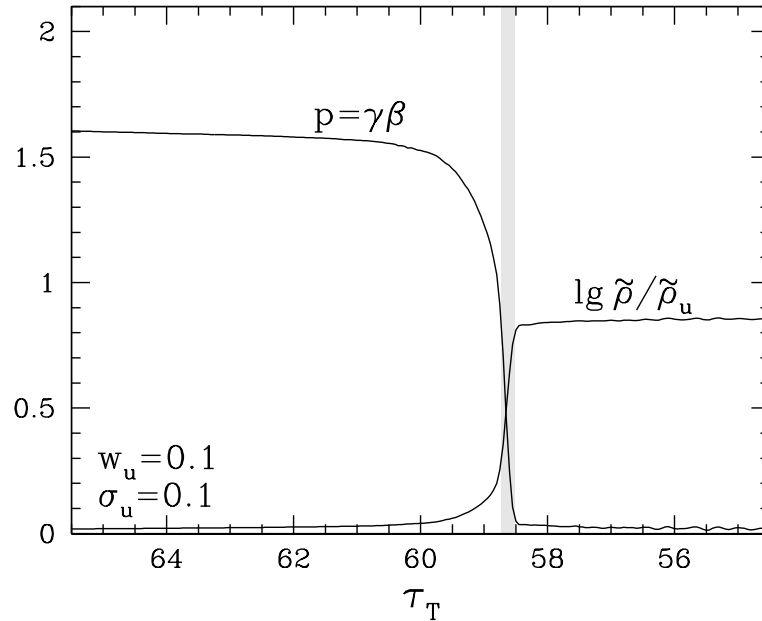
Spacially averaged spectra



Highly non-thermal spectra appears near the shock
 Possible origin of Band spectrum

Effects of magnetic field

Beloborodov 2017

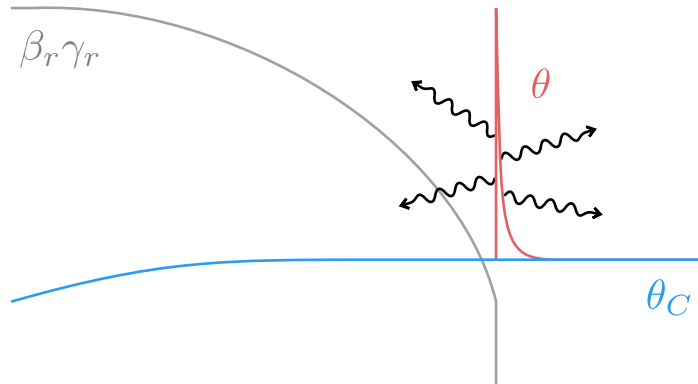


Certain fraction of DS energy is contained in compressed B-field



Subshock is formed

Lundman et al. 2018



Synchrotron emission at subshock can be an important source of photons

Self-consistent numerical calculation of RRMS

Photon Rich regime : photons advected from the upstream is dominant

Ito et al. (2018) Infinite shock

Full radiation transfer with pair production, no optimistic approximation
wide range of upstream condition is covered

$$2 < \Gamma_u < 10, \quad 0.01 < \xi_u < 10, \quad 10^3 < n < 10^5$$

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Simulation with photon escape (shock breakout)

structure, spectra, application to GRBs

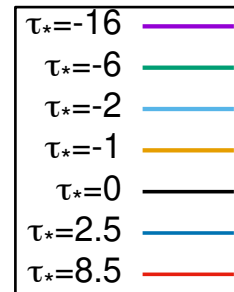
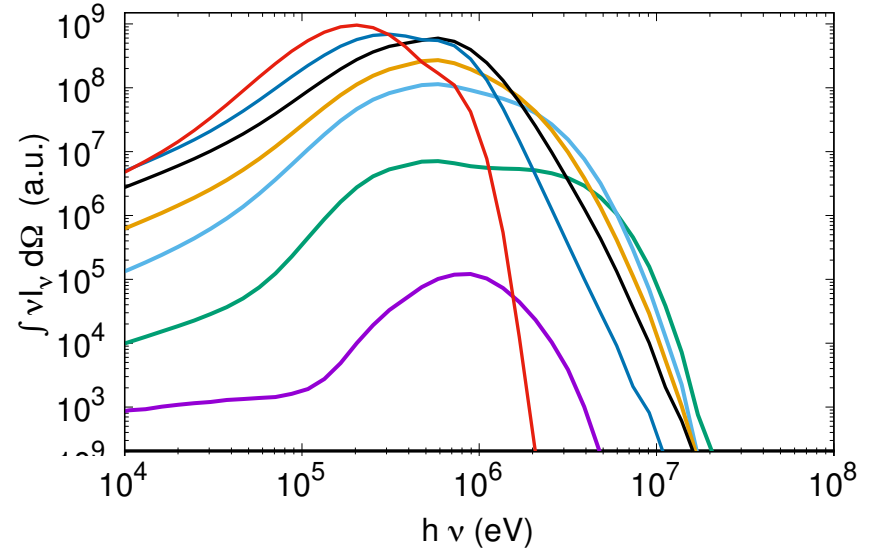
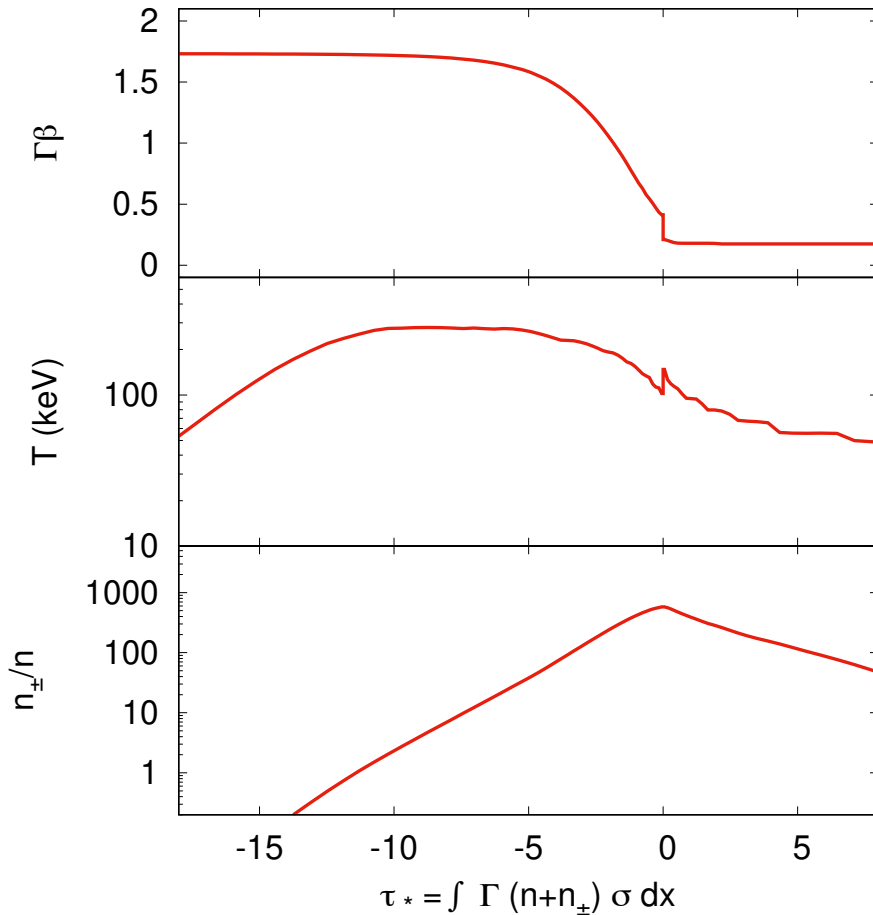
Photon Starved regime : photons produced in the downstream is dominant

Ito et al. in prep II ., Infinite shock

Full radiation transfer with pair production,
free-free emission + absorption, no optimistic approximation

Photon Starved regime

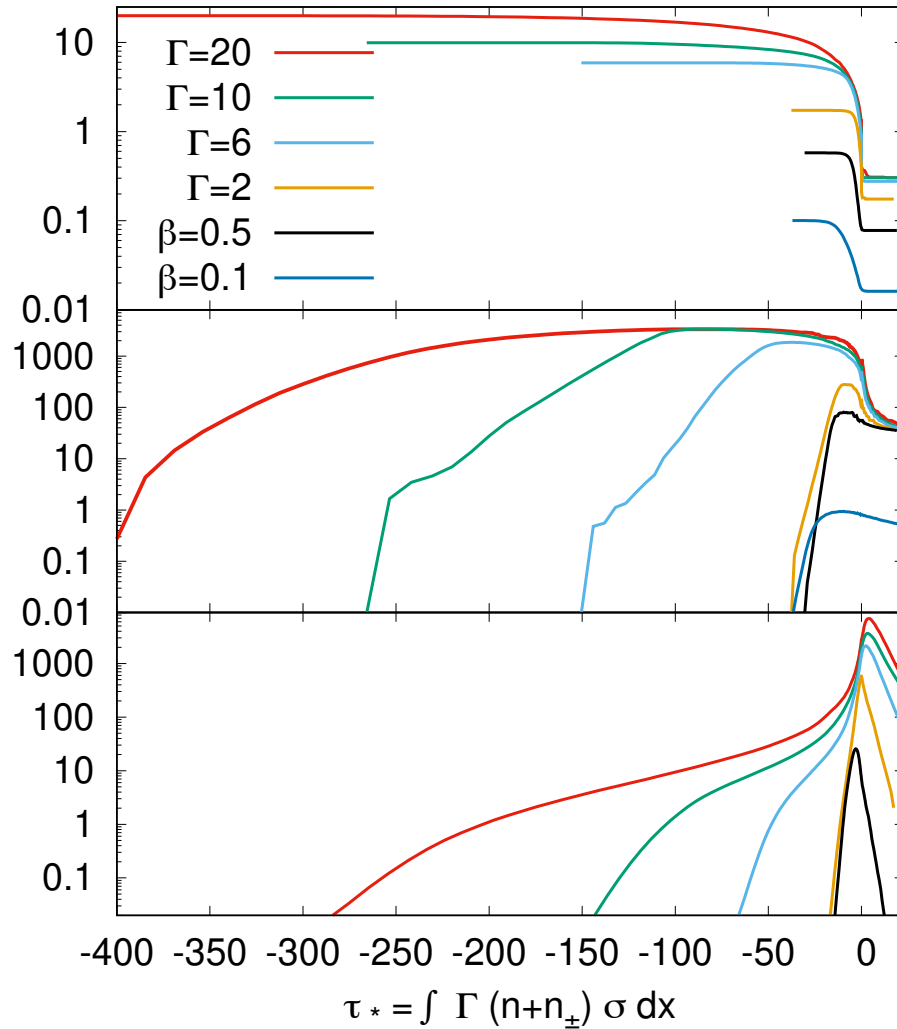
$$\Gamma_u = 2 \quad n_u = 10^{15} \text{ cm}^{-3} \quad \tilde{n} = 10$$



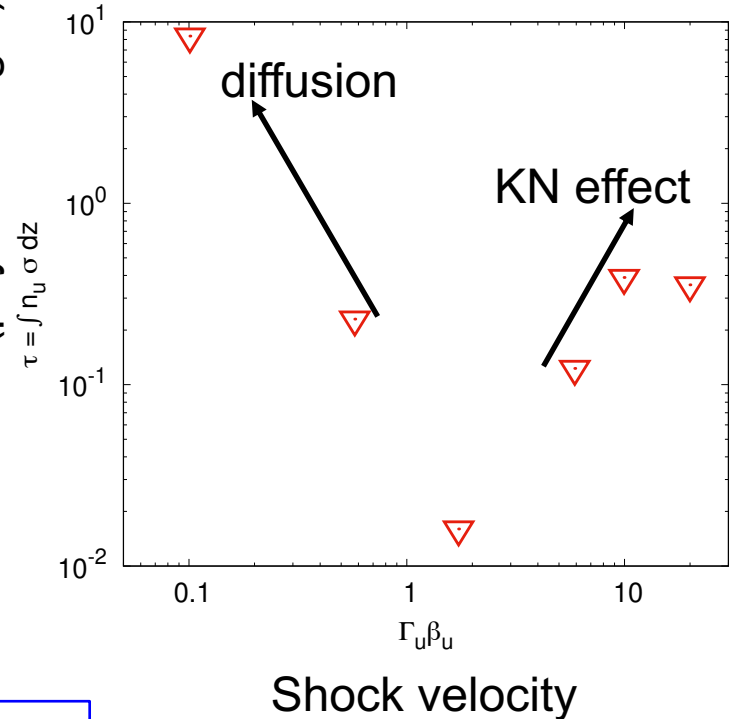
free-free emission
is source of photon

subshock is always
present for $\Gamma_u > \sim 2$

Photon Starved regime



Shock width (physical length)

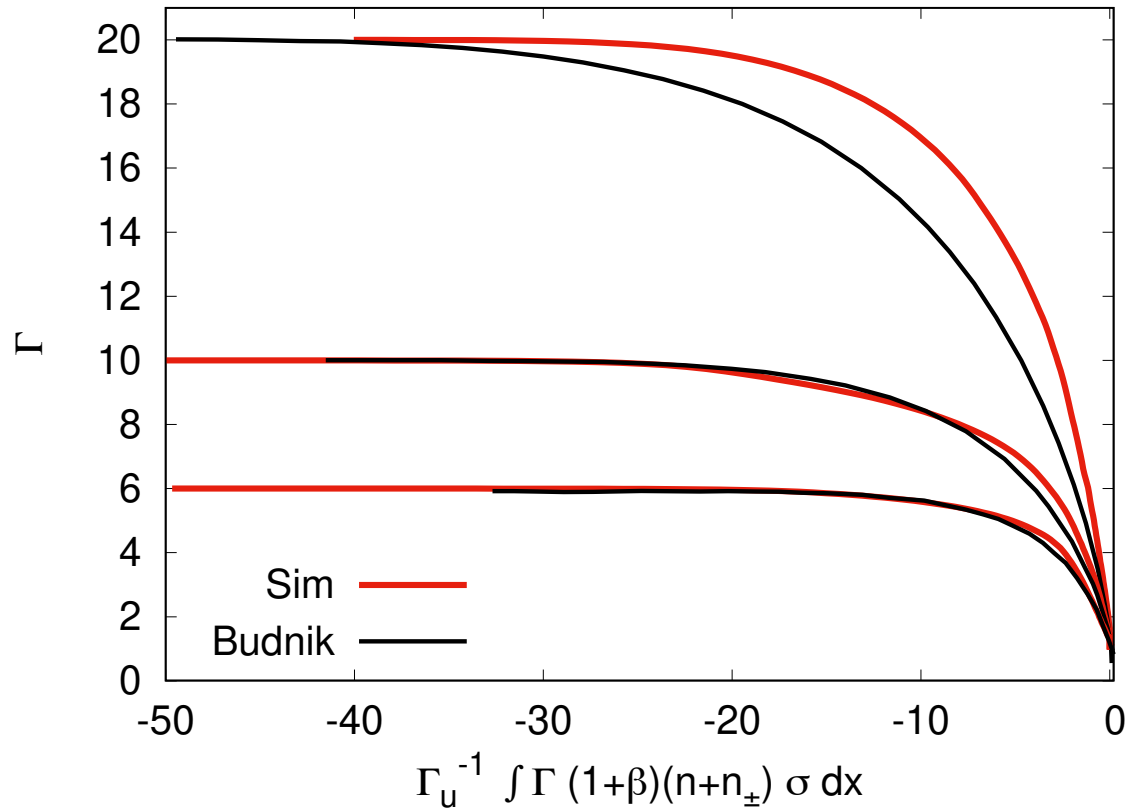


Optical depth of shock upstream at which break out starts

Photon Starved regime

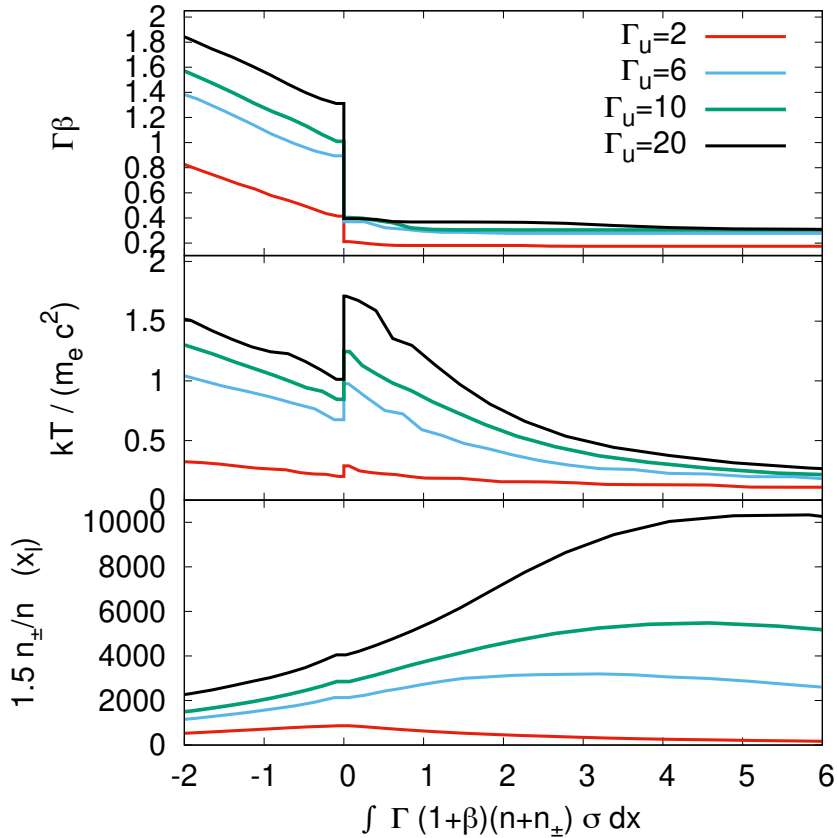
Comparison with Budnik + 2010

US region

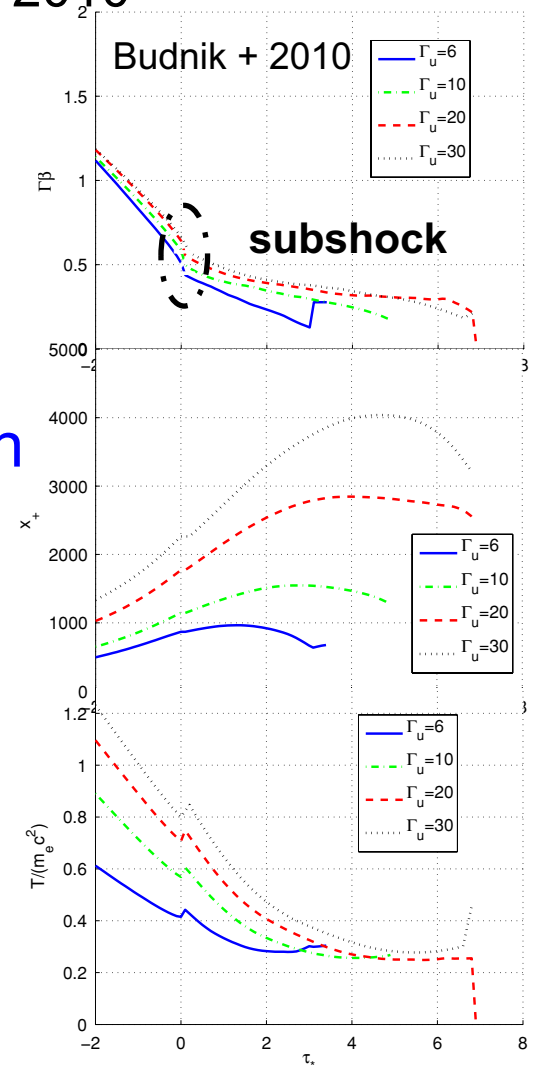


Photon Starved regime

Comparison with Budnik + 2010



DS region



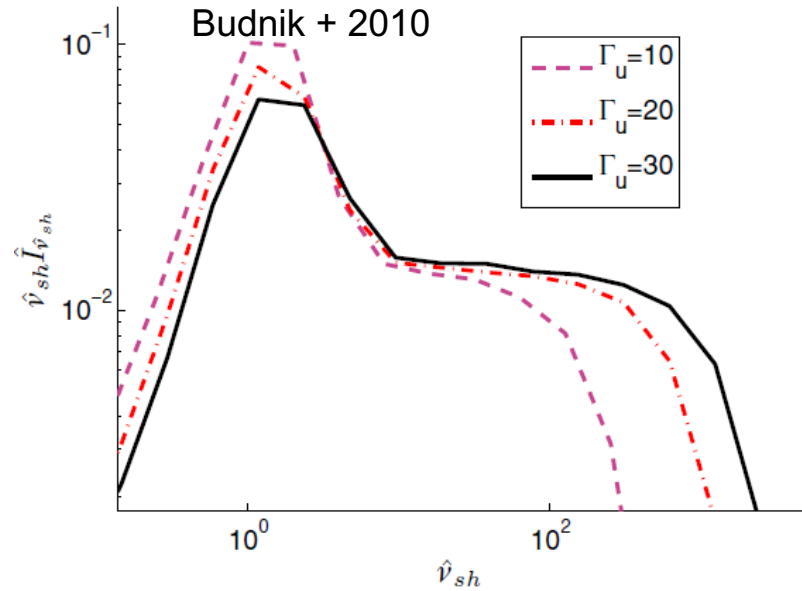
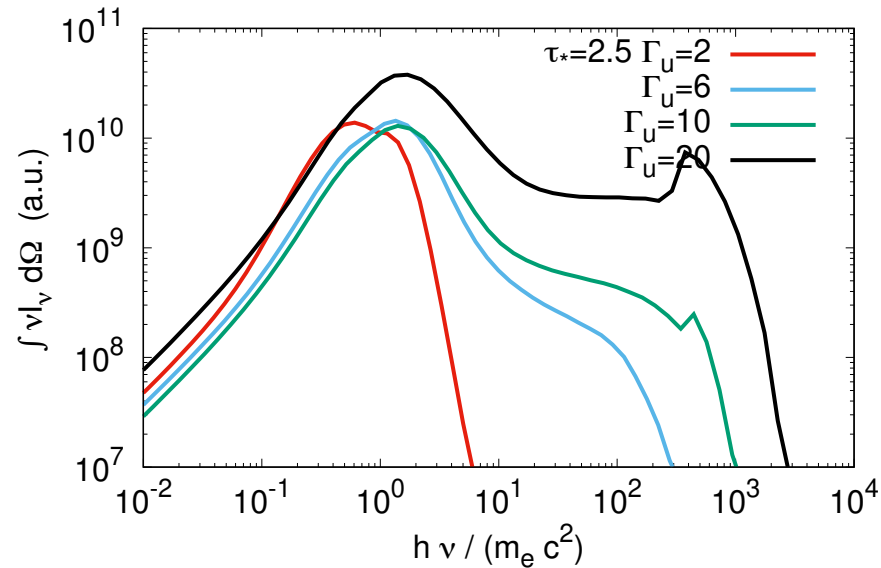
DS temperature is regulated to ~ 200 keV for $\Gamma_u \gg 1$ due to vigorous pair production

Subshock is stronger

Photon Starved regime

Comparison with Budnik + 2010

Spectrum inside the shock

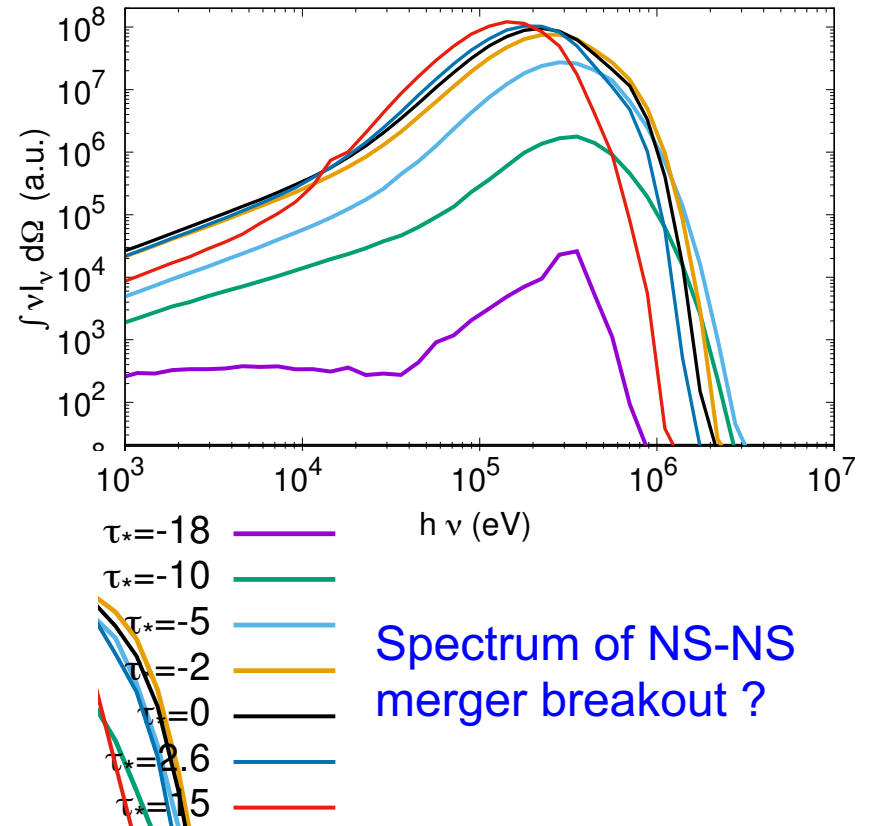
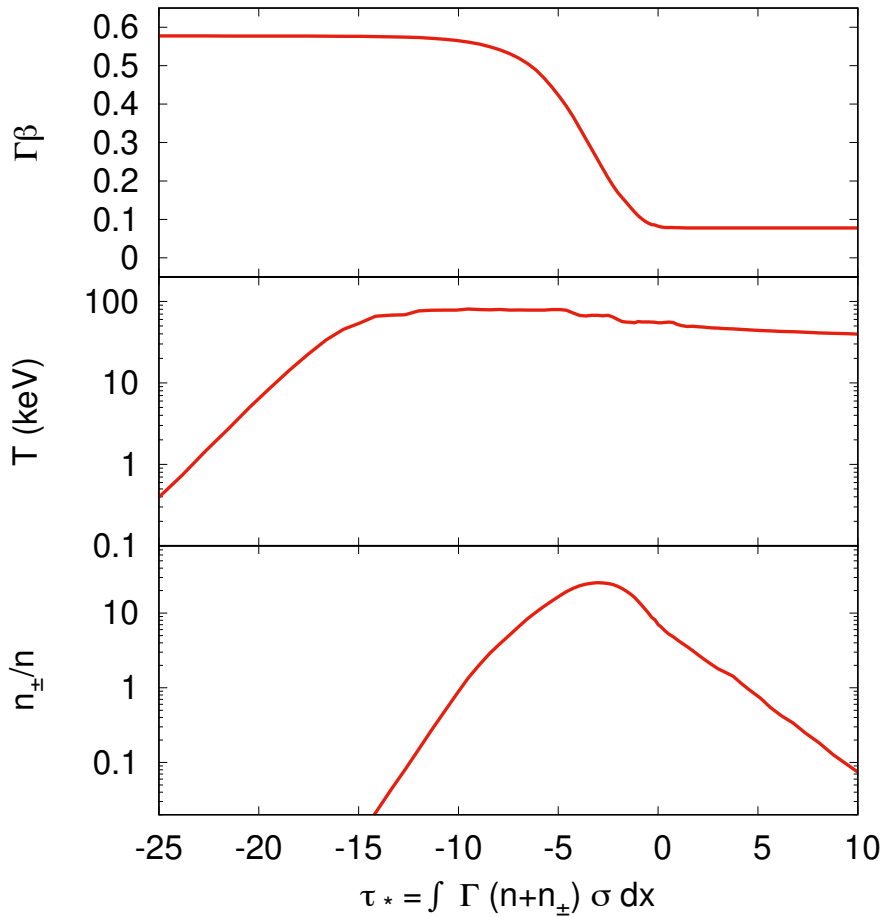


Peak position is fixed at $\sim 3 kT_d \sim 600$ keV for $\Gamma_u \gg 1$

Notable difference in the high energy spectrum

Photon Starved regime

$$\beta_u = 0.5 \quad n_u = 10^{15} \text{ cm}^{-3} \quad \tilde{n} = 10$$



Summary

Self consistent simulation of RRMS is performed

- As in the previous studies we find the deceleration length to be $\Delta\tau \sim 1$
- Strong anisotropy develops near the shock and give rise to highly non-thermal spectrum and copious pair production
- Necessity of subshock at certain regime
- Possible origin of Band spectrum
- Broad agreement with Budnik + 2010 is obtained for photon starved regime, but there is also notable difference

Future work

- photon escape calculation at photon starved regime
 - Implementation of magnetic fields
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